

Economics 350:

Two Interpretations of the Mincer Equation

Learning-by-doing vs. On-the-job Training

Based in part on James Heckman, Lance Lochner, and Ricardo Cossa's

"Learning-by-doing vs. on-the-job training: Using variation induced by the EITC to distinguish between models of skill formation," in Phelps, Edmund S. *Designing inclusion: tools to raise low-end pay and employment in private enterprise*. Cambridge Univ Press, 2003, pp. 74–130.

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- 1 Is learning rivalrous with or complementary with working?
Rivalrous with or complementary with earning?
- 2 Do people pay for their learning? What is the form of the payment? Foregone earnings? Foregone leisure? Both?
- 3 What is the correct price of time to include in a labor supply equation? Is the measured average wage the correct price of time?
- 4 What is the correct interpretation of empirical Mincer earnings equations? What do we learn from cross-section estimates?

Point of Departure:

- Two observationally equivalent interpretations of

$$\ln W = \alpha_0 + \alpha_1 S + \alpha_2 x + \alpha_3 x^2$$

- S = schooling
- x = work experience
- α_1 = “average rate of return” to schooling
- α_2, α_3 = “returns to experience”

Mincer's Justification

- OJT model appeals to Becker-Ben Porath model of experience x .
- Learning comes at the expense of earning.
- $k(x)$ earnings forgone as % of potential earnings.
- Assume:
 - ① Constant rates of return (or if heterogeneous assume independent of level of investment: r_p).
 - ② $k(x) = 1 - \frac{x}{T}$ where T is the maximum possible amount of experience.
 - ③ Effect of OJT (in logs) additively separable from schooling.
 - ④ T functionally independent of S . (Each year of schooling adds one year to effective working life.)
 - ⑤ $r(x)$ same for all x .
- Then (1), (2), (3), (4) and (5) \Rightarrow Mincer model. (See Mincer handout.)

- $\alpha_1 = r_s$; average “rate of return to schooling.”
- $\alpha_2, \alpha_3 \Rightarrow r_p$; average rate of return to post school investment.
- Can show:

$$\left(\alpha_2 = \left(r_p + \frac{r_p}{2T} \right); \alpha_3 = -\frac{r_p}{2T} \right)$$

(see “Mincer” notes).

Second Model

- Empirically indistinguishable from first model.
- x = cumulated work experience.
- The only cost of x is forgone leisure.
- Work produces current and future wage growth.
- $\ln W = \alpha_1 + \alpha_2 S + \alpha_3 x + \alpha_4 x^2$.
- Keane and Wolpin (1997, 2001) and many successor models.
- Keane, 2016, *EJ*, on reading list.
- Question: can we distinguish the two models?

General model and special cases: 2 period analysis: Worker Problem

- (C_0, L_0) : Consumption and leisure in “0”
- (C_1, L_1) : Consumption and leisure in “1”

$$\text{Preferences: } U(C_0, L_0) + \frac{1}{1 + \rho} U(C_1, L_1) \quad (1)$$

- r is the borrowing rate – perfect certainty.

- H_0 = initial human capital; H_1 = final human capital
- Production function of human capital (“technology of skill formation”):

$$H_1 = H_0 + F(\theta_0, H_0, 1 - L_0)$$

$$F_{\theta_0} \geq 0, F_{H_0} \geq 0, F_{1-L_0} \geq 0.$$
- Can add depreciation (assume no depreciation for simplicity).
- θ_0 = “quality” (investment content) of job in period 0.
- As $\theta_0 \uparrow$ $H_1 \uparrow$ ($F_{\theta_0} > 0$)
- $\theta_1 \equiv 0$; no investment in second period because no tomorrow.
- Assume $\rho = r = 0$.
- θ_0 is valuable.
- It helps produce human capital.
- However, you have to be at a firm to realize the investment opportunity.
- Does it have a price?

- Earnings in “0”: $W(H_0, 1 - L_0, \theta_0)$
- Earnings in “1”: $W(H_1, 1 - L_1, \theta_1)$
- Budget Constraint:

$$C_0 + C_1 = \underbrace{W(H_0, 1 - L_0, \theta_0)}_{\text{Earnings in period 0}} + \underbrace{W(H_1, 1 - L_1)}_{\text{Earnings in period 1}} \quad (2)$$

Pricing of human capital services in final output:

- R : rental rate on units of human capital (efficiency units model).
- $W(H_0, 1 - L_0, \theta_0) = \underbrace{RH_0(1 - L_0)}_{\text{potential earnings}} - \underbrace{P(\theta_0, 1 - L_0, H_0)}_{\substack{\text{amount paid by agent to} \\ \text{acquire human capital} \\ \text{i.e., to access } \theta_0}}$
- $W(H_1, 1 - L_1) = RH_1(1 - L_1)$
- $P(\theta_0, 1 - L_0, H_0)$ is *the cost of quality* θ_0 with $1 - L_0$ hours of work and with the agent having H_0 amount of human capital with training content θ_0 .

Becker-Ben Porath Model

- Leisure fixed: $L_0 = L_1 = \bar{L}$
- Jobs priced out in a special way
- Price of learning content θ in a job: $P(\theta_0, 1 - L_0, H_0) = P(\theta_0)$
- Production function: $H_1 = F(\theta_0, H_0) + H_0$
- $\theta_0 = I$ (time spent investing)
- $P(\theta_0) = RH_0I$ (cost of investment)
- $W(H_0, 1 - L_0, \theta_0) = RH_0(1 - \bar{L}) - RH_0I$
- Can add leisure (Blinder and Weiss, 1976; Heckman, 1976)
- The Ben-Porath (1967) model has a special functional form

$$H_1 = G(H_0\theta_0) + H_0 \quad (3)$$

- “Neutrality” (MC of investment = MR of investment)
- **Question: What are the first order conditions for the model (1), (2), and (3) with leisure fixed $L_0 = L_1 = \bar{L}$?**
- **How does investment depend on H_0 and R ?**



Learning by Doing (LBD) Model in the Literature

- Cost of learning is foregone leisure.
- Ignored in Becker-Ben Porath models.
- Investment is a “free good.”

$$\frac{\partial P}{\partial(1 - L_0)} = \frac{\partial P}{\partial\theta_0} = 0$$

$$\frac{\partial F}{\partial(1 - L_0)} > 0 \quad ; \quad \frac{\partial F}{\partial\theta_0} = 0$$

(Imai and Keane, 2004; Keane, 2016)

- Implicitly θ_0 : the same at all jobs.
- Usually kept implicit.
- *Free lunch. (No direct cost of learning.)*
- The only cost of learning is *foregone leisure*.
- Many intermediate cases are possible.

Firm Side of the Problem

- Firm has a valuable good: training possibilities.
- Firms heterogeneous in training opportunities.
- Two sector model of the firm.
- Firms: can produce skills and use skills for producing final output, offer training opportunities, or both.
- Profits for a one-worker firm offering opportunity θ_0 :

$$\underbrace{\Pi}_{\text{Profits}} = \underbrace{J((1 - L_0), H_0, \theta_0)}_{\text{Output}} + \underbrace{P(\theta_0, (1 - L_0), H_0)}_{\substack{\text{Revenue from selling} \\ \text{training opportunities} \\ \text{to workers}}} - \underbrace{WRH_0(1 - L_0)}_{\text{Labor Costs}}$$

- $J_{\theta_0} \leq 0$.

- *Hedonic equilibrium* for firms and workers in skill production sector:

$P(\theta_0, (1 - L_0), H_0, R)$ is market clearing pricing function.

- (Will establish properties later.)
- Equates demand and supply across jobs, indexed by θ, L_0 .
- **Question: What is the life cycle mobility of workers across firms?**

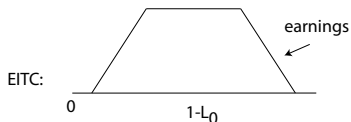
Can One Distinguish Between the Two Models?

- See Cossa, Heckman et al. (2003).

Consider taxes and subsidies in periods “0” and “1”.

Model 1: OJT (Becker-Ben Porath with Leisure)

- Motivated by analysis of EITC (Earned Income Tax Credit) program (Cossa et al., 2003).



- Assume learning takes place on the job.
- τ_0, τ_1 are proportional subsidies: $\tau_0 > 0, \tau_1 > 0$.
- $R = 1$
- Individuals maximize (1): $U(C_0, L_0) + U(C_1, L_1)$ subject to

$$C_0 + C_1 = \underbrace{(1 + \tau_0)H_0(1 - l_0 - L_0)}_{\text{Measured after tax/subsidy earnings in period 0}} + \underbrace{(1 + \tau_1)H_1(1 - L_1)}_{\text{Measured after tax/subsidy earnings in period 1}}$$

- Assume $H_1 = F(l_0) + H_0$ (abstract from self productivity).
- FOC for l_0 : $(1 + \tau_0)H_0 \leq (1 + \tau_1)(1 - L_1)F'(l_0)$
- **Question: What is the FOC for the Ben Porath version of the model with labor supply?**
- $H_1 = F(l_0 H_0) + H_0$
- $(1 + \tau_0)H_0 \leq (1 + \tau_1)(1 - L_1)G'(lH_0)H_0$
- Neutrality: H_0 raises productivity proportional to opportunity cost.

Consider the General Model

Compensate for income effects (λ constant or Frisch demands),

- $\tau_0 > \tau_1 = 0$: Period 0 subsidy raises MC of l_0 : $H_1 \downarrow$
- $\tau_1 > \tau_0 = 0$: Period 1 subsidy raises MR of l_0 : $H_1 \uparrow$
- $\tau_0 = \tau_1 > 0$: Flat subsidy increases $h_1 = 1 - L_1$ (time spent in market working) and raises MR of l_0 : $(l_0, H_1) \uparrow$ (remember that wealth effects are neutralized).

Digression:

- Why? Consider the following Lagrangian:

$$\mathcal{L} = U(C_0, L_0) + U(C_1, L_1) \\ - \lambda [C_0 + C_1 - (1 + \tau_0)H_0(1 - I_0 - L_0) - (1 + \tau_1)H_1(1 - L_1)]$$

- FOC: C_0, C_1

$$U_1(C_0, L_0) = \lambda$$

$$U_1(C_1, L_1) = \lambda$$

- FOC: L_0, L_1

$$U_2(C_0, L_0) = \lambda(1 + \tau_0)H_0$$

$$U_2(C_1, L_1) = \lambda(1 + \tau_1)H_1$$

- FOC: l_0
- Assume $H_1 = F(l_0) + H_0$

$$(1 + \tau_0)H_0 = (1 + \tau_1)F'(l_0)(1 - L_1)$$

λ is Held Constant

- Suppose initially that we have separability

$$U(C_0, L_0) = \phi(C_0) + \eta(L_0)$$

$$U(C_1, L_1) = \phi(C_1) + \eta(L_1)$$

- Then if $\tau_0 = \tau_1 \uparrow$, $L_0, L_1 \downarrow \therefore I_0 \uparrow, H_1 \uparrow$
- In the general case where $\tau_0 = \tau_1 = \tau$, as $\tau \uparrow$, price of leisure increases and agents substitute toward consumption
- $(1 - L_1) \uparrow \Rightarrow I_0 \uparrow \Rightarrow H_1 \uparrow$

- If we add back wealth and income effects discourage work and reduce investment in all cases.
- **Question: For a Ben Porath Technology with labor supply, what is the answer to these questions for these subsidy changes?**

Model 2: Learning By Doing (LBD): Cost of Learning is Same as Cost of Work–Foregone Leisure

- $R = 1$
- Individuals maximize $U(C_0, L_0) + U(C_1, L_1)$ subject to

$$C_0 + C_1 = (1 + \tau_0)H_0(1 - L_0) + (1 + \tau_1)H_1(1 - L_1).$$

and

$$H_1 = H_0 + \phi(1 - L_0) \quad (\text{Period "1" earnings})$$

FOC:

$$\begin{aligned}
 U_2(C_0, L_0) &= \lambda \left[\underbrace{H_0(1 + \tau_0)}_{\substack{\text{Marginal after subsidy} \\ \text{measured effect} \\ \text{of an hour of work} \\ \text{on after-tax earnings}}} + \overbrace{\phi'(1 - L_0)(1 - L_1)(1 + \tau_1)}^{\substack{\text{Effect of} \\ \text{current hour of work} \\ \text{on future earnings}}} \right] \\
 U_2(C_1, L_1) &= \lambda \left[\underbrace{H_0 + \phi(1 - L_0)}_{\substack{\text{Measured effect of an extra} \\ \text{hour of work on after subsidy} \\ \text{on earnings}}} \right] (1 + \tau_1)
 \end{aligned}$$

Compensate for income effects (λ constant)

- $\tau_0 = \tau_1 > 0$: Flat subsidy increases the current and future return to work $h_0 = 1 - L_0$ and $h_1 = 1 - L_1$.
- $\therefore H_1 \uparrow$.
- $\tau_0 > \tau_1 = 0$: Period 0 subsidy raises current return to h_0 , $(H_1) \uparrow$
- $\tau_1 > \tau_0 = 0$: Period 1 subsidy raises future return to h_1 , $(H_1) \uparrow$
- Wealth and income effects discourage work and reduce learning and investment in all cases.

Model 2': LBD with a Market for Learning Opportunities (No Free Lunch and Heterogeneous Firms)

- Suppose firms may offer different learning opportunities indexed by $\theta \in (\underline{\theta}_0, \bar{\theta}_0)$.
- So $H_1 = H_0 + \phi(1 - L_0, \theta_0)$ where $\frac{\partial^2 \phi}{\partial(1-L_0)\partial\theta_0} > 0$.
- With a distribution of firm types, a market for learning will emerge.
- All old workers and young workers who expect high L_1 (low h_1) place little value on learning, θ_0 .
- Pricing function $P(\theta_0)$ may arise with $P'(\theta_0) > 0$. (Worker pays for learning opportunities)
- This adds a new wrinkle to the LBD model.
- Wage earnings:
 - In the first period: $W(H_0, \theta_0) = H_0(1 - L_0) - P(\theta_0)$.
 - In the second period, it is $H_1(1 - L_1)$

- We acquire a new first order condition in the LBD model.
- Individuals choose firm type or learning opportunity (θ) according to:

$$(1 + \tau_0)P'(\theta) = (1 + \tau_1)(1 - L_1)\frac{\partial\phi(1 - L_0, \theta_0)}{\partial\theta_0} \quad (*)$$

- Consider taxes and subsidies in this model.
- As before, consider an income-compensated change from an initial position: $\tau_0 = \tau_1 = 0$.
- $\tau_0 = \tau_1 > 0$: Flat subsidy increases current and future return to h_0 (= period zero hours of work) and raises return to θ_0 by increasing h_0 and h_1 (period 1 hours of work).
- \therefore This is a force for $H_1 \uparrow$.
- But it raises the cost of buying θ_0 , a force for $H_1 \downarrow$ (see *).

- $\tau_0 > \tau_1 = 0$: Period 0 subsidy raises current return to h_0 and the MC of θ_0 .
- **Ambiguous on H_1** (everything else constant).
- $\tau_1 > \tau_0 = 0$: Period 1 subsidy raises future return to h_0 and return to θ_0 .
- $\therefore H_1 \uparrow$.
- Test of model not clear anymore.
- **Note:** Can equate this model with OJT model if θ_0 equated to l_0 in Ben Porath. Then the two models are indistinguishable.
- Implicit is a theory of life cycle mobility (stepping stone mobility).

Implications for Measured Wages

OJT:

- a First period earnings $<$ potential earnings if investment is paid by foregone earnings (wage rates understated).
- b First period earnings $=$ potential earnings if investment off the job or not paid via earnings.

LBD (free lunch):

- First period earnings $<$ potential earnings. Wage rates understated (price of time is greater).