# Web Appendix for "Inequality in Human Capital and Endogenous Credit Constraints"\*

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January 11, 2017

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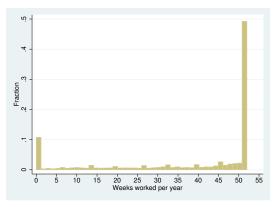
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# A Web Appendix

## A.1 Data and Basic Analysis

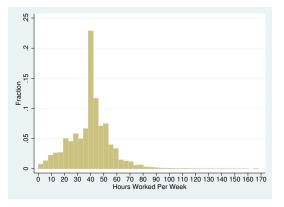
	Observation Left
Total observations for all individuals	
	124,099
Keep if male	62,620
Keep if white	30,925
Drop if missing schooling or working information for the entire sample period	25,639





Source: NLSY97 white males.

### Figure A2: Hours Worked Per Week



Source: NLSY97 white males.

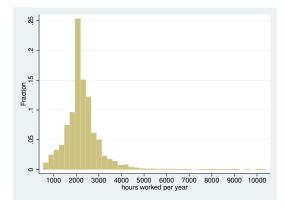


Figure A3: Total Hours Worked Per Year (Full-time Employed)

Source: NLSY97 white males.

Table A2: Descriptive Statistics of NLSY97 Sample (Years 1997 to 2011)

	mean	sd	min	max	Ν
Age	24.04	4.42	17.00	33.00	31,403
Education	12.79	2.38	9.00	20.00	$27,\!828$
Years Worked	3.27	3.49	0.00	15.00	26,821
In School	0.24	0.42	0.00	1.00	28,738
Full-Time Working	0.57	0.50	0.00	1.00	$28,\!174$
Part-Time Working	0.21	0.41	0.00	1.00	$28,\!174$
Full-Time Hourly Wage	13.93	9.44	3.00	123.55	$10,\!874$
Part-Time Hourly Wage	10.27	11.82	3.00	200.00	$4,\!609$
Net Worth	14917.95	30063.15	-75000.00	100000.00	$6,\!881$
Total Parental Transfers	803.20	2800.01	0.00	30000.00	24,882
Parents' Education	13.18	1.95	8.00	16.00	30,393
Parents' Net Worth	162988.31	186831.49	-11769.47	706168.25	24,074

Table A3: Key Variables by Education (Age 25)

	<12 yrs	12 yrs	13 to 15 yrs	>=16 yrs
Years Worked	5.71	5.30	3.79	1.75
Net Worth	14657.63	24033.25	21432.79	19242.44
Full-Time Hourly Wage	11.06	14.01	15.21	17.26
Part-Time Hourly Wage	15.15	20.78	13.99	14.59

	(1)	(2)	(3)	(4)
Years of Schooling after 4-Year College	0.0151	0.0465**	0.00989	0.0382**
	(0.018)	(0.017)	(0.015)	(0.015)
Years of Schooling $\geq 12$	$0.0926^{*}$	0.134**	0.167**	0.212**
	(0.049)	(0.048)	(0.045)	(0.044)
Years of Schooling $\geq 14$	-0.0107	$0.0535^{*}$	-0.0125	0.0533**
	(0.027)	(0.028)	(0.026)	(0.026)
Years of Schooling $\geq 16$	$0.141^{**}$	$0.224^{**}$	$0.0809^{**}$	$0.174^{**}$
	(0.042)	(0.042)	(0.035)	(0.035)
Years Worked	$0.0541^{**}$		$0.0645^{**}$	
	(0.018)		(0.016)	
Years Worked Squared	-0.000960		-0.00134	
	(0.001)		(0.001)	
Yrs Worked (Post School)		$0.0816^{**}$		$0.0807^{**}$
		(0.013)		(0.011)
Yrs Worked Squared (Post School)		$-0.00272^{**}$		$-0.00244^{**}$
		(0.001)		(0.001)
Cognitive Ability $\times$ High School Dropout	$0.0556^{*}$	$0.0504^{*}$	$0.0642^{**}$	$0.0600^{**}$
	(0.031)	(0.030)	(0.028)	(0.027)
Noncognitive Ability $\times$ High School Dropout	0.0888**	$0.0917^{**}$	0.0470	0.0483
	(0.035)	(0.035)	(0.030)	(0.030)
Cognitive Ability $\times$ Years of Schooling 12 to 15	0.0633**	0.0615**	0.0314**	0.0295**
	(0.014)	(0.014)	(0.013)	(0.013)
Noncognitive Ability $\times$ Years of Schooling 12 to 15	0.0600**	0.0609**	0.0648**	0.0667**
	(0.012)	(0.012)	(0.012)	(0.012)
Cognitive Ability $\times$ 4-Year College Graduate	0.120**	0.113**	0.141**	0.123**
	(0.027)	(0.026)	(0.022)	(0.021)
Noncognitive Ability $\times$ 4-Year College Graduate	0.0817**	0.0588**	0.103**	0.0778**
	(0.031)	(0.030)	(0.022)	(0.022)
Work Part-Time			0.0108	0.0226
Construct	0 1 C 0 **	0.007**	(0.054)	(0.053)
Constant	$2.169^{**}$	$2.087^{**}$	$2.021^{**}$	1.981**
Observations	(0.087)	(0.064)	(0.074)	(0.056)
Observations Adjusted $R^2$	2600	2693 0.1521	3534	3649
Var of Error Term	$\begin{array}{c} 0.1395 \\ 0.26 \end{array}$	$\begin{array}{c} 0.1531 \\ 0.25 \end{array}$	0.1346	$\begin{array}{c} 0.1398 \\ 0.29 \end{array}$
Var of Log Wage	$0.20 \\ 0.31$	$\begin{array}{c} 0.25\\ 0.31\end{array}$	$0.29 \\ 0.31$	$\begin{array}{c} 0.29 \\ 0.31 \end{array}$
0 0				
Mean of Log Wage	2.63	2.63	2.63	2.63

Table A4:	OLS	regression:	Log	Hourly	Wage
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Standard errors in parentheses

Columns (1)-(2): always works full-time after leaving school; Columns (3)-(4): always works after leaving school. \* p < 0.10, \*\* p < 0.05

### A.2 Additional Parameterizations

We estimate the following Tobit model as a function not only of parents' education and net worth terciles but also of individuals' decisions on schooling and employment:

$$\begin{aligned} \log(tr_{p,t}+1) &= \beta_{\text{tr},p,1} d_{e,t} \mathbf{1} (d_{e,t} + e_t \ge 13 \ \& \ d_{e,t} + e_t \le 14) \\ &+ \beta_{\text{tr},p,2} d_{e,t} \mathbf{1} (d_{e,t} + e_t \ge 15 \ \& \ d_{e,t} + e_t \le 16) + \beta_{\text{tr},p,3} d_{e,t} \mathbf{1} (d_{e,t} + e_t > 16) \\ &+ \beta_{\text{tr},p,4} \mathbf{1} (d_{k,t} = 0 \ \& \ d_{e,t} = 0) \\ &+ \beta_{\text{tr},p,5} t + \beta_{\text{tr},p,6} t \cdot d_{e,t} \mathbf{1} (d_{e,t} + e_t \ge 13) + \beta_{\text{tr},p,7} \mathbf{1} (t = 17) + \beta_{\text{tr},p,8} \mathbf{1} (t > 23) \\ &+ \beta_{\text{tr},p,5} t + \beta_{\text{tr},p,6} t \cdot d_{e,t} \mathbf{1} (d_{e,t} + e_t \ge 13) + \beta_{\text{tr},p,7} \mathbf{1} (t = 17) + \beta_{\text{tr},p,8} \mathbf{1} (t > 23) \\ &+ \beta_{\text{tr},p,9} \mathbf{1} (s_p = T2) + \beta_{\text{tr},p,10} \mathbf{1} (s_p = T3) \\ &+ \beta_{\text{tr},p,11} \mathbf{1} (e_p = 12) + \beta_{\text{tr},p,12} \mathbf{1} (e_p \ge 13 \ \& \le 15) \\ &+ \beta_{\text{tr},p,13} \mathbf{1} (e_p \ge 16) + \beta_{\text{tr},p,14} \mathbf{1} (e_p \ge 16 \ \& s_p = T3) \\ &+ \beta_{\text{tr},p,15} \mathbf{1} (e_p = 12) d_{e,t} \mathbf{1} (d_{e,t} + e_t \ge 13) \\ &+ \beta_{\text{tr},p,16} \mathbf{1} (e_p \ge 13 \ \& \le 15) d_{e,t} \mathbf{1} (d_{e,t} + e_t \ge 13) \\ &+ \beta_{\text{tr},p,17} \mathbf{1} (e_p \ge 16) d_{e,t} \mathbf{1} (d_{e,t} + e_t \ge 13) \\ &+ \beta_{\text{tr},p,18} \theta_c + \beta_{\text{tr},p,19} \theta_n + \beta_{\text{tr},p,0} + \epsilon_{p,t}. \end{aligned}$$

In our data, we do not observe parental transfers beyond age 30. However, given that we are focusing on parental transfer targeting the youth's college education, it is reasonable to assume that parental transfers are zero for a youth after age 30 due to data limitation, i.e.  $tr_{p,t} = 0$  for  $t \ge 30$ . This assumption is appropriate as we focus on the role of parental transfer on young adults' college attainment and the majority of individuals obtain their college degree before age 30. For the same reason, here we only focus on non-negative parental transfers. Negative parental transfers may be important for older adults and their parents for a different purpose, but it is outside the scope of this paper.

Parental consumption subsidy is given as  $tr_{c,t} = \chi \cdot \mathbf{1}(t < 18)$ , where  $\chi$  is the value of direct consumption subsidy provided by the parents such as shared housing and meals when

the youth attends high school.

Government transfers,  $tr_{g,t}$ , are comprised of two components: an unemployment benefit component  $tr_{g,t}^b$  that is offered for individuals who are currently unemployed ( $\mathbf{1}(d_{k,t} = 0 \& d_{e,t} = 0)$ ), and a means-tested component  $tr_{g,t}^c$  that supports a minimum consumption floor  $c_{min}$ : i.e.,  $tr_{g,t} = tr_{g,t}^b \mathbf{1}(d_{k,t} = 0 \& d_{e,t} = 0) + tr_{g,t}^c$ .

Government means-tested transfers  $tr_{g,t}^c$  bridge the gap between an individual's available financial resources and the consumption floor  $c_{min}$ . Hubbard, Skinner, and Zeldes (1995), Keane and Wolpin (2001), and French and Jones (2011) show that allowing for the effects of means-tested benefits is important in understanding savings behavior of poor households.

## A.3 Parameter Estimates

	(1)	
In First/Second Year College	$6.534^{**}$	(0.657)
In Third/Fourth Year College	$7.713^{**}$	(0.712)
In Graduate School	$6.768^{**}$	(0.795)
Unemployed	$0.258^{**}$	(0.076)
Age	$-0.215^{**}$	(0.014)
Age * in School	-0.286**	(0.030)
Age 17	$-0.753^{**}$	(0.102)
> Age 23	$-0.173^{*}$	(0.097)
Parents' Net Worth T2	-0.078	(0.086)
Parents' Net Worth T3	0.096	(0.092)
Parents' Schooling 12 Years	0.042	(0.079)
Parents' Schooling 13 to 15 Years	$0.402^{**}$	(0.079)
Parents' Schooling $\geq 16$ Years	$0.813^{**}$	(0.116)
Parents' Schooling $\geq 16$ Years * Parents' Net Worth T3	$0.363^{**}$	(0.123)
Parents' Schooling 12 Years * in School	$1.076^{**}$	(0.278)
Parents' Schooling 13 to 15 Years $*$ in School	$1.319^{**}$	(0.260)
Parents' Schooling $\geq 16$ Years * in School	$1.667^{**}$	(0.267)
Cognitive Ability	$0.134^{**}$	(0.026)
Noncognitive Ability	$0.149^{**}$	(0.042)
Constant	$6.309^{**}$	(0.307)
Observations	14788	
$R^2$	0.252	

Standard errors in parentheses

Parental transfers are in 2004 dollars.

\* p < 0.10,\*\* p < 0.05

	$\theta_c$ : Cognitive	$\theta_n$ : Noncognitive			
	Mean				
Parents Wealth 3rd Tercile	0.304	1.507			
	(0.050)	(0.093)			
Parents Wealth 2nd Tercile	0.000	1.027			
	(0.050)	(0.085)			
Parents 4-Yr College	0.354	1.378			
	(0.069)	(0.141)			
Parents Some College	0.314	0.782			
	(0.043)	(0.077)			
Parents High School	0.241	0.570			
	(0.055)	(0.107)			
Constant	-0.541	-1.545			
	(N.A.)	(N.A.)			
	Varia	nce Matrix			
$\theta_c$ : Cognitive	1.000				
	(N.A.)				
$\theta_n$ : Noncognitive	0.280	1.000			
	(0.050)	(N.A.)			

Table A6: Parameter Estimates of Joint Initial Distribution of  $(\theta_c, \theta_c)^*$ 

Constant terms are normalized such that  $\mathbb{E}(\theta_c) = \mathbb{E}(\theta_n) = 0$ . \*Standard errors in parentheses.

	ASVAB: Arithmetic Reasoning	ASVAB: Mathematics Knowledge	ASVAB: Paragraph Comprehen- sion	ASVAB: Word Knowledge	Noncognitive: Violent Behavior (1997)	Noncognitive: Had Sex bef. Age 15	Noncognitive: Theft Behavior (1997)
Cognitive Ability	0.743 ( 0.013 )	0.696 ( 0.015 )	0.654 ( 0.017 )	0.569 ( $0.015$ )			
Noncognitive Ability				. ,	-0.661 ( 0.035 )	-1.181 ( 0.079 )	-0.369 ( $0.029$ )
Age in 1997	0.151 ( 0.001 )	0.255 ( $0.001$ )	$\begin{array}{c} 0.152 \\ ( \ 0.001 \ ) \end{array}$	0.192 ( 0.001 )	0.103 ( $0.003$ )	0.104 ( 0.005 )	0.097 ( $0.002$ )
Parental Wealth 3rd Tercile	(0.069) 0.024	$0.134 \\ 0.026$	$0.084 \\ 0.026$	$0.017 \\ 0.028$	$0.567 \\ 0.088$	$1.012 \\ 0.170$	$0.448 \\ 0.055$
Parental Wealth 2nd Tercile	0.193 ( $0.027$ )	0.203 ( $0.025$ )	0.242 ( 0.028 )	0.179 ( $0.029$ )	0.435 ( $0.081$ )	0.814 ( 0.134 )	0.236 ( $0.057$ )
Parents' Yrs of Schooling	0.106 ( 0.001 )	0.110 ( 0.001 )	0.108 ( 0.001 )	0.115 ( 0.001 )	(0.030) (0.004)	-0.014 ( 0.006 )	0.018 ( 0.002 )
Constant	-4.114 ( 0.015 )	-5.600 ( 0.015 )	-4.228 ( 0.015 )	-4.932 ( 0.016 )	-2.218 ( 0.047 )	-2.094 (0.080)	-2.190 ( 0.030 )
Measurement Error SD	0.426 ( 0.012 )	0.448 ( 0.011 )	0.492 ( 0.011 )	0.518 ( 0.010 )	0.978 ( 0.059 )	1.452 ( 0.096 )	0.463 ( 0.026 )

Table A7: Parameter Estimates of Measurement Equations

		Our Model		Alternativ	ve Model
Description	Parameter	Estimate	S.E.	Estimate	S.E.
Pa	anel A: $d_{e,t} \cdot u_e$	$_{e}(\Omega_{t})$			
Attending High School	$\phi_{e,0}$	0.4386	0.0113	0.4510	0.0102
Attending College	$\phi_{e,1}$	0.0000	0.0049	-0.0172	0.0029
Attending College After Age 23	$\phi_{e,a}$	-0.1868	0.0075	-0.1605	0.0041
Attending Graduate School	$\phi_{e,2}$	-0.4275	0.0066	-0.4477	0.0033
Schooling $\times$ Cognitive Ability	$\alpha_{e,c}$	0.1825	0.0033	0.2537	0.0018
Schooling $\times$ Noncognitive Ability	$\alpha_{e,n}$	0.2160	0.0041	0.2508	0.0023
Schooling $\times$ Parents 4-Year College	$\phi_{e,p}$	0.0699	0.0061	0.0050	0.0030
Psychic Cost of Returning to School	$\phi_{e,e}$	0.3596	0.0059	0.6515	0.0042
S.D. of Preference Shock to Schooling	$\sigma_{e}$	0.1675	0.0039	0.1000	0.0036
Pane	el B: $u_k(d_{k,t}, d)$	$(e_{e,t}, \Omega_t)$			
Working Part Time When in School	$\phi_{k,e}$	-0.0773	0.0020	-0.0603	0.0014
Working Part Time When Not in School	$\phi_{k,0}$	-0.0332	0.0010	-0.0338	0.0008
Working Full Time	$\phi_{k,1}$	-0.0822	0.0010	-0.0615	0.0007
Working Full Time $\times$ Age	$\phi_{k,2}$	0.0029	0.0001	0.0006	0.0001
Working $\times$ Cognitive Ability	$\alpha_{k,c}$	-0.0637	0.0029	-0.0237	0.0084
Working $\times$ Noncognitive Ability	$lpha_{k,n}$	-0.0814	0.0048	-0.0942	0.0048

Table A8: Parameter Estimates of Flow Utility Function on Schooling and Working (Our Model *vs.* Alternative Model)

 $\begin{aligned} u_e = &\phi_{e,0} \mathbf{1} (d_{e,t} + e_t \le 12) + (\phi_{e,1} + \phi_{e,a} \mathbf{1} (t > 22)) \cdot \mathbf{1} (d_{e,t} + e_t > 12 \& d_{e,t} + e_t \le 16) + \phi_{e,2} \mathbf{1} (d_{e,t} + e_t > 16) \\ &+ \alpha_{e,c} \theta_c + \alpha_{e,n} \theta_n + \phi_{e,p} (e_p - 12) \mathbf{1} (e_p > 12) - \phi_{e,e} (1 - d_{e,t-1}) + \sigma_e \epsilon_{e,t} \\ u_k = &[\phi_{k,e} \cdot \mathbf{1} (d_{k,t} = 0.5 \& d_{e,t} = 1) + \phi_{k,0} \cdot \mathbf{1} (d_{k,t} = 0.5 \& d_{e,t} = 0) + \mathbf{1} (d_{k,t} = 1) \cdot (\phi_{k,1} + \phi_{k,2} (age - 17)) \\ &\cdot (1 + \alpha_{k,c} \theta_c + \alpha_{k,n} \theta_n) \end{aligned}$ 

Table A9: Subjective Discount Rate:  $\rho(\theta_c, \theta_n) = \rho_0(1 - \rho_c \theta_c - \rho_n \theta_n)$  (Our Model *vs.* Alternative Model)

		Our Model		Alternative Model		
Description	Parameter	Estimate	S.E.	Estimate	S.E.	
Cognitive Ability	$ ho_c$	0.0874	0.0086	0.0963	0.0127	
Noncognitive Ability	$ ho_n$	0.2910	0.0109	0.1733	0.0128	
Level Parameter	$ ho_0$	0.0245	0.0012	0.0210	0.0008	

The associated discount factor is  $\exp(-\rho(\theta_c, \theta_n)) = 0.9758$  in our model and  $\exp(-\rho(\theta_c, \theta_n)) = 0.9792$  in alternative model.

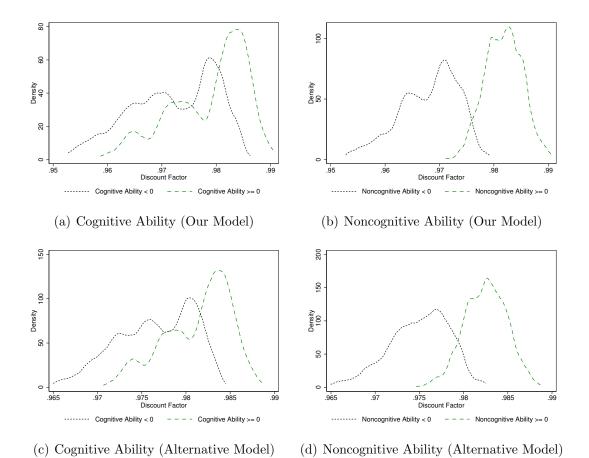


Figure A4: Density of Estimated Discount Factors by Abilities:  $\exp(-\rho(\theta_c, \theta_n))$  (Our Model *vs.* Alternative Model)

Table A10: Parameter Estimates on Human Capital Production Function and Wage Equation (Our Model vs. Alternative Model)

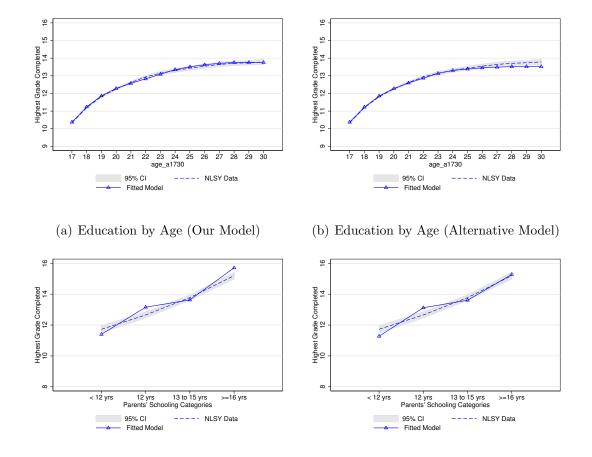
		Our M	lodel	Alternati	ve Model
Description	Parameter	Estimate	S.E.	Estimate	S.E.
Intercept Parameter	$\beta_{\psi,0}$	1.8884	0.0018	1.9072	0.0042
Experience	$\beta_{\psi,k}$	0.0767	0.0002	0.0533	0.0005
Experience Squared/100	$\beta_{\psi,kk}$	-0.2683	0.0013	-0.2718	0.0019
Years of Schooling $-12$	$\beta_{\psi,e,0}$	0.0465	0.0005	0.0610	0.0020
Years of Schooling $= 12$	$\beta_{\psi,e,1}$	0.1432	0.0026	0.1320	0.0037
Years of Schooling $> 12, < 16$	$\beta_{\psi,e,2}$	0.1435	0.0015	0.1393	0.0041
Years of Schooling $\geq 16$	$\beta_{\psi,e,3}$	0.2806	0.0031	0.2873	0.0044
Cognitive Ability $\times$ (Years of Schooling $< 12$ )	$\alpha_{\psi,c,0}$	0.0529	0.0034	0.0322	0.0070
Cognitive Ability × (Years of Schooling $\geq 12, < 16$ )	$\alpha_{\psi,c,1}$	0.0529	0.0031	0.0322	0.0058
Cognitive Ability $\times$ (Years of Schooling $\geq 16$ )	$\alpha_{\psi,c,2}$	0.1433	0.0028	0.0922	0.0048
Noncognitive Ability $\times$ (Years of Schooling $< 12$ )	$\alpha_{\psi,n,0}$	0.0275	0.0076	0.0304	0.0035
Noncognitive Ability $\times$ (Years of Schooling $\geq 12, < 16$ )	$\alpha_{\psi,n,1}$	0.0512	0.0017	0.0623	0.0029
Noncognitive Ability $\times$ (Years of Schooling $\geq 16$ )	$\alpha_{\psi,n,2}$	0.0892	0.0017	0.0723	0.0036
Part-Time	$\beta_{w,0}$	-0.0082	0.0263	-0.0099	0.0086
Part-Time $\times$ Enroll	$\beta_{w,1}$	-0.4863	0.0042	-0.5210	0.0058
Scale Parameter of Productivity Shock (Years of Schooling $< 16$ )	$b_0$	0.1388	0.0051	0.1392	0.0013
Scale Parameter of Productivity Shock (Years of Schooling $\geq 16$ )	$b_1$	0.1424	0.0007	0.1384	0.0018
Shape Parameter of Productivity Shock (Years of Schooling $< 16$ )	$a_0$	15.3558	0.4056	19.8838	0.3523
Shape Parameter of Productivity Shock (Years of Schooling $\geq 16$ )	$a_1$	15.8092	0.0615	21.4807	0.4661
Depreciation Rate of Experience	$\delta_k$	0.1135	0.0022	0.1880	0.0035

$$\begin{split} \log \psi_t = & \beta_{\psi,0} + \beta_{\psi,k} k_t + \beta_{\psi,kk} k_t^2 / 100 + \beta_{\psi,e,0} (e_t - 12) \\ & + \beta_{w,e,1} \mathbf{1} (e_t = 12) + \beta_{w,e,2} \mathbf{1} (e_t > 12 \& e_t < 16) + \beta_{w,e,3} \mathbf{1} (e_t \ge 16) \\ & + (\alpha_{\psi,c,0} \theta_c + \alpha_{\psi,n,0} \theta_n) \cdot \mathbf{1} (e_t < 12) \\ & + (\alpha_{\psi,c,1} \theta_c + \alpha_{\psi,n,1} \theta_n) \cdot \mathbf{1} (e_t \ge 12 \& e_t < 16) \\ & + (\alpha_{\psi,c,2} \theta_c + \alpha_{\psi,n,2} \theta_n) \cdot \mathbf{1} (e_t \ge 16) + \epsilon_{w,t} - \mathbb{E} (\epsilon_{w,t}) \\ & \log w_t = \log \psi_t + \mathbf{1} (d_{k,t} = 0.5) (\beta_{w,0} + \beta_{w,1} d_{e,t}). \end{split}$$

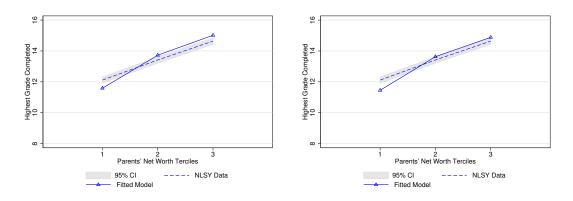
The density of productivity shock  $\epsilon_{w,t}$  is:

$$p(\epsilon_{w,t}) = \frac{1}{\Gamma(a)b^a} (\epsilon_{w,t})^{a-1} e^{-(\epsilon_{w,t})/b}.$$
(2)

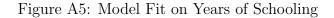
### A.4 Model Goodness of Fit



(c) Education by Parental Education (Our (d) Education by Parental Education (Alterna-Model) tive Model)



(e) Education by Parental Wealth (Our Model) (f) Education by Parental Wealth (Alternative Model)



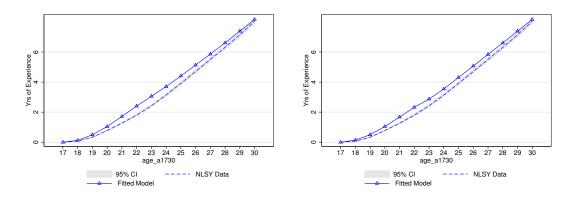




Figure A6: Model Fit on Years Worked

Table fill, model in, Emean regression on Emerne	Table A11:	Model Fi	t: Linear	<sup>•</sup> Regression	on Enrollment
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	Our Model	Alternative Model	Data	Data S.E.
Previously in School	0.3265	0.4337	0.474	0.010
Age	-0.0377	-0.0239	-0.033	0.004
Age = 17	0.2347	0.2025	0.186	0.014
Parental Education	0.0847	0.0406	0.082	0.011
Cognitive Ability	0.0837	0.0877	0.051	0.004
Noncognitive Ability	0.1101	0.1073	0.058	0.005

Note: Cognitive ability and noncognitive ability are estimated factor scores from the first stage. Parameter estimate on the constant term is not reported here.

Table A12: Model Fit: Linear Regression on Full-Time Employment

	Our Model	Alternative Model	Data	Data S.E.
Years of Schooling	0.0235	0.0206	0.013	0.002
Cognitive Ability	0.0006	0.0066	0.005	0.004
Noncognitive Ability	0.0140	0.0092	0.009	0.004

Note: Cognitive ability and noncognitive ability are estimated factor scores from the first stage. Parameter estimate on the constant term is not reported here.

	Our Model	Alternative Model	Data	Data S.E.
Years Worked	0.0973	0.0873	0.076	0.011
Years Worked Squared	-0.3424	-0.4498	-0.164	0.093
Years of Schooling	0.0130	0.0533	0.043	0.011
Years of Schooling $= 12$	0.1253	0.0995	0.146	0.041
Years of Schooling $> 12, < 16$	0.1536	0.1381	0.150	0.054
Years of Schooling $\geq 16$	0.3839	0.3477	0.269	0.078
Cognitive Ability $\times$ (Years of Schooling $< 12$ )	0.0537	0.0101	0.031	0.024
Noncognitive Ability $\times$ (Years of Schooling $< 12$ )	0.0334	-0.0078	0.022	0.021
Cognitive Ability $\times$ (Years of Schooling $\geq 12, < 16$ )	0.0629	0.0524	0.031	0.016
Noncognitive Ability $\times$ (Years of Schooling $\geq 12, < 16$ )	0.0623	0.0667	0.074	0.015
Cognitive Ability $\times$ (Years of Schooling $\geq 16$ )	0.1194	0.0539	0.116	0.019
Noncognitive Ability $\times$ (Years of Schooling $\geq 16$ )	0.0707	0.0274	0.057	0.019
Previously Not Working	-0.0443	-0.0594	-0.089	0.037
Std Dev*	0.5383	0.5489	0.541	0.006

#### Table A13: Model Fit: Log Hourly Wage Regression

Note: Cognitive ability and noncognitive ability are estimated factor scores from the first stage.

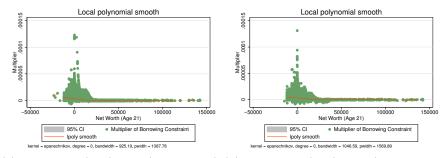
Parameter estimate on the constant term is not reported here.

\*Square root of error variance.

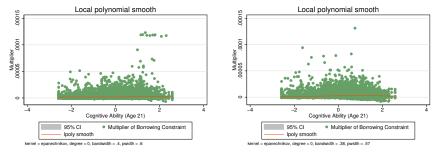
	Our Model	Alternative Model	Data	Data S.E.
Cognitive Ability	-0.0075	-0.0556	0.003	0.036
Noncognitive Ability	0.0969	-0.0510	0.220	0.033
Log Wage	0.8114	0.4297	0.636	0.061
Age > 20	0.5116	1.2872	0.352	0.079
Age $>25$	0.5747	0.2636	0.544	0.089

Note: Cognitive ability and noncognitive ability are estimated factor scores from the first stage. Parameter estimate on the constant term is not reported here.

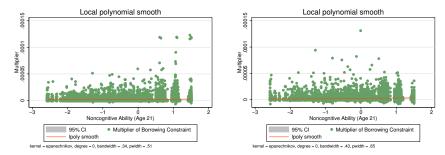
# A.5 Additional Results



(a) Multiplier  $(\lambda_{s,t})$  vs  $s_t$  (Our Model) (b) Multiplier  $(\lambda_{s,t})$  vs  $s_t$  (Alternative Model)



(c) Multiplier  $(\lambda_{s,t})$  vs  $\theta_c$  (Our Model) (d) Multiplier  $(\lambda_{s,t})$  vs  $\theta_c$  (Alternative Model)



(e) Multiplier  $(\lambda_{s,t})$  vs  $\theta_n$  (Our Model) (f) Multiplier  $(\lambda_{s,t})$  vs  $\theta_n$  (Alternative Model)

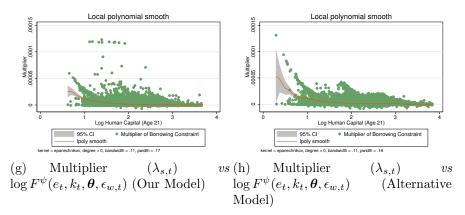
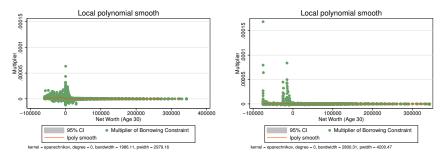
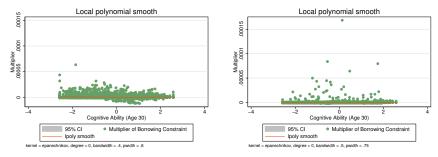


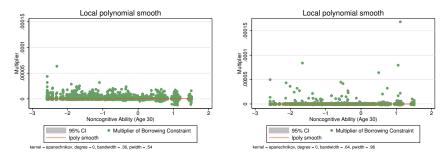
Figure A7: Kuhn-Tucker Multiplier of the Borrowing Constraint at Age 21



(a) Multiplier  $(\lambda_{s,t})$  vs  $s_t$  (Our Model) (b) Multiplier  $(\lambda_{s,t})$  vs  $s_t$  (Alternative Model)



(c) Multiplier  $(\lambda_{s,t})$  vs  $\theta_c$  (Our Model) (d) Multiplier  $(\lambda_{s,t})$  vs  $\theta_c$  (Alternative Model)



(e) Multiplier  $(\lambda_{s,t}) vs \theta_n$  (Our Model) (f) Multiplier  $(\lambda_{s,t}) vs \theta_n$  (Alternative Model)

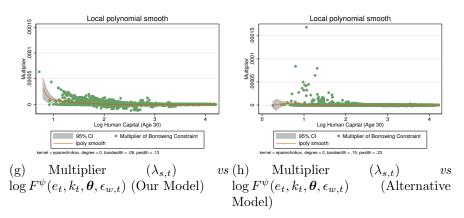
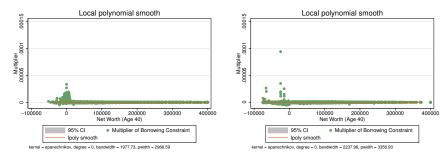
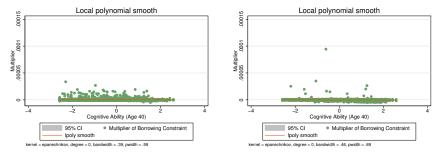


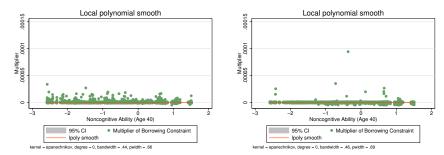
Figure A8: Kuhn-Tucker Multiplier of the Borrowing Constraint at Age 30



(a) Multiplier  $(\lambda_{s,t})$  vs  $s_t$  (Our Model) (b) Multiplier  $(\lambda_{s,t})$  vs  $s_t$  (Alternative Model)



(c) Multiplier  $(\lambda_{s,t})$  vs  $\theta_c$  (Our Model) (d) Multiplier  $(\lambda_{s,t})$  vs  $\theta_c$  (Alternative Model)



(e) Multiplier  $(\lambda_{s,t}) vs \theta_n$  (Our Model) (f) Multiplier  $(\lambda_{s,t}) vs \theta_n$  (Alternative Model)

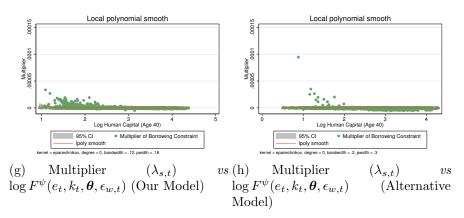
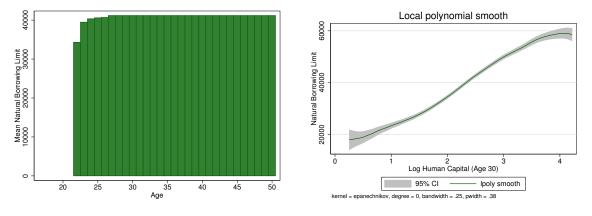
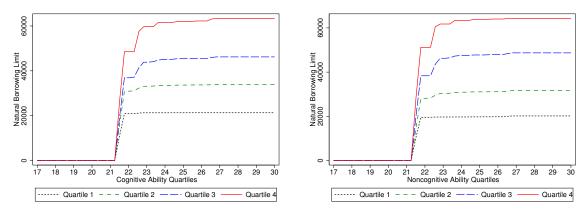


Figure A9: Kuhn-Tucker Multiplier of the Borrowing Constraint at Age 40



(a) Fixed Borrowing Limit over Ages 17 to 50 (b) Fixed Borrowing Limit vs Human Capital

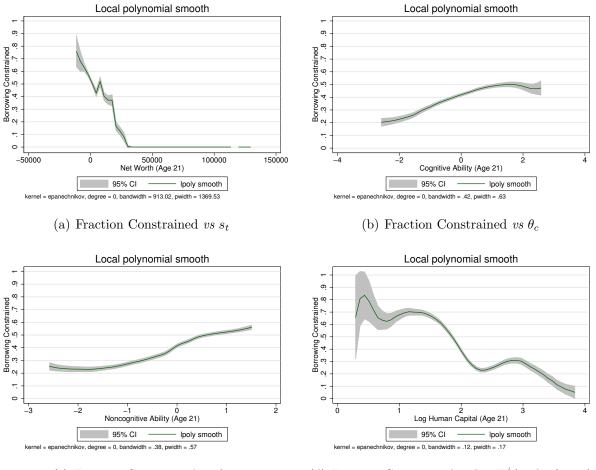
Figure A10: Mean of Borrowing Limit  $\bar{L}_t^s(e_{t+1}, k_{t+1}, \theta)$  for Alternative Model



(a) Fixed Borrowing Limit vs Cognitive Ability

(b) Fixed Borrowing Limit vs Noncog. Ability

Figure A11: Evolution of Average Borrowing Limit by Ability Endowments for Alternative Model



(c) Fraction Constrained  $vs \theta_n$ 

(d) Fraction Constrained vs log  $F^{\psi}(e_t, k_t, \boldsymbol{\theta}, \epsilon_{w,t})$ 

Figure A12: Borrowing Constrained Youths  $(s_{t+1} \leq -\bar{L}_t^s(e_{t+1}, k_{t+1}, \theta) \& \lambda_{s,t} > 0)$  at Age 21 for Alternative Model

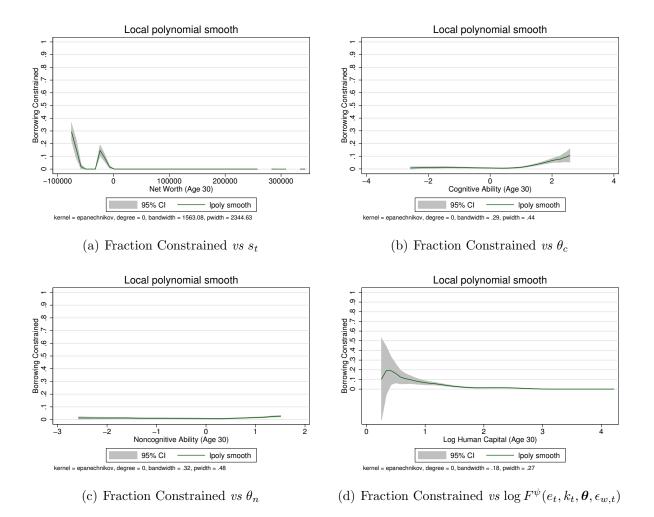


Figure A13: Borrowing Constrained Youths  $(s_{t+1} \leq -\bar{L}_t^s(e_{t+1}, k_{t+1}, \theta) \& \lambda_{s,t} > 0)$  at Age 30 for Alternative Model

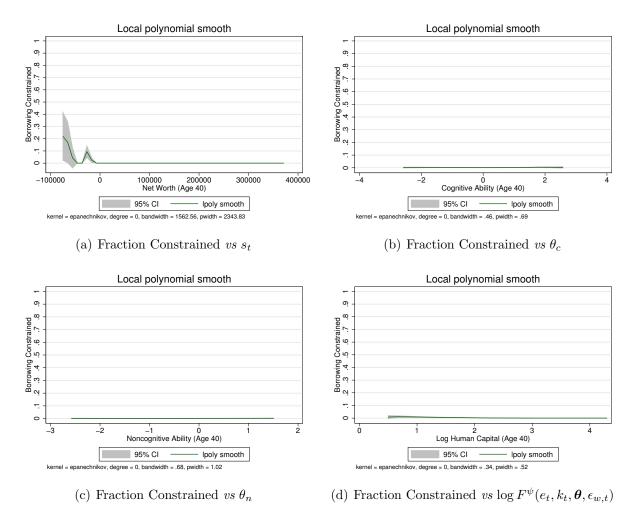
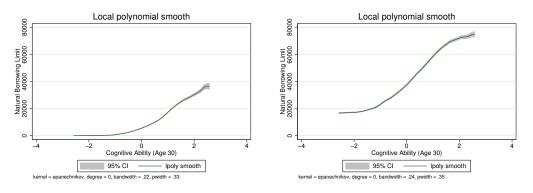


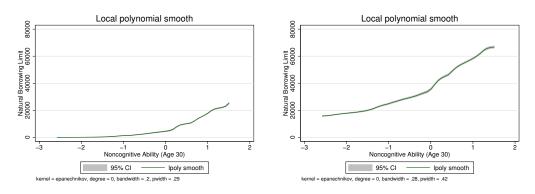
Figure A14: Borrowing Constrained Youths  $(s_{t+1} \leq -\bar{L}_t^s(e_{t+1}, k_{t+1}, \theta) \& \lambda_{s,t} > 0)$  at Age 40 for Alternative Model

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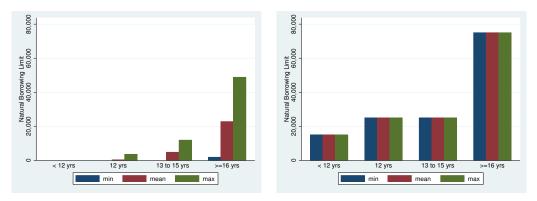
On average, the average natural borrowing limits increase with cognitive ability, noncognitive ability, and education for both our model and alternative model. However, there is substantial heterogeneity in the amount of natural borrowing limit within each education category.



(a) Natural Borrowing Limit & Cognitive (b) Fixed Borrowing Limit & Cognitive Abil-Ability at Age 30 (Our Model) ity at Age 30 (Alternative Model)



(c) Fixed Borrowing Limit & Noncognitive (d) Fixed Borrowing Limit & Noncognitive Ability at Age 30 (Our Model) Ability at Age 30 (Alternative Model)



(e) Fixed Borrowing Limit & Education at (f) Fixed Borrowing Limit & Education at Age 30 (Our Model) Age 30 (Alternative Model)

Figure A15: Fixed Borrowing Limit & Education (Age 30)

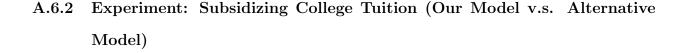
## A.6 Counterfactual Experiments

#### A.6.1 Equalizing Initial Endowments

Table A15: Inequality in Education, Wages, and Consumption under Different Experiments at Age 30 (Our Model)

	Inequality (Var of log)			Changes in Inequality $(\%)$			
-	Educ	Wage	С	Educ	Wage	С	
Benchmark	0.0395	0.3313	0.1002	N.A.	N.A.	N.A.	
	Counterfactual Experiments						
Subsidizing College Tuition	0.0389	0.3319	0.1010	-1.43	0.17	0.79	
Increasing Student Loan Limits	0.0397	0.3346	0.1116	0.57	0.98	11.39	

Note: Inequality in Education (Educ), wages, and consumption (C) are measured using variance of log years of schooling, log hourly wage rates, and log consumption at age 30, respectively. Changes in inequality is calculated as the percentage changes in inequality compared to the benchmark model.



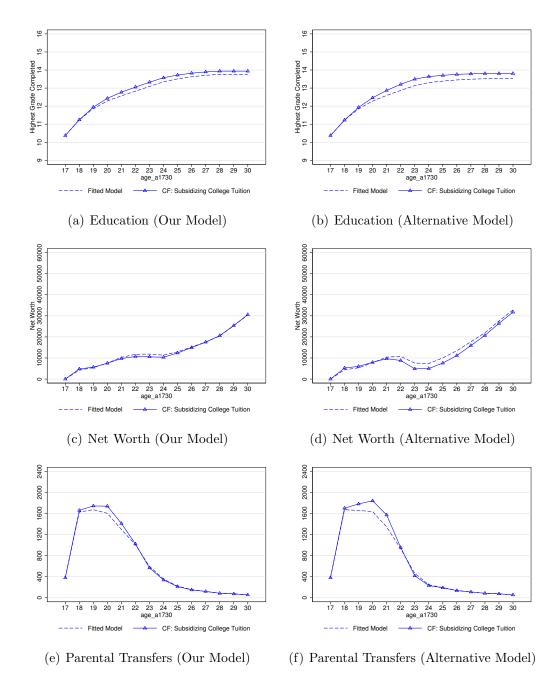


Figure A16: Counterfactual Simulation of Subsidizing College Tuition on Education, Net Worth, and Transfers

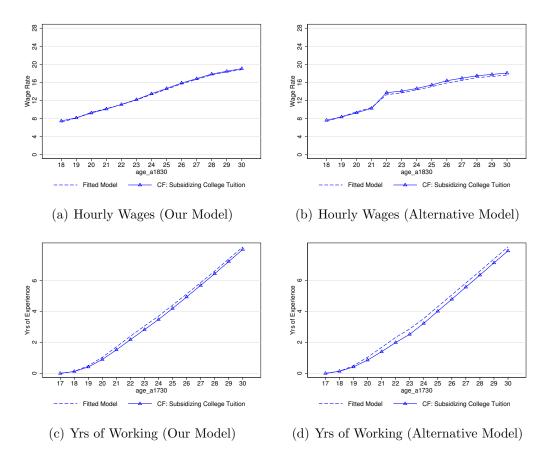
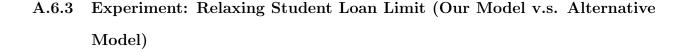


Figure A17: Counterfactual Simulation of Subsidizing College Tuition on Wage and Years of Working



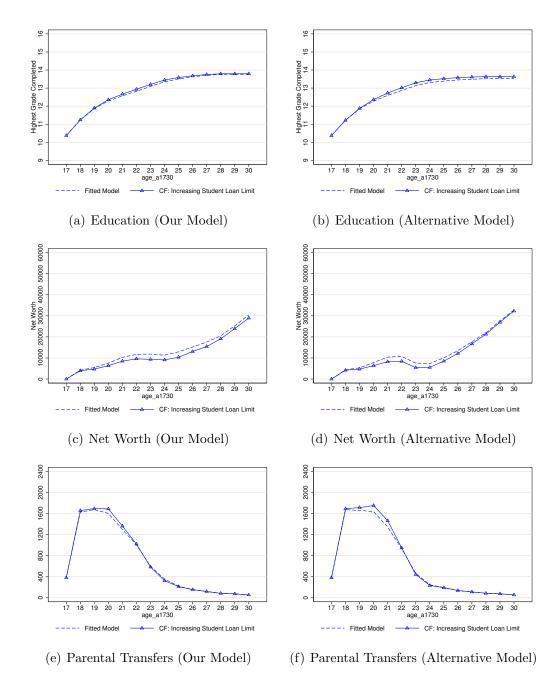


Figure A18: Counterfactual Simulation of Increasing Student Loan Limits on Education, Net Worth, and Transfers

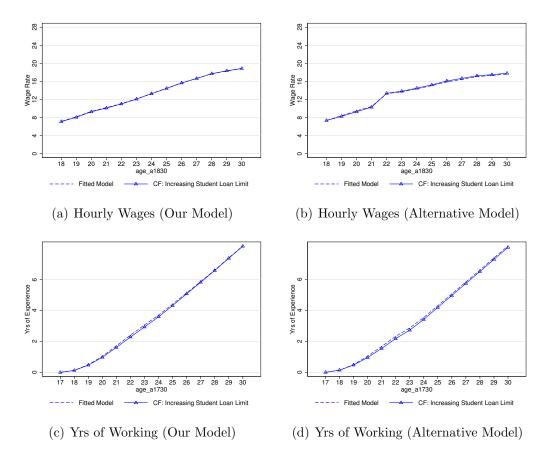


Figure A19: Counterfactual Simulation of Increasing Student Loan Limits on Wage and Years of Working

## References

- French, Eric, and John Bailey Jones, 2011, The Effects of Health Insurance and Self-Insurance on Retirement Behavior, *Econometrica* 79, 693–732.
- Hubbard, R. Glenn, Jonathan Skinner, and Stephen P. Zeldes, 1995, Precautionary Saving and Social Insurance, *Journal of Political Economy* 103, 360–399.
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