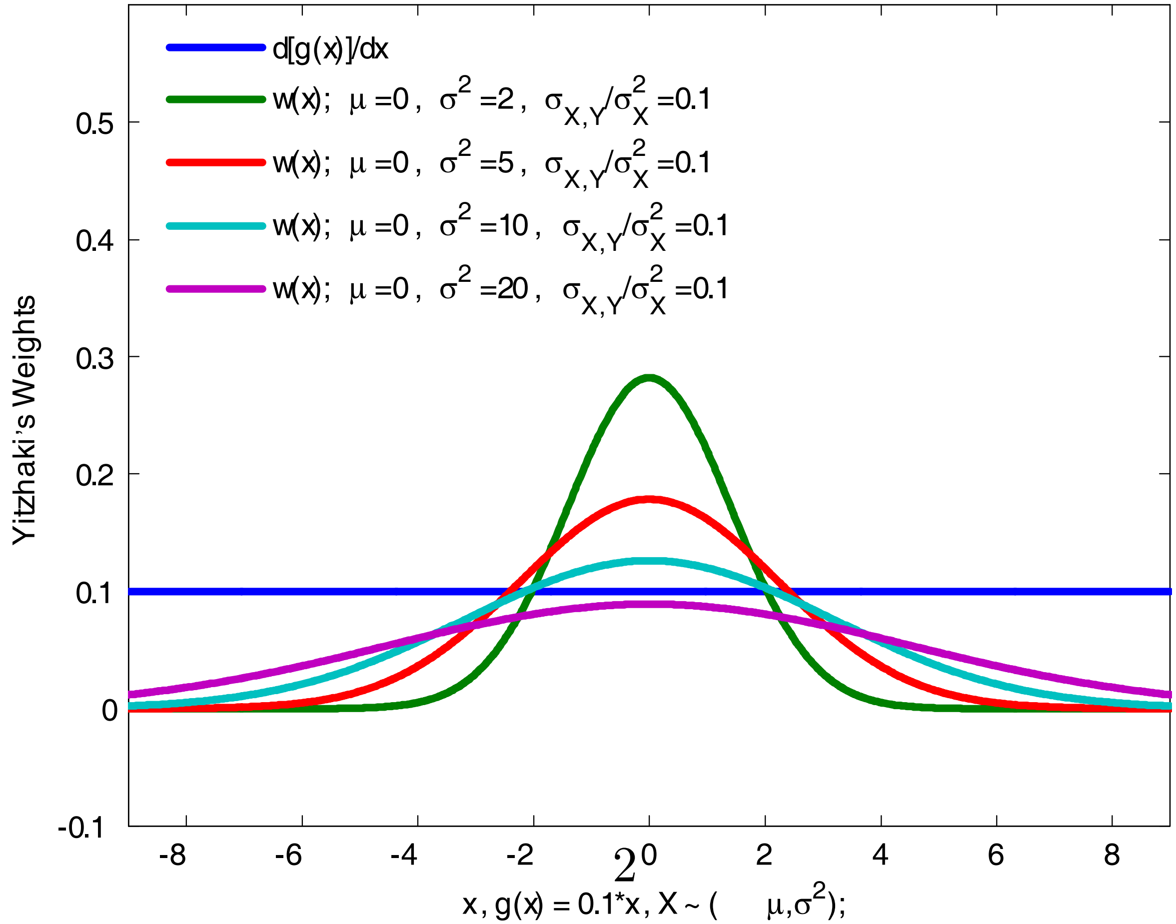
Yitzhaki Weights Examples

James J. Heckman

Econ 312, Spring 2022

Yitzhaki's Weights for X Normal



$$E\left(Y|X=x\right)=g(x)\Rightarrow\frac{Cov(X,Y)}{Var(X)}=\int_{-\infty}^{\infty}g'(t)w(t)dx$$

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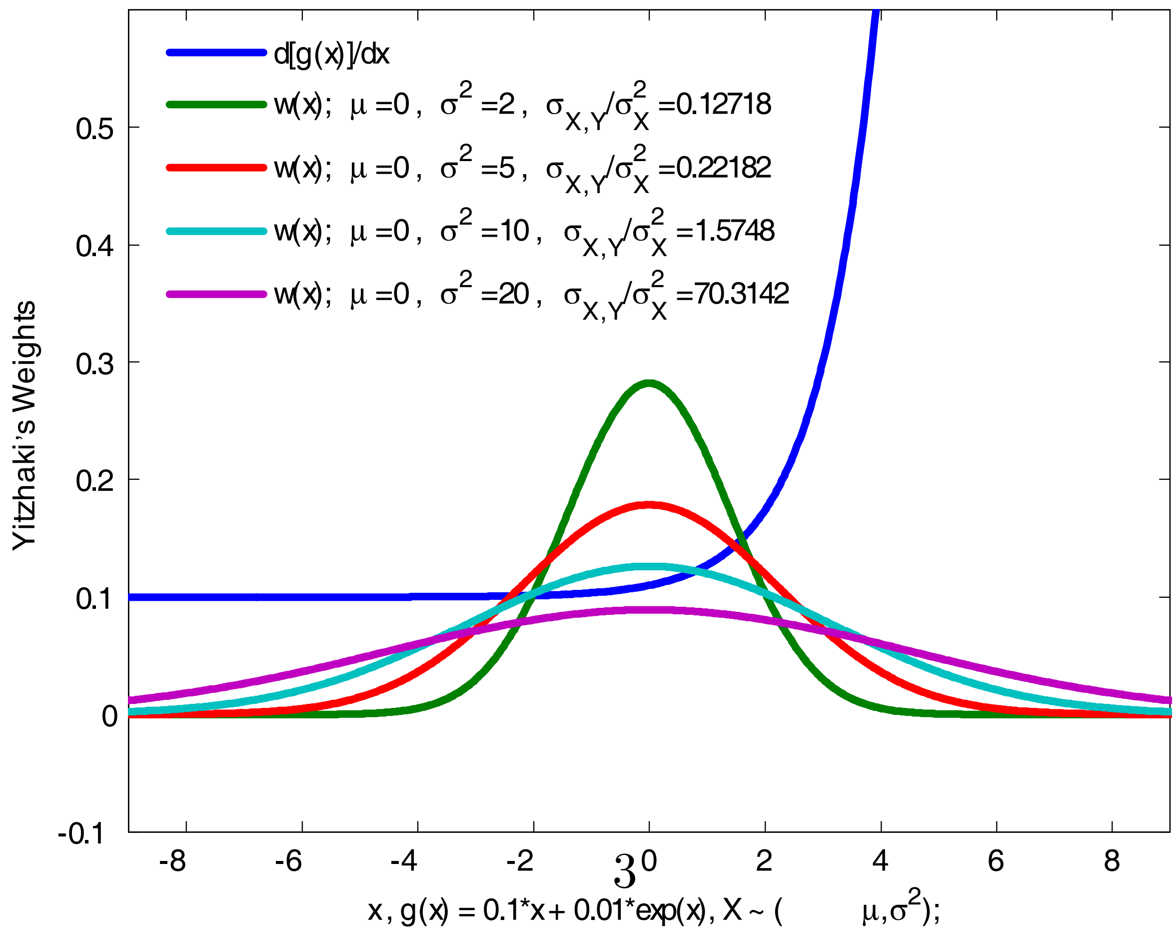

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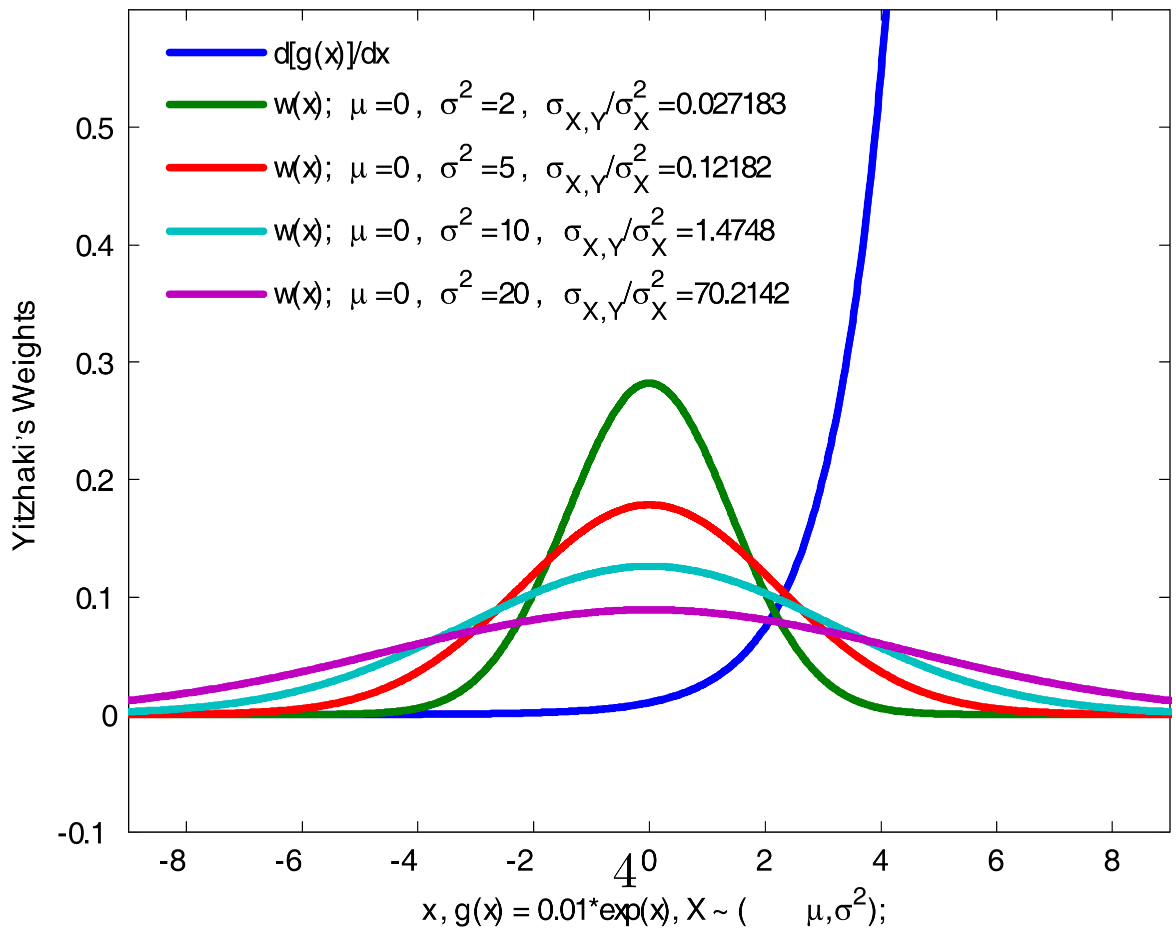

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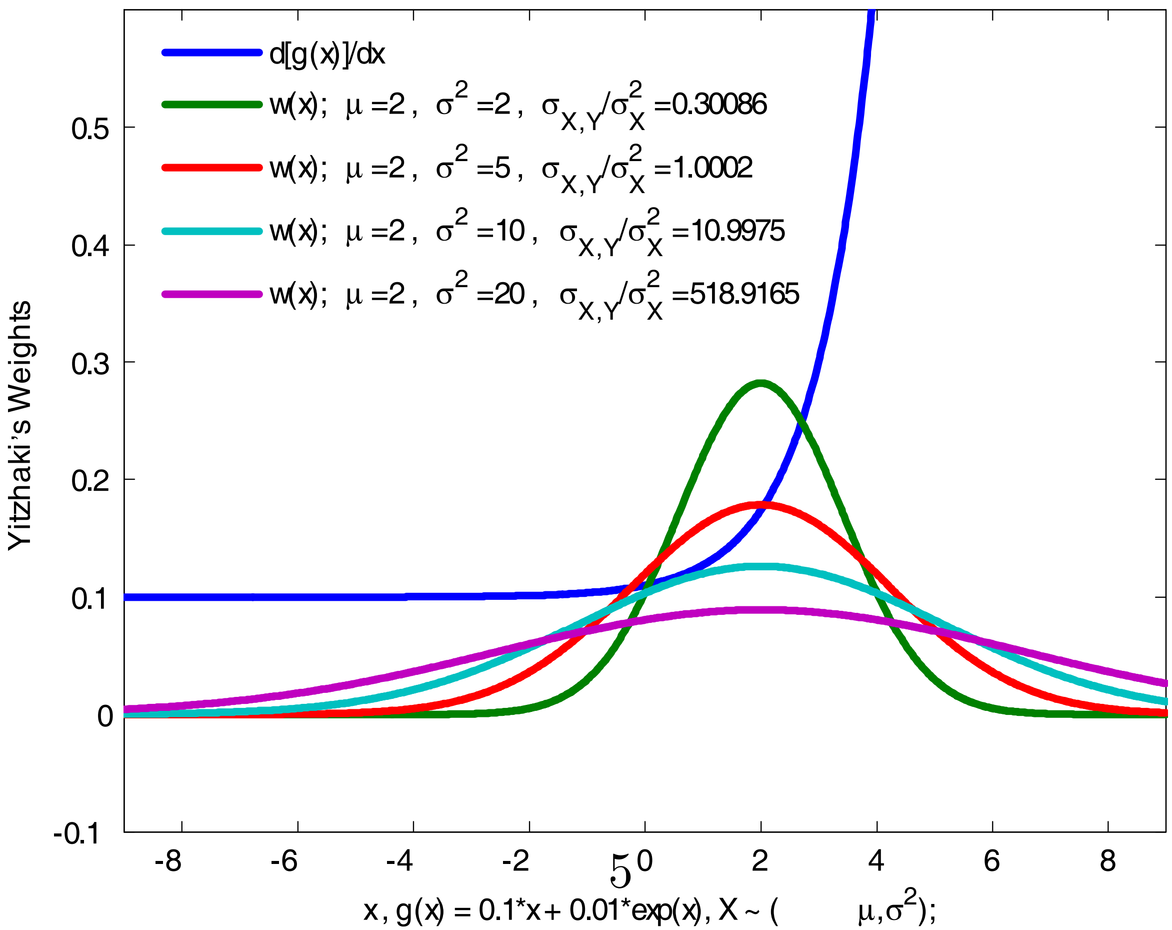

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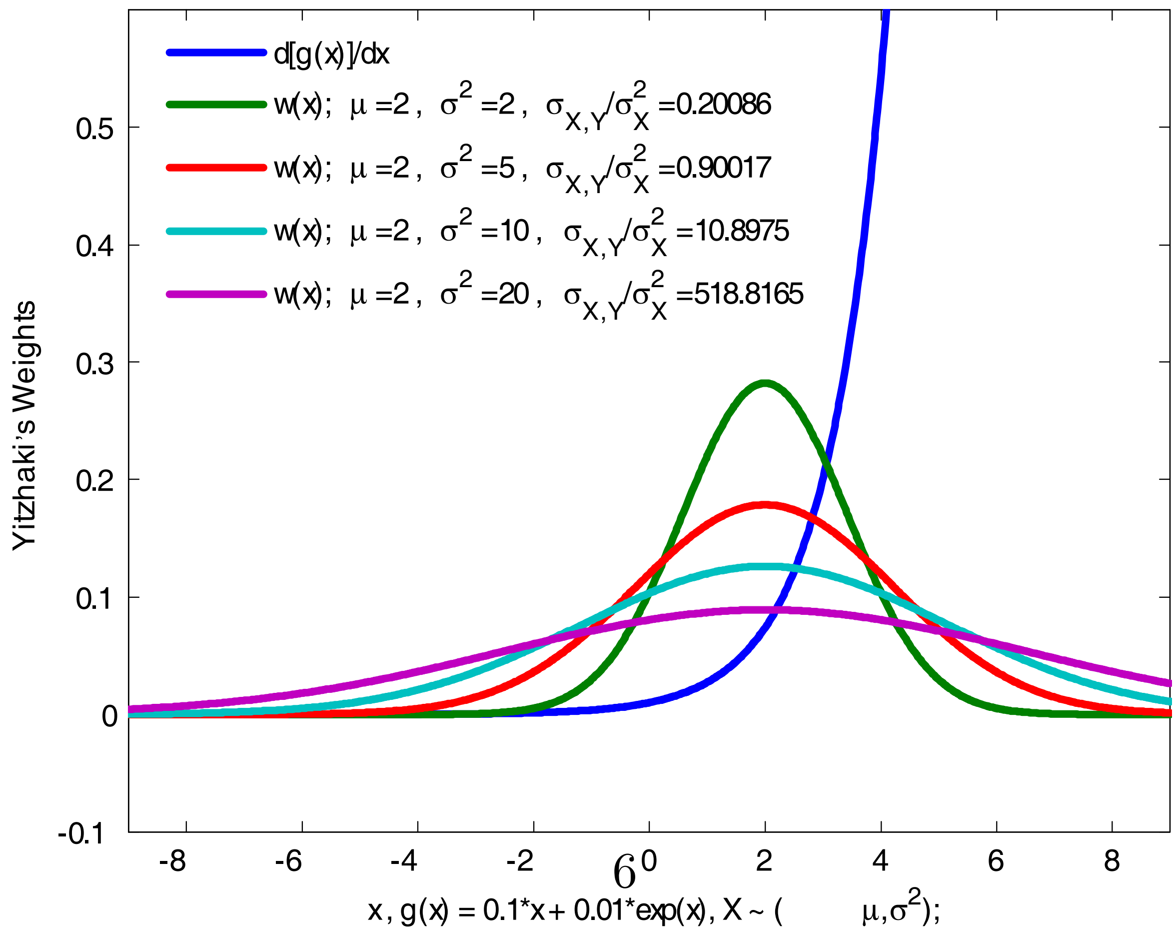

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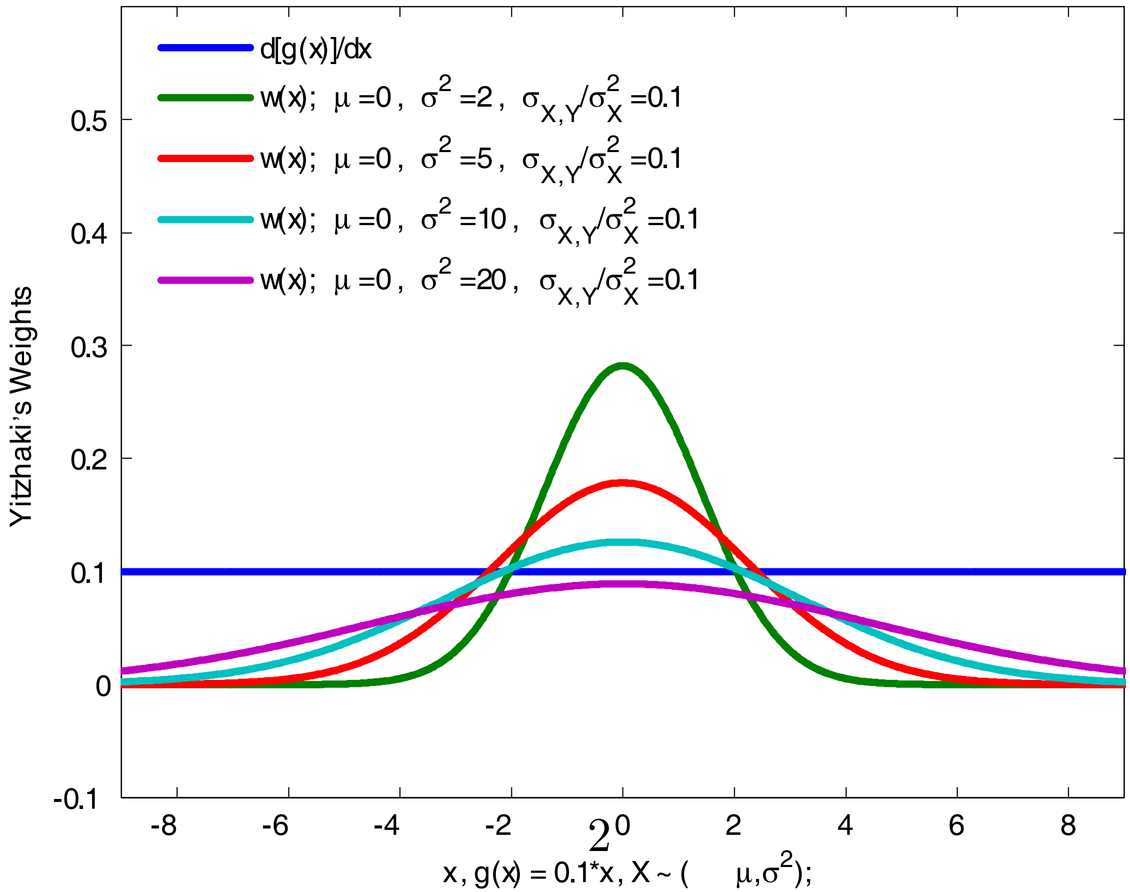

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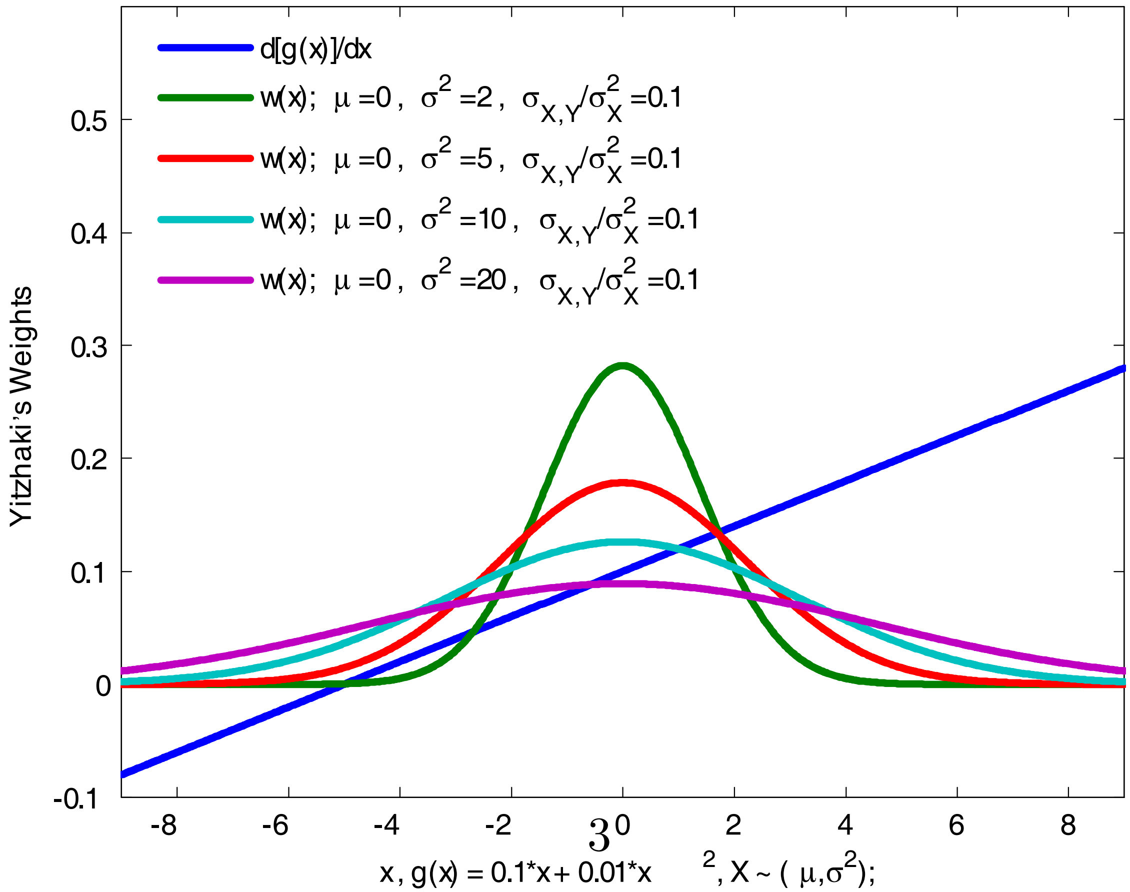

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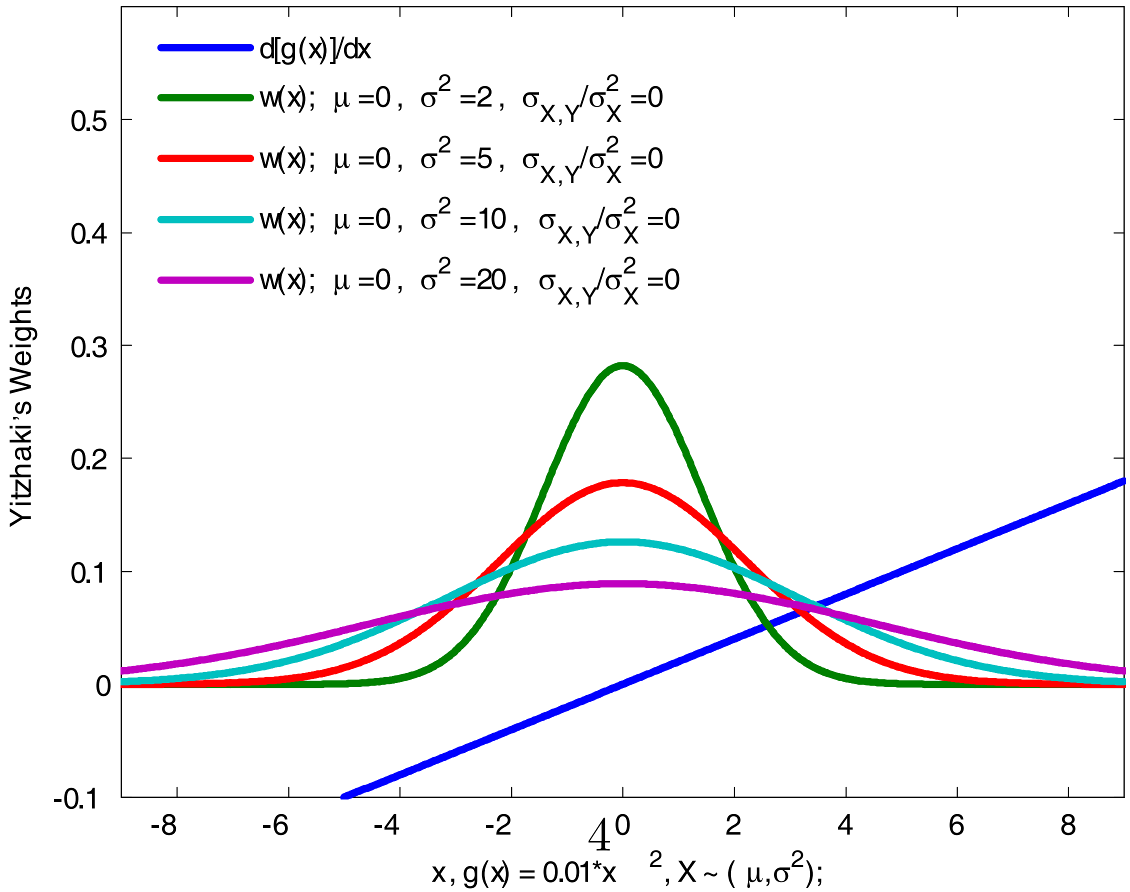

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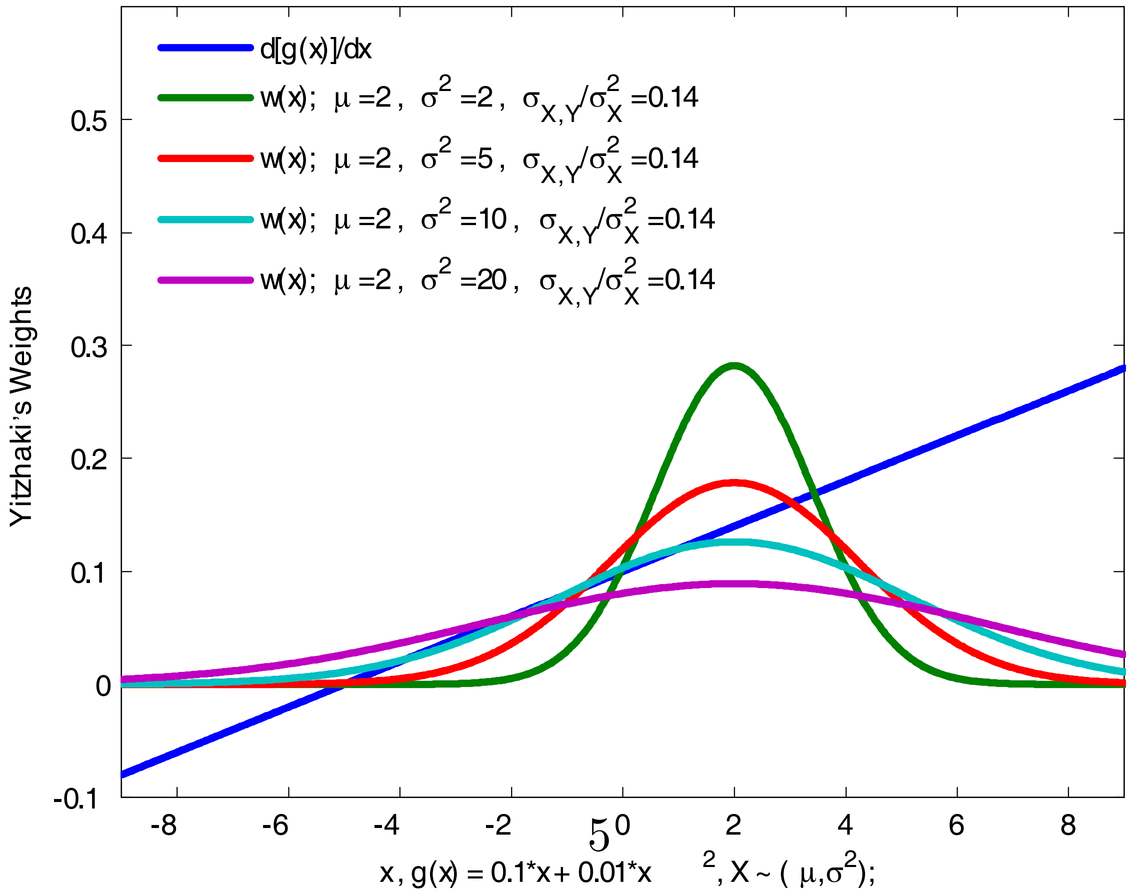

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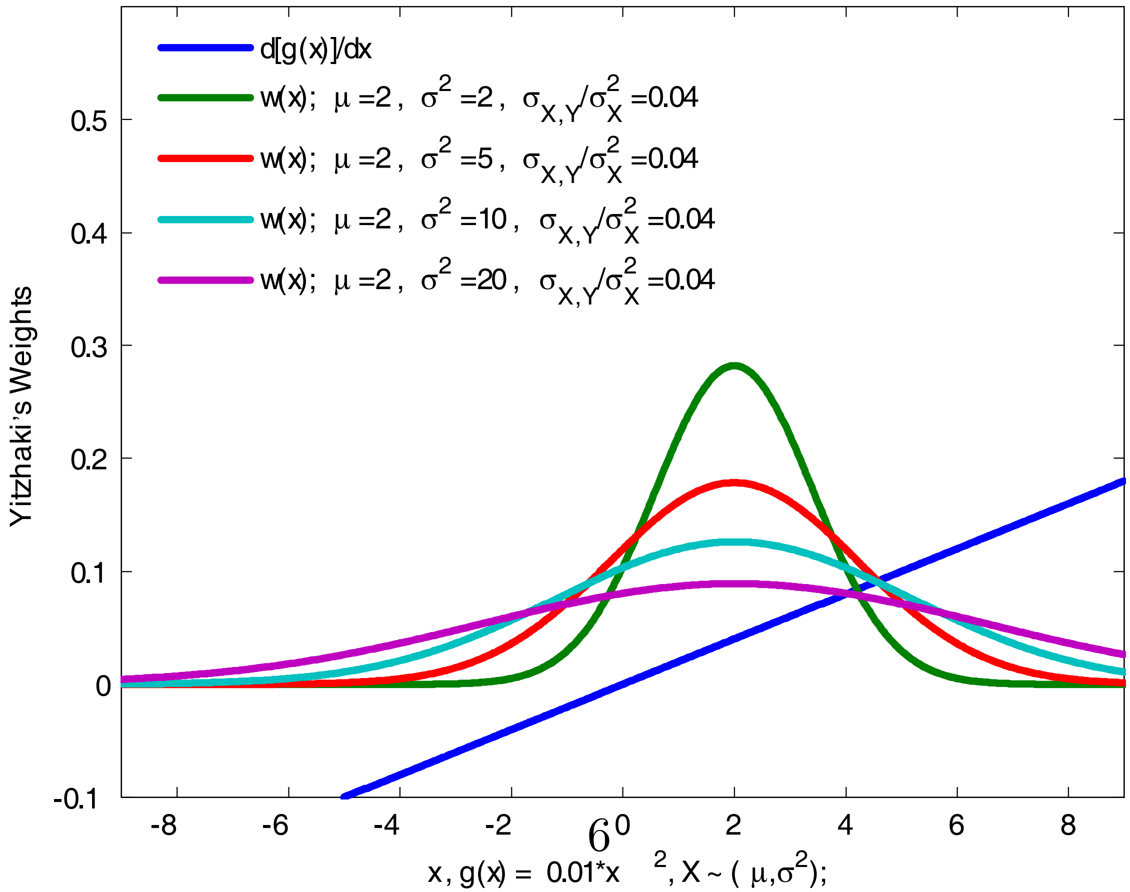

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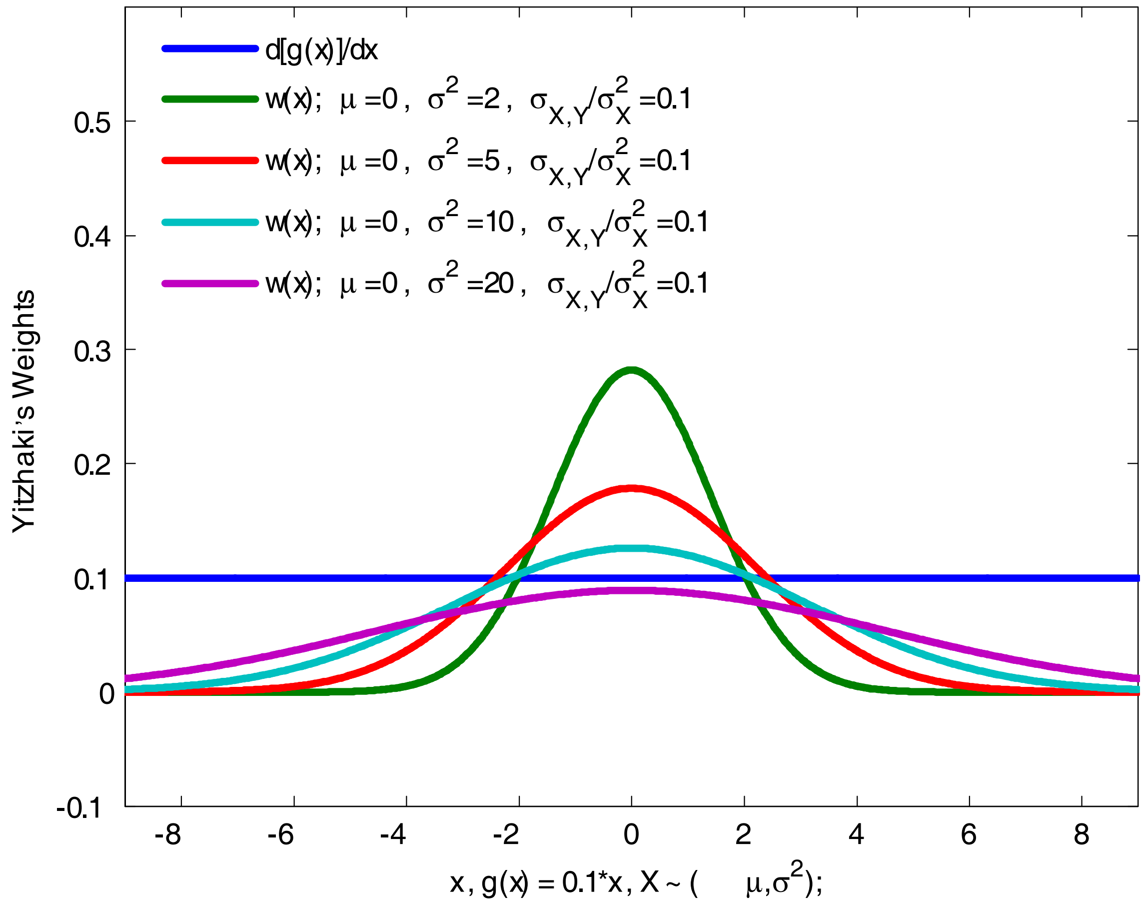

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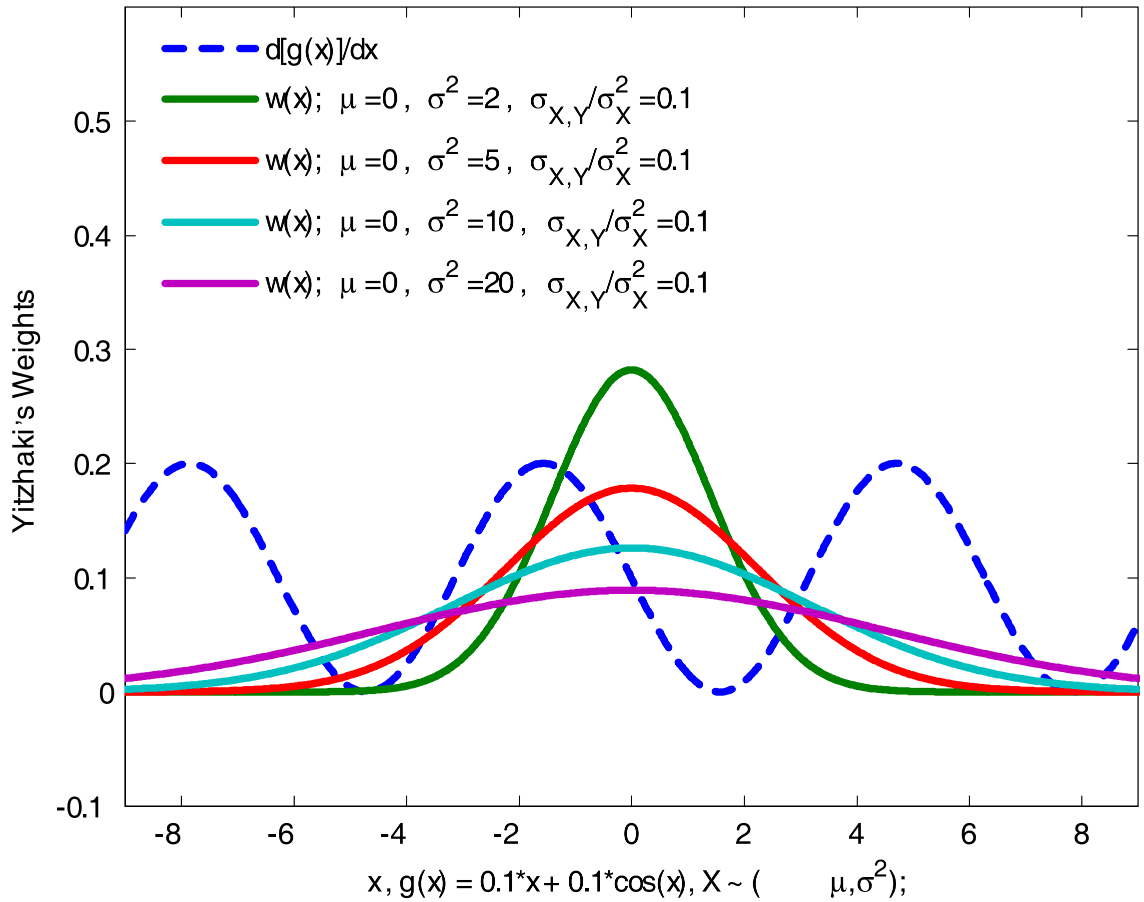

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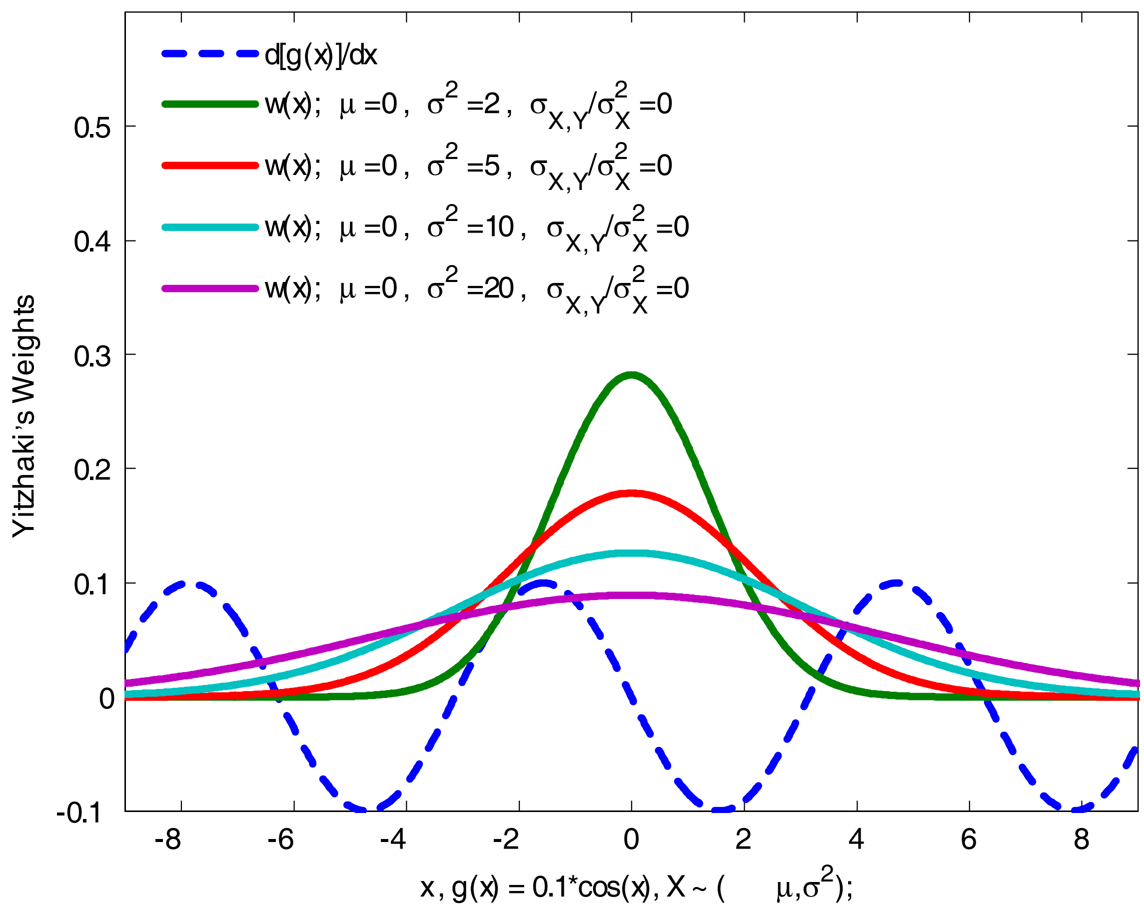

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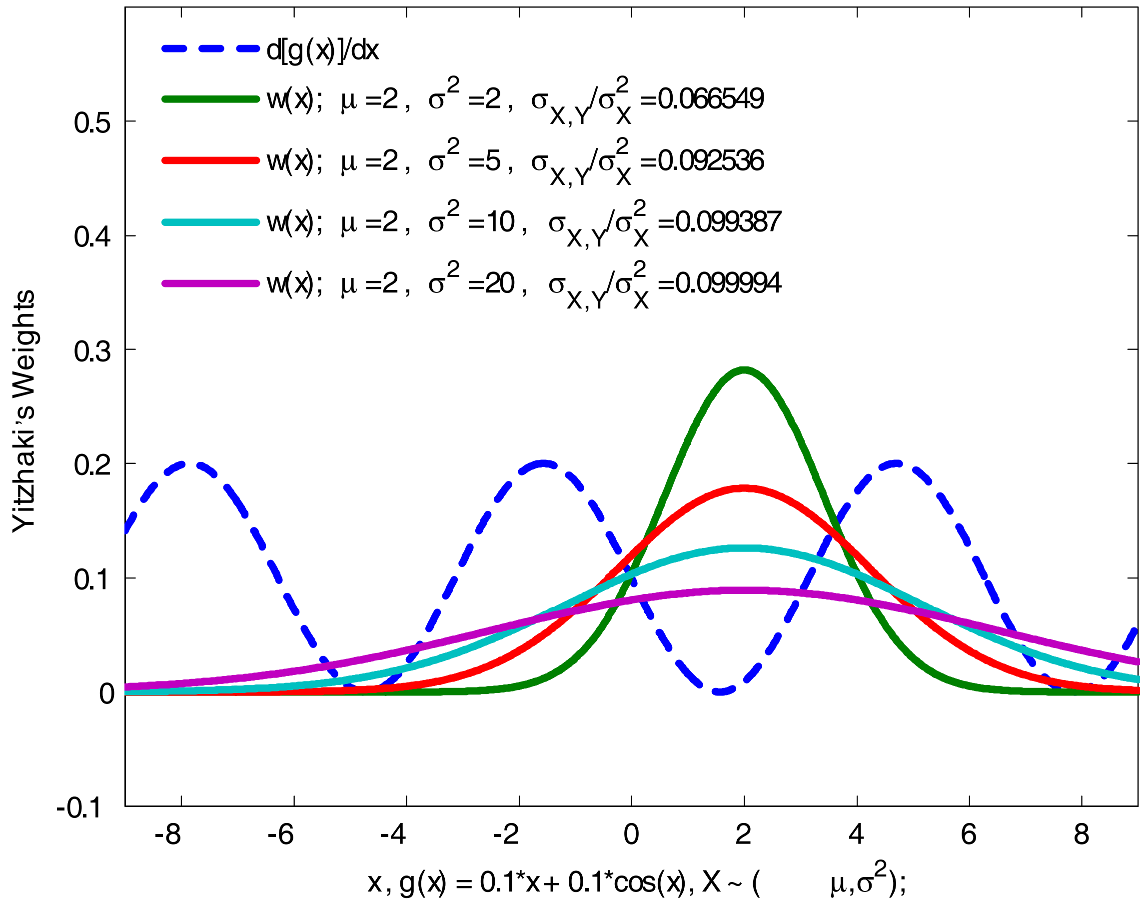

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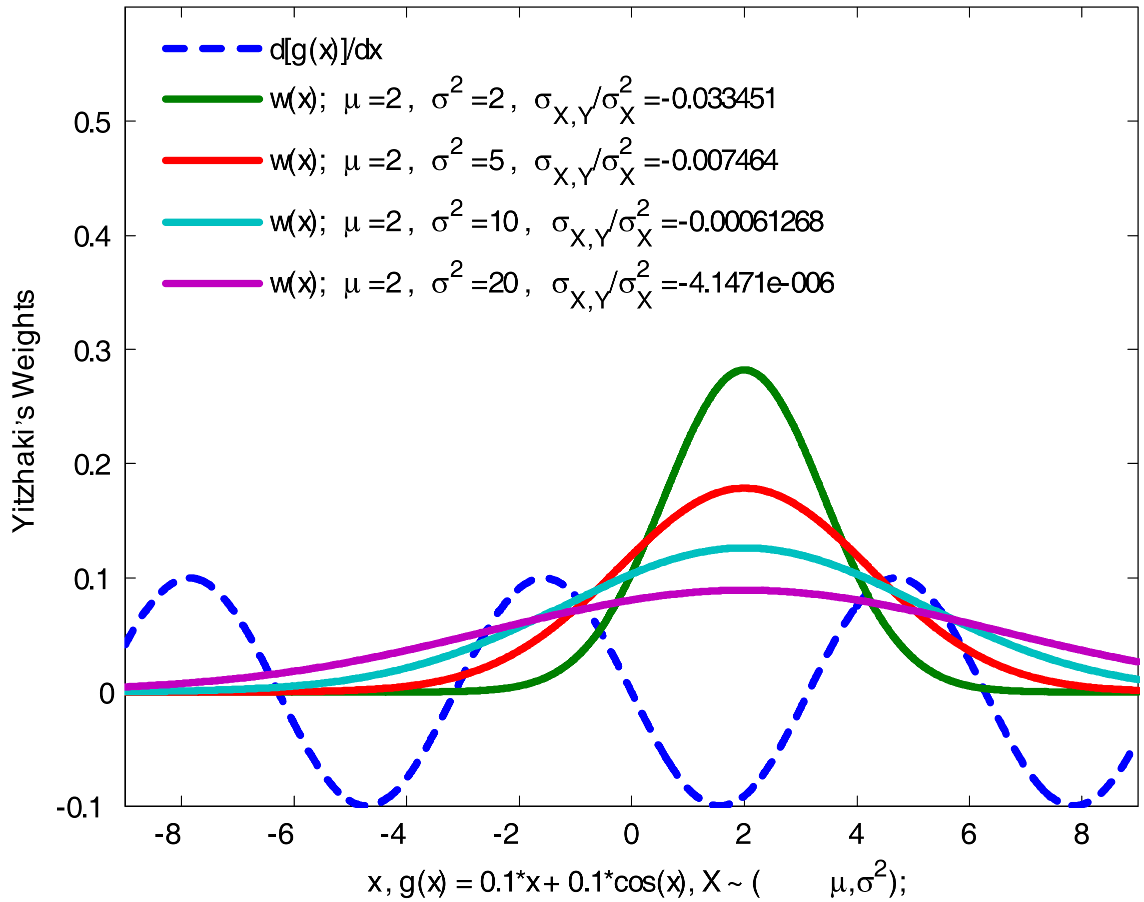

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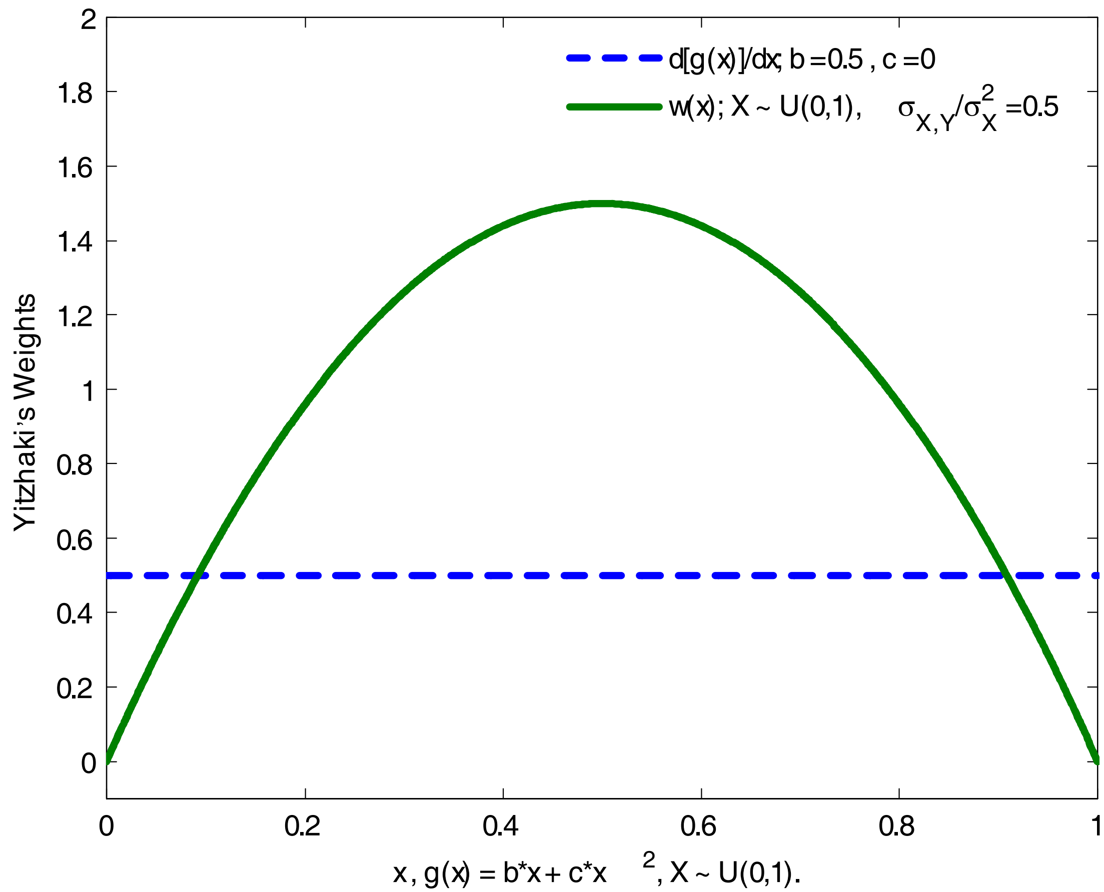

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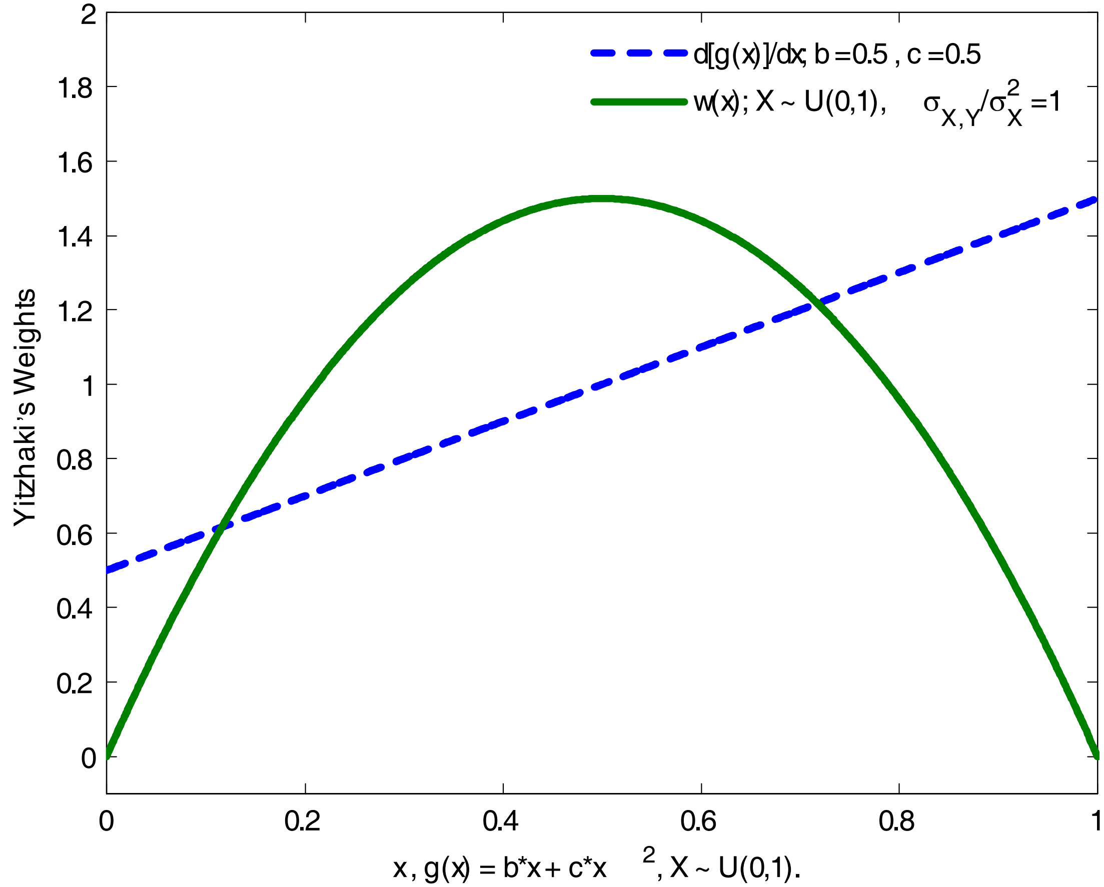

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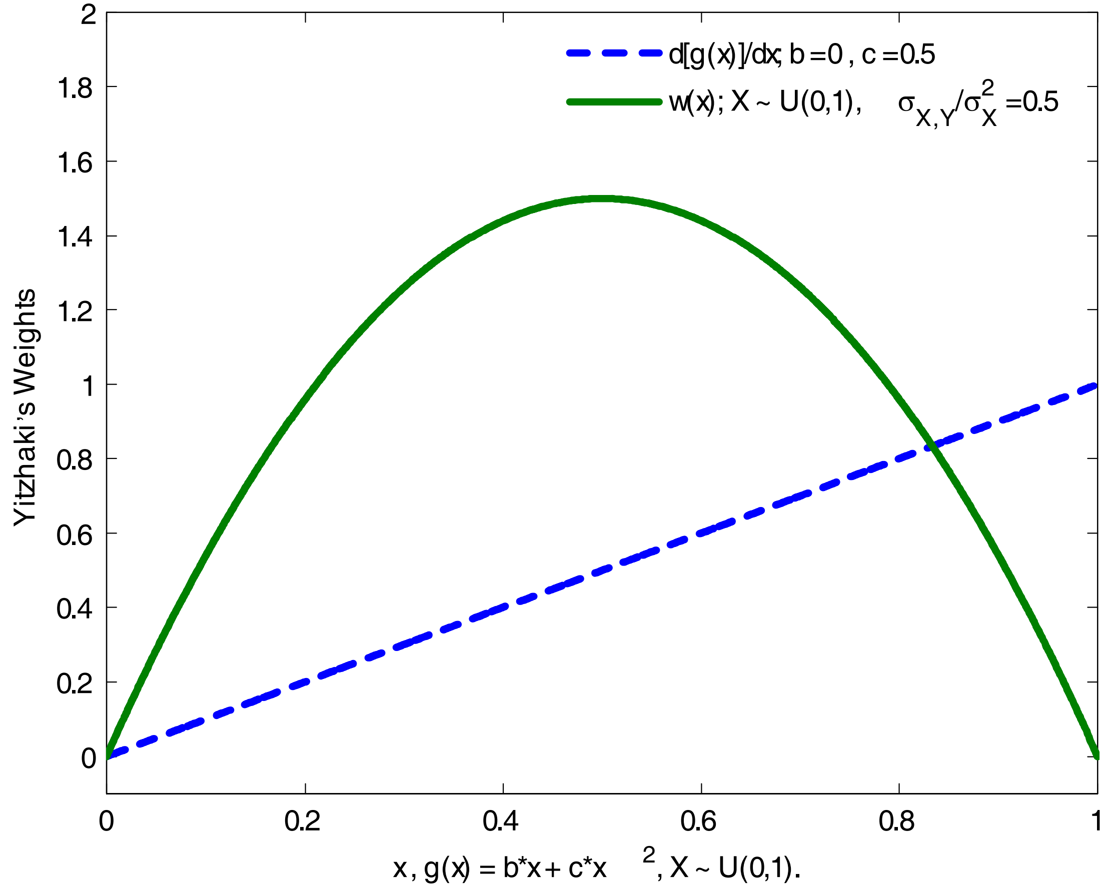

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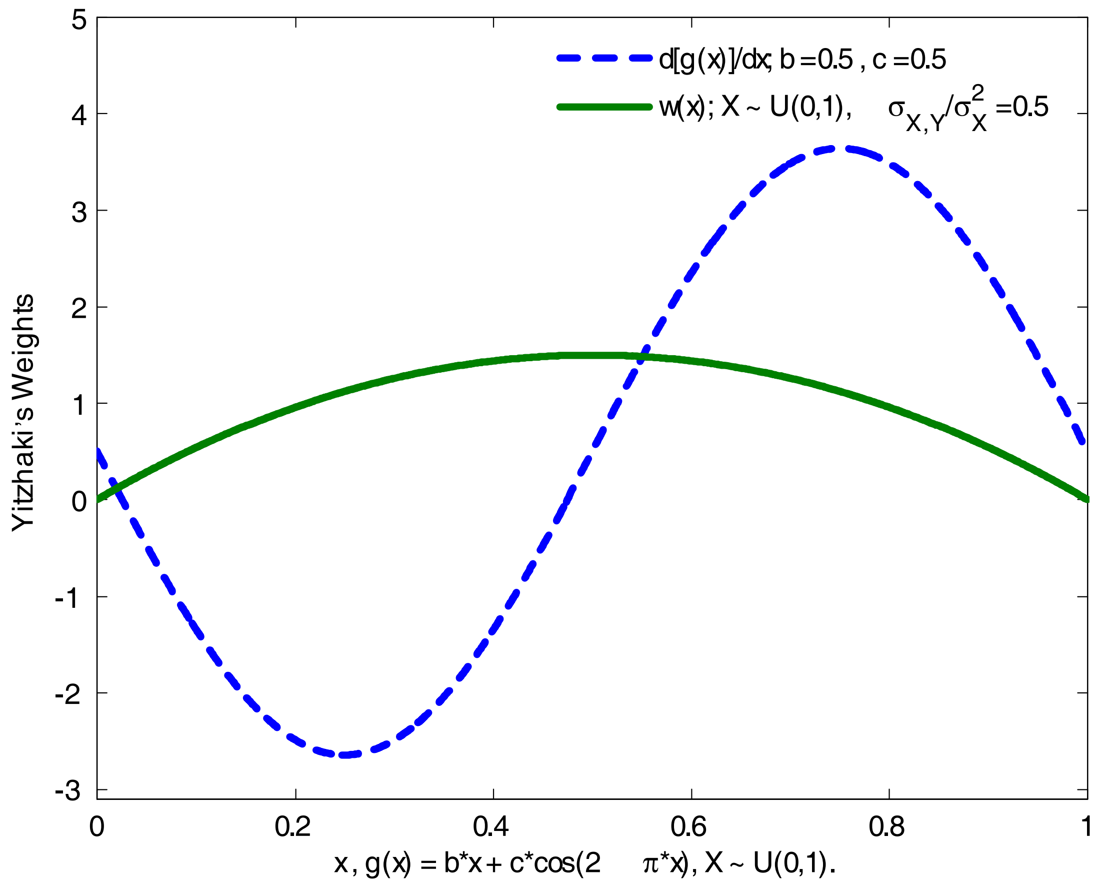

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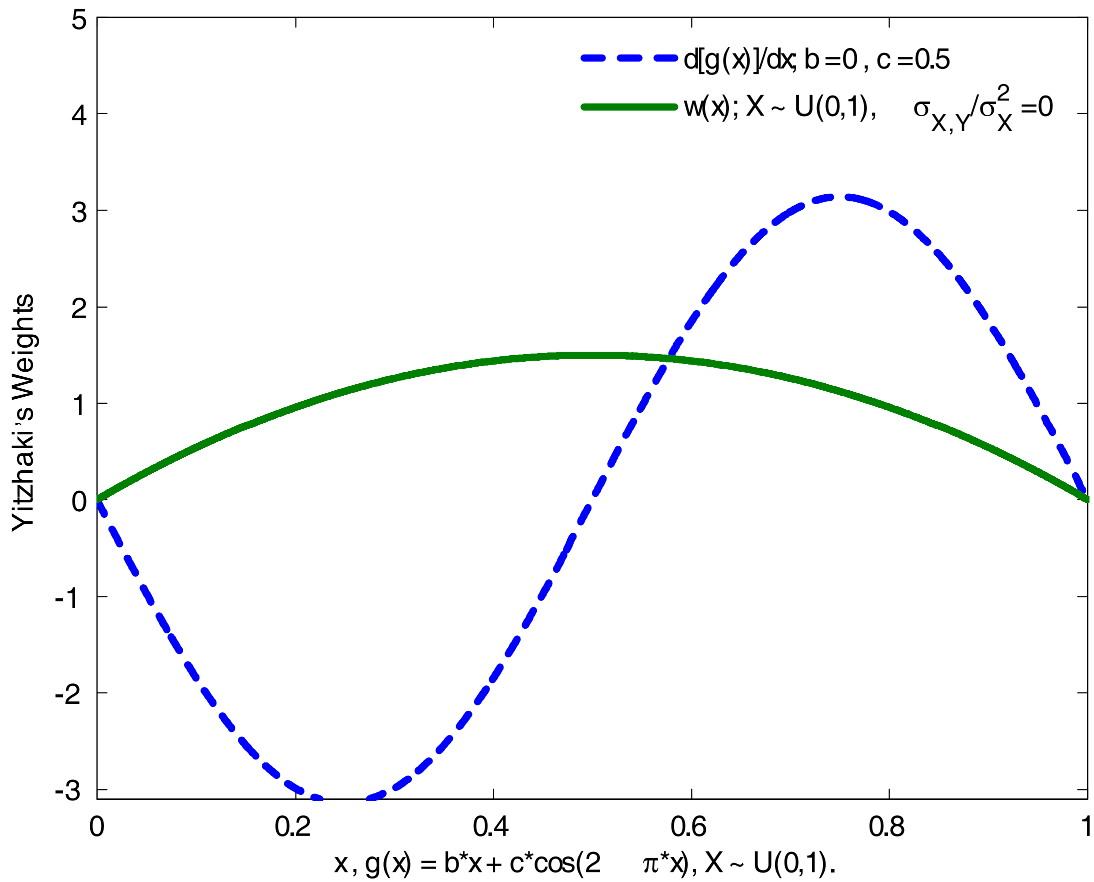

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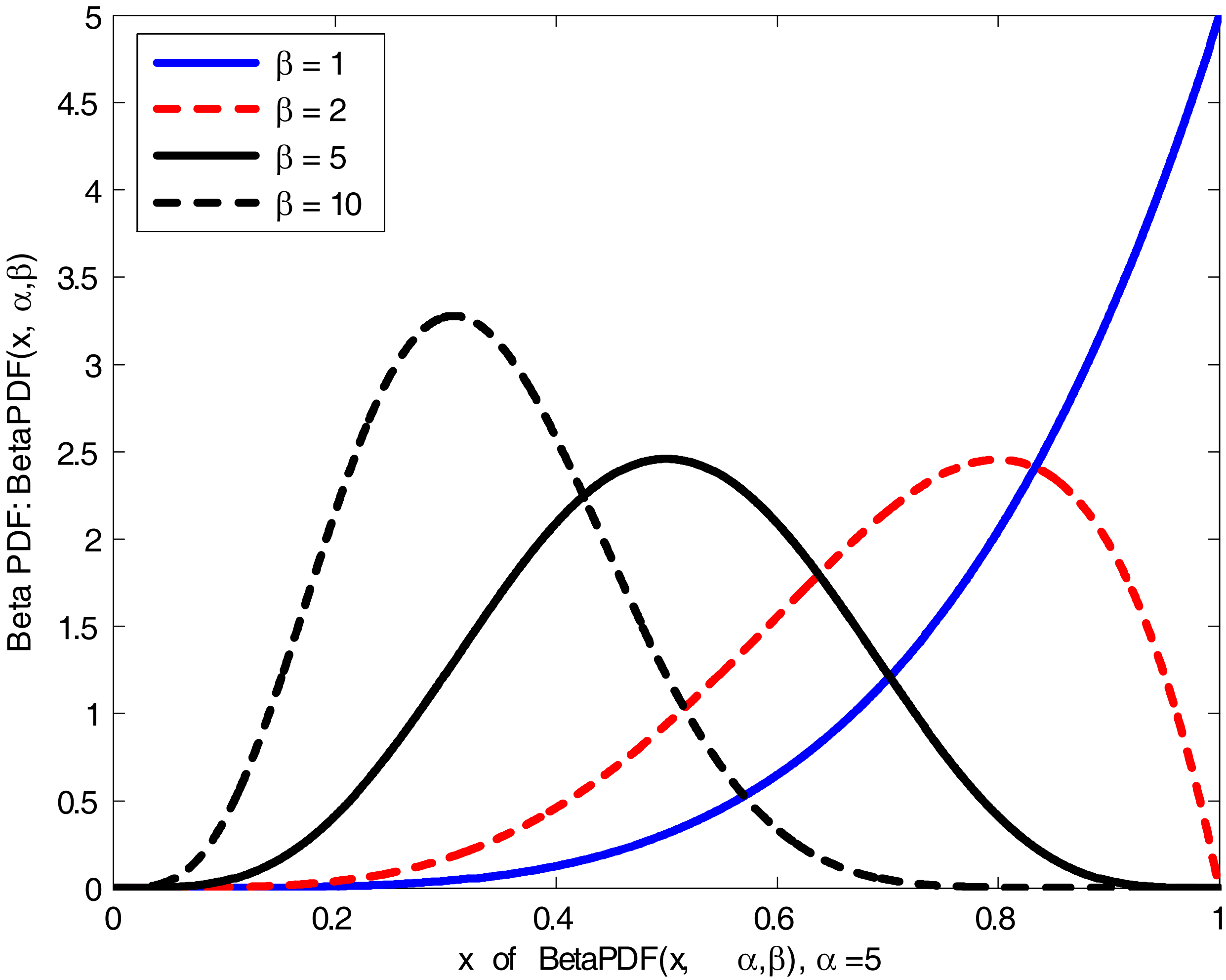
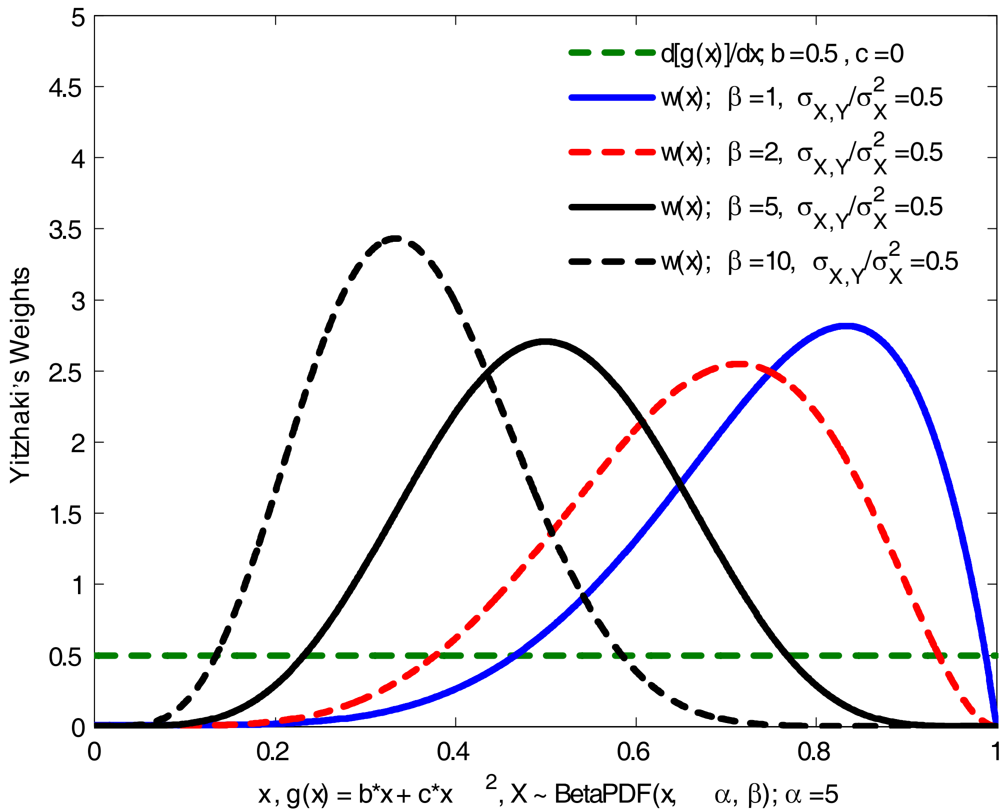
The Beta Probability Density Function



$$BetaPDF(x, \alpha, \beta) = \frac{x^{\alpha-1}(1-x)^{\beta-1}}{B(\alpha,\beta)};\ \alpha = 5;$$

Yitzhaki's Weights for $\mathbf{X} \sim BetaPDF(x, \alpha, \beta)$



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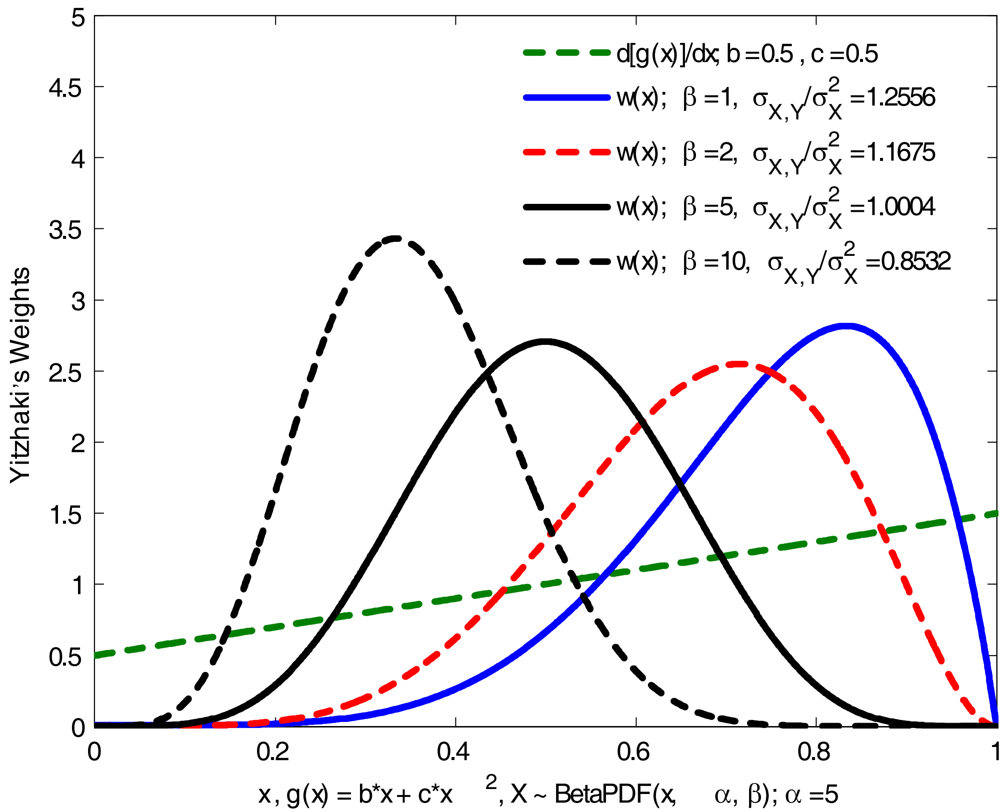

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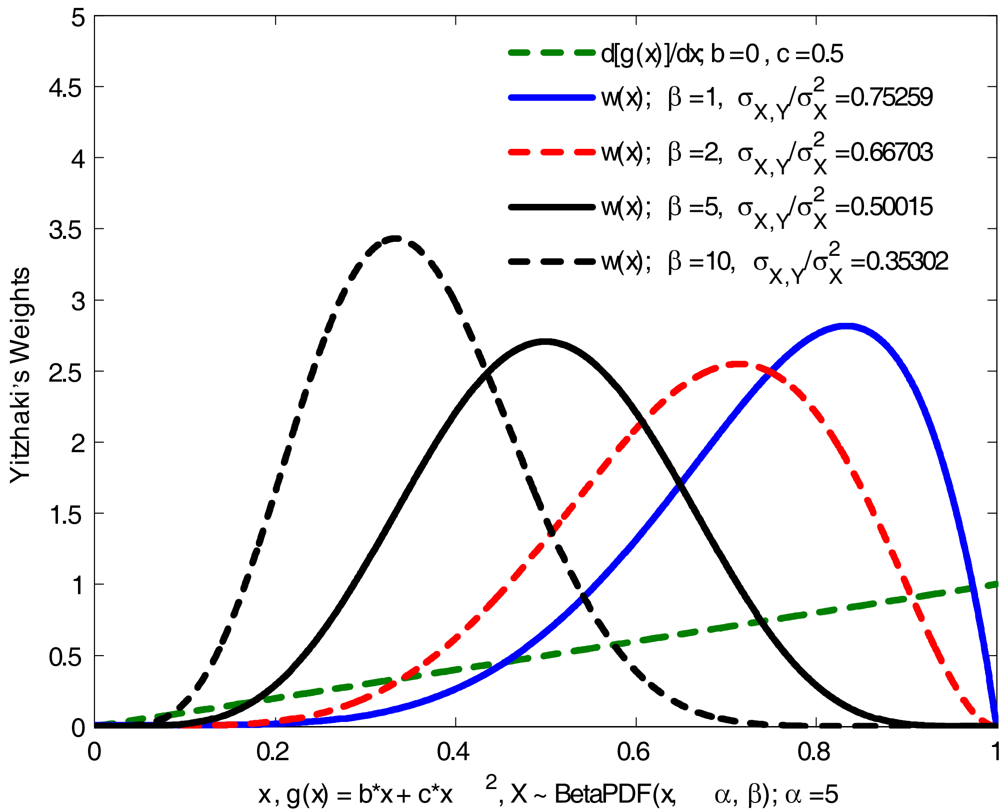

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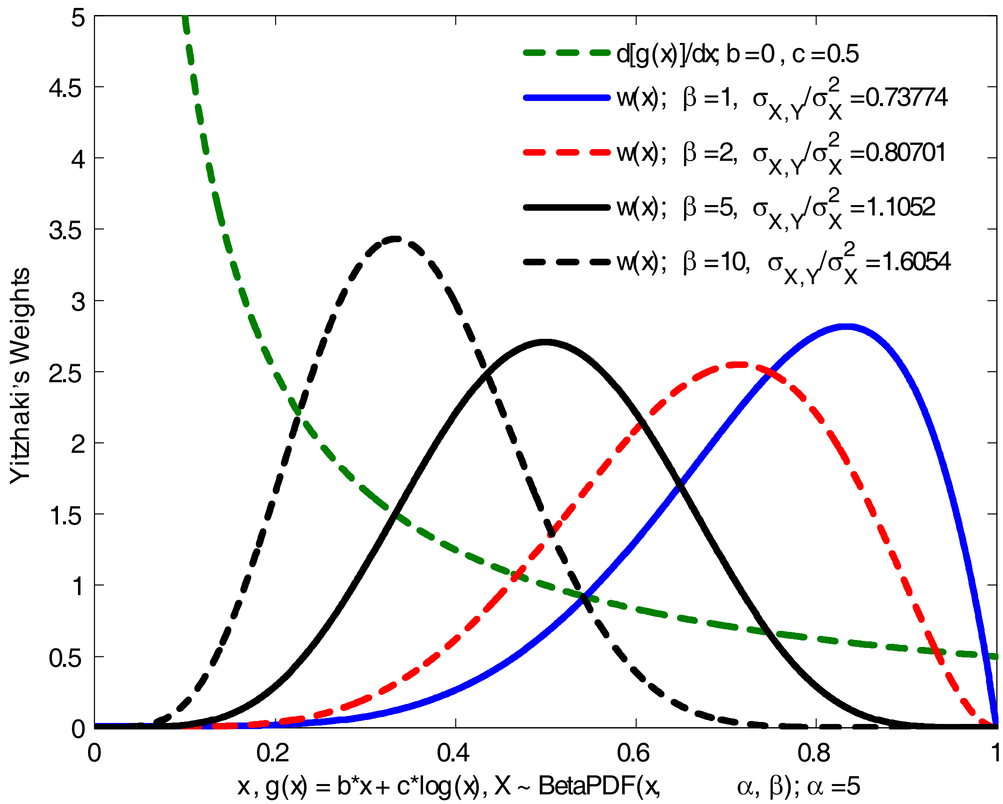

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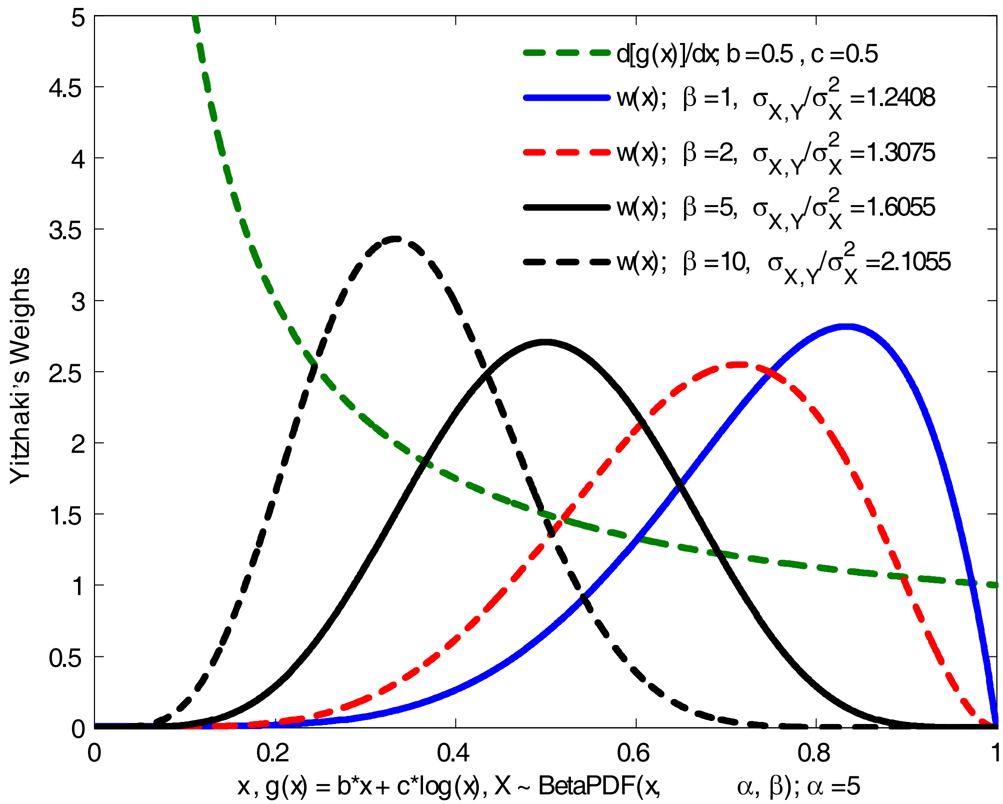

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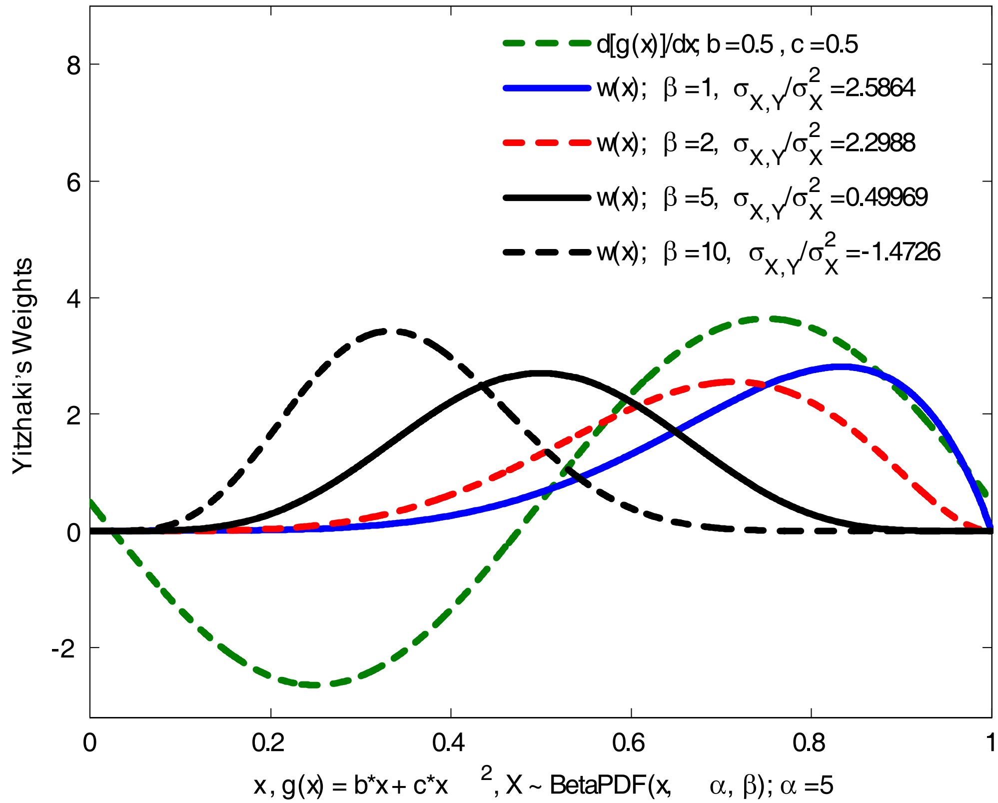

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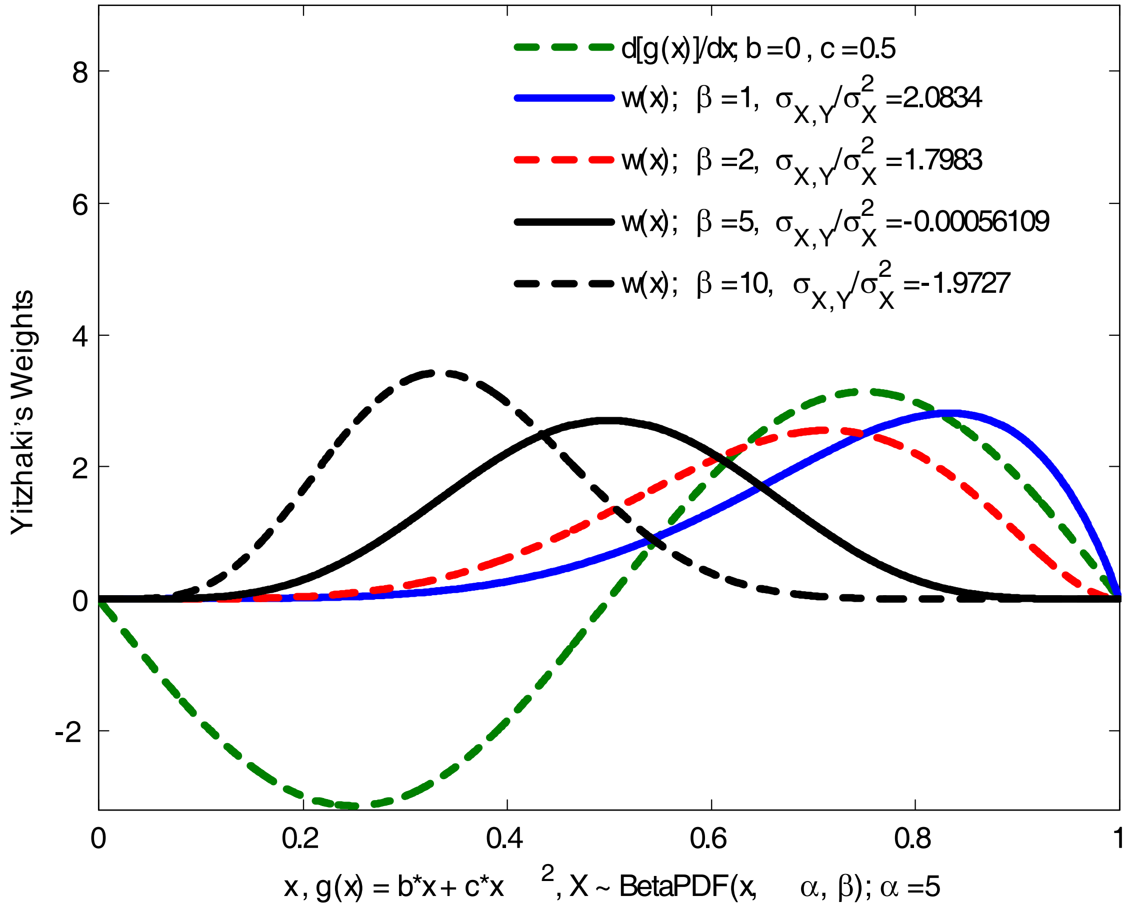

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