

Appendix

A NFP Randomization Protocol

Pregnant women were enrolled as they visited the Medical Center during pregnancy. The randomization protocol was sequential, that is to say that each participant was randomized according to the order of enrollment. Pregnant women who accepted to enroll were classified in strata defined by 5 characteristics:

1. Maternal race (African American vs non-African American);
2. Maternal age (< 17 , $17 - 18$, > 18 years);
3. Gestational age at enrollment (< 20 , ≥ 20 weeks);
4. Employment status of the head of household and
5. 4 geographic regions of residence.¹⁷

Within strata, randomization was performed following the [Soares and Wu \(1983\)](#) method as follows:

1. If the participant had a sibling already enrolled in the program, the participant was assigned to the same treatment status of the elder sibling.
2. Else, the participant was randomized according to control (C) or treatment group (T). However, if the sample size difference between treatment and control group is larger than a threshold, the participant is deterministically assigned to the treatment status that has fewer participants.
3. Next the participant was randomized again into her final treatment status. If in step 2 the participant was assigned to the control, she is next randomized to:
 - *Group 1*: control women that received free transportation to and from their prenatal appointments (sample size: 166).
 - *Group 2*: control women that received developmental screening and referral services at ages 6, 12 and 24 months in addition to the benefits of Group 1 (sample size: 514).

If she was assigned to the treatment group previously, she is next randomized into

- *Group 3*: treated women that had home visits by nurses during pregnancy, one visit in the hospital and one visit at home after childbirth in addition to the benefits of Group 2 (sample size: 230).
- *Group 4*: treated women that received home visits by nurses during pregnancy until the child's 2^{nd} birthday in addition to the benefits of Group 2 (sample size: 228)

¹⁷The regions are: Inner City, Bisson, Cawthon and Hollywood.

As in the previous step, if the absolute difference in group size exceed some threshold then the participant was deterministically assigned to the group with the lowest number of participants. Otherwise, the pregnant woman was randomly assigned.

Importantly, the randomization method incorporated a trigger mechanism that deterministically assigned a treatment status to participants if the sequence of assignments became too imbalanced due to sampling variation. In this context, imbalance was measured by the difference of persons assigned to T and the persons assigned to C. In practice less than 1% of the women were assigned according to the trigger mechanism. Thus, the NFP Memphis trial can be treated as a non-sequential protocol.

B Instruments

B.1 HOME

The Home Observation for Measurement of the Environment (HOME) was first developed in the 1960s by Caldwell. It measures the quality and quantity of stimulation and support available to a child at home (Bradley and Caldwell (1984)). The test is based on the child and is carried on during a visit of 45 to 90 minutes. A more in depth explanation of the HOME inventory is in Bradley and Caldwell (1984).

There are several versions of the inventory. The initial version, Infant/Toddler HOME, is for kids aged 0 to 3 years old. It consists of 45 binary-choice items grouped into 6 subscales. The Early Childhood HOME is for kids aged 3 to 6 years old. It consists of 55 binary-choice items clustered into 8 subscales. Finally, the Middle Childhood HOME is used for kids aged 6 to 10 years old. It consists of 59 items in 8 subscales. The NFP uses the first version of the Inventory, the Infant/Toddler HOME.

The 45 items of the HOME inventory contain the six following subscales:

1. *Emotional and Verbal Responsiveness of the Mother (11 items): measures the mother's ability to communicate with the child.*
2. *Avoidance of Restriction and Punishment (8 items): measures the mother's ability to discipline the child.*
3. *Organization of the Environment (6 items): measures the daily changes in the child's environments.*
4. *Provision of Appropriate Play Material (9 items): measures the types of toys and their contributions to the child's motor skills.*
5. *Maternal Involvement with Child (6 items): measures the aspects in which the mother is involved in the child's daily life.*
6. *Opportunities for Variety in Daily Stimulation (5 items): measures the levels of interaction the mother and other family members have with the child.*

The NFP measured the HOME Inventory when the child was 12 and 24 months old.

B.2 KABC

The Kafuman Assessment Battery for Children (KABC) was developed by Alan S. Kaufman and Nadeen L. Kaufman in 1983 with a later revision in 2004. The KABC focuses on processes required to solve problems compared to intelligence. The KABC contains 16 subtests (10 mental processing and 6 achievement), which can be grouped into 3 scales. Due to the nature of the subtests, 13 subtests can be taken at once, with the mandatory age range to be between 7 to 12.5 years old. The NFP used the following 11 subtests:

1. *Sequential Processing Scale (Hand Movements, Number Recall, Word Order): measures short-term memory and problem-solving skills. It emphasizes how children are able to follow ordered sequences.*
2. *Simultaneous Processing Scale (Gestalt Closure, Triangles, Matrix Analogies, Spatial Memory, Photo Series): measures problem-solving skills. It involves several processes at once such as scenes in a partially completed picture.*
3. *Achievement Scale (Arithmetic, Riddles, Reading/Decoding): measures achievement and focus on applied skills and facts learned through the home/school environment.*

The NFP Program used these three scales when the child was 6 years old.

B.3 PPVT

The Peabody Picture Vocabulary Test (PPVT) is an individual verbal intelligence test that measures receptive vocabulary, developed by Llyod M. Dunn and Leota M. Dunn in 1959. It is a verbal test that lasts between 20 and 30 minutes. The child is presented a series of pictures. There are four pictures in a page. The examiner states a word and asks the child to associate it with a picture. The diffusion of the figures increases over time. The exam stops when the child answers six out of eight questions incorrectly. After completion, a raw score is given, normalized to a mean of 100 and standard deviation of 15. The NFP Program used PPVT when the child was 6 years old.

B.4 WISC-III

The Wechsler Intelligence Scale for Children — Third Edition (WISC-III) was created in 1949. The third edition was published in 1991 (Wechsler, 1991). WISC is an intelligence test for children between the ages 6 and 16 years old. It can be completed without reading or writing. The exam takes between 65 and 80 minutes. There are two subscales: verbal and performance, which provide a Verbal IQ (VIQ), a Performance IQ (PIQ), and a Full Scale IQ (FSIQ). The NFP only used the coding, part of the Processing Speed Index.

1. *Coding: the child marks rows of shapes with different lines to transcribe a digit-symbol code. It measures visual or motor integration and visual scanning.*

The NFP Program used WISC-III when the child was 6 years old.

B.5 CBCL

The Child Behavior Checklist (CBCL) is a parent-report questionnaire developed by Thomas M. Achenbach. In it, the child is rated on several behavioral and emotional problems. The goal of the inventory is to assess internalizing and externalizing behaviors. The responses are recorded using a Likert scale: 0 = Not True, 1 = Sometimes True, 2 = Very True. The preschool checklist (18 months to 5 years) contains 100 questions and the school-age checklist (6 to 18 years) contains 120 questions. The preschool checklist questions can be broken down into the following subscales: anxious/depressed, withdrawn, sleeping problems, somatic problems, aggressive behavior, and destructive behavior. The school-age checklist questions can be broken down into the following subscales: withdrawn, somatic complaints, anxious/depressed, social problems, thought problems, attention problems, delinquent behavior, aggressive behavior, and other problems. The NFP Program used the CBCL when the child was 2 and 6 years old.

B.6 C-DISC

The Computerized Diagnostic Interview Schedule for Children (C-DISC) is a comprehensive and structured interview that studies mental health disorders such as general anxiety, panic, eating, elimination, depression, ADHD, and conduct. The majority of the questions are “yes and no”. Some questions have additional options such as “sometimes”. The C-DISC has about 3,000 questions with 358 core questions that the child must answer. About 1300 questions are asked depending on the answer to the core questions. There are 732 questions that ask about age of onset and treatment for reported symptoms. Lastly, there are about 700 questions from the optional whole-life module. The NFP Program used C-DISC when the child was 9 years old.

B.7 MacArthur

The MacArthur Story Stem Battery (MSSB) was created by the MacArthur Narrative Working Group that included Bretherton, Buchsbaum, and several other collaborators. The story stem method is where the examiner presents a story to the child that culminates at a high point, at which the child is then asked to complete the story; this type of method allows insight into the child’s inner workings of the mind. The

MSSB uses 15 stories and measures: dysregulated aggression, empathy/warmth, emotional integration, and performance anxiety.

1. *Dysregulated Aggression Dimension: aggression, injury, danger, destruction, dishonesty, escalation of conflict, negative story endings, inappropriate child power, controlling toward examiner.*
2. *Empathy/Warmth Dimension: empathy-helping, affiliation, affection, reparation or guilt, parental warmth.*
3. *Emotional Integration Construct: ability to maintain story coherence with the inclusion of emotional expression. The affects included are joy, anger, distress, concern, sadness.*
4. *Avoidance or Withdrawal Dimension: characters leaving the scene repetition of previous story fragments, denial of central conflict or challenge, family characters leave, avoiding separation from parents, dissociative behaviors.*
5. *Performance Anxiety Dimension: unwillingness to verbalize, unresponsiveness to examiner, anxious behaviors.*

The NFP Program used the MSSB when the child was 6 years old.

C Method for Permutation-based Inference

As mentioned, the standard model of program evaluation describes the observed outcome Y_i of participant $i \in J$ by

$$Y_i = D_i Y_{i,1} + (1 - D_i) Y_{i,0}, \quad (15)$$

where $J = \{1, \dots, N\}$ denotes the sample space indexing set, D_i denotes the treatment assignment for participant $i \in J$, ($D_i = 1$ if treatment occurs, $D_i = 0$ otherwise) and $(Y_{i,0}, Y_{i,1})$ are potential outcomes for participant i when treatment is *fixed* at control and treatment status respectively.

Randomized experiments solve potential problems of selection bias by inducing independence between counterfactual outcomes $(Y_{i,0}, Y_{i,1})$ and treatment status D_i when conditioned on the pre-program variables X used in the randomization protocol. All variables are defined in the common probability space (Ω, \mathcal{F}, P) . In our notation, a randomized experiment must satisfy the following assumption:

Assumption A-1. $Y(\mathbf{d}) \perp\!\!\!\perp D \mid X; \mathbf{d} \in \text{supp}(D),$

where variables $X = (X_i; i \in J), D = (D_i; i \in J)$ are N -dimensional vectors of treatment assignments and pre-program variables, and $Y(\mathbf{d}) = (Y_{i,d_i}; i \in J, d_i \in \{0, 1\})$ and $\mathbf{d} \in \text{supp}(D) = \{0, 1\}^{|J|}$ denotes the vector of counterfactual outcomes. In the same fashion, we represent the vector of observed outcomes of Equation (15) by $Y = (Y_i; i \in \mathcal{I})$. The no treatment hypothesis is equivalent to the statement that the conditional counterfactual outcome vectors share the same distribution:

Hypothesis H-1. $Y(\mathbf{d}) \stackrel{d}{=} Y(\mathbf{d}') \mid X ; \mathbf{d}, \mathbf{d}' \in \text{supp}(D),$

Hypothesis **H-1** can be restated in more tractable form:

Hypothesis H-1'. Under Assumption **A-1** and Hypothesis **H-1**, we have that $Y \perp\!\!\!\perp D \mid X.$

Testing Hypothesis **H-1'** poses some statistical challenges. First, small sample sizes cast doubt on inference that rely on the asymptotic behavior of test statistics. We address the problem of small sample size by generating the exact of a test statistic conditioned on data. Second, the presence of multiple outcomes allows for the arbitrary selection of statistically significant outcomes. The selectively reporting statistically significant outcomes is often termed *cherry picking* and generates a downward biased inference with smaller p -values. We solve the problem of cherry picking by implementing a multiple-hypothesis testing based on the stepdown procedure of (Romano and Wolf, 2005a). They explain that the stepdown procedure strongly controls for Family-wise error rate (FWER), while classical tests do not. Also, Romano and Wolf (2005a) shows that the strong FWER control can be obtained by ensuring a certain monotonicity condition on the test statistics. This requirement is weaker than the assumption of subset pivotality, used in various methods of resampling outcomes presented in Westfall and Young (1993).

In summary, our method is based on three steps. First, we seek to characterise the exact conditional distribution of $D|X$. Specifically we characterize the a multiset $D_x(\mathbf{d})$, defined by:

$$D_x(\mathbf{d}) = \{\mathbf{d}' \in \{0, 1\}^{|J|} ; P(D = \mathbf{d}|X = x) = P(D = \mathbf{d}'|X = x)\},$$

such that the distribution of D conditioned on realised data is uniform among elements of $D_x(\mathbf{d})$. Next we use the assumption of null hypothesis of no treatment effects, i.e. $H_0 : Y \perp\!\!\!\perp D|X$, to generate the exact conditional distribution of a test statistic $T(Y, D)|X$. Upon it, we can construct an inference that controls for the probability of falsely rejecting the null hypothesis. We control for this probability in two ways: (1) in the case of single (joint) null hypothesis, we control for the standard Type-I error; (2) in the case of multiple hypothesis inference, we control for the Family-wise error rate.

More notation is necessary to describe the method. Let K represent the indexing set for all available outcomes $Y_k; k \in K$. We represent the single (joint) null hypothesis that a set $L \subset K$ of outcomes $Y_k; k \in L$ are jointly independent of treatment status D conditional on pre-program variables X by

$$H_L : Y_L \perp\!\!\!\perp D|X, \text{ where } Y_L = (Y_k : k \in L). \quad (16)$$

When L is a singleton, say $L = \{k\}$, then the null hypothesis is given by $H_{\{k\}} : Y_k \perp\!\!\!\perp D|X$. In this notation, we can write the joint Hypothesis H_L as $H_L = \cap_{k \in L} H_{\{k\}}$.

Our goal is to test a single (joint) null hypothesis controlling for the probability of a Type I error at level α , that is, $P(\text{reject } H_L | H_L \text{ is true}) \leq \alpha$. To do so, we rely on the fact that, under Hypothesis (16),

$$(Y_L, D) | X \stackrel{d}{=} (Y_L, gD) | X \quad \forall g \in \mathbf{G}_X, \quad (17)$$

where \mathbf{G}_X comprises all the permutations within strata of X , that is,

$$\mathbf{G}_X = \{g ; g : J \rightarrow J \text{ is a bijection and } g(j) = j' \Rightarrow (X_j) = (X_{j'})\},$$

and gD is a vector defined by:

$$gD = (\tilde{D}_i \in \text{supp}(D); i \in J \text{ and } \tilde{D}_i = D_{g(i)}).$$

We use Relation (17) to generate a statistical test whose exact distribution the test statistic $T_L(Y_L, gD)$ is obtained by re-evaluating $T_L(Y_L, gD)$ as g varies in \mathbf{G}_X . Note that the inference on Hypothesis 16 is dependent on the choice of statistics. That is to say that even though any statistics $T_L(Y_L, D)$ whose value provide evidence against the null hypothesis can be used, the inference is dependent on this choice of statistic. An example of such statistic is the maximum of the t-statistic associated with the difference in means between treated and control groups over outcomes Y_k such that $k \in L$. Formally,

$$T_L(Y_L, D) = \max_{k \in L} T_k(Y_k, D), \quad (18)$$

where $T_k(Y_k, D)$ is the t-statistics for outcome Y_k . Relation (17) implies that $T_L(Y_L, D) | X \stackrel{d}{=} T_L(Y_L, gD) | X$ for any $g \in \mathbf{G}_X$. Moreover, let $\mathbf{d} \in \{0, 1\}^{|J|}$ such that $P(D = \mathbf{d} | X = x) > 0$, then the distribution of D conditioned on $X = x$ is uniform across elements of $\mathbf{D}_x(\mathbf{d})$ (see [Lehmann and Romano \(2005\)](#), Chapter 15). Thus, a critical value $c_{L,x}(Y_L, \mathbf{d}, \alpha)$ such that $P(T_L(Y_L, D) > c_{L,x}(Y_L, \mathbf{d}, \alpha) | X = x, H_L \text{ is true}) \leq \alpha$ can be computed as:

$$c_{L,x}(Y_L, \mathbf{d}, \alpha) = \inf_{t \in \mathbf{R}} \left\{ \sum_{\mathbf{d}' \in \mathbf{D}_x(\mathbf{d})} I\{T_L(Y_L, \mathbf{d}') \leq t\} \geq (1 - \alpha) |\mathbf{D}_x| \right\},$$

where $I\{\cdot\}$ is the indicator function. The following notation is useful to further characterize $c_{L,x}(Y_L, \mathbf{d}, \alpha)$. Let $T_{L,x}^{(1)}, \dots, T_{L,x}^{(|\mathbf{D}_x(\mathbf{d})|)}$ be the sequence of increasing ordered statistics $T_L(Y_L, \mathbf{d}')$ as \mathbf{d}' varies in $\mathbf{D}_x(\mathbf{d})$. In this notation we can write the critical value as

$$c_{L,x}(Y_L, \mathbf{d}, \alpha) = T_{L,x}^{(\lceil (1-\alpha) |\mathbf{D}_x| \rceil)} \quad (19)$$

where $\lceil a \rceil$ stands for the smallest integer bigger or equal than a .

Under the null hypothesis H_L , the probability of a test statistic be bigger or equal than the statistic $T_L(Y_L, \mathbf{d})$ actually observed, i.e. the p-value, is given by:

$$p_{L,x}(\mathbf{d}) = \inf_{\alpha \in [0,1]} \left\{ c_{L,x}(Y_L, \mathbf{d}, \alpha) \leq T_L(Y_L, \mathbf{d}) \right\}. \quad (20)$$

Now let $r_{L,x} \in \{1, \dots, |\mathbf{D}_x(\mathbf{d})|\}$ be the lowest rank that the value of the observed test statistic $T_L(Y_L, \mathbf{d})$ takes in the sequence $T_{L,x}^{(1)}, \dots, T_{L,x}^{(|\mathbf{D}_x(\mathbf{d})|)}$, that is to say:

$$r_{L,x} = 1 + \sum_{\mathbf{d}' \in \mathbf{D}_x(\mathbf{d})} I\{T_L(Y_L, \mathbf{d}') < T_L(Y_L, \mathbf{d})\}.$$

Thus:

$$T_{L,x}^{(r_{L,x})} = T_L(Y_L, \mathbf{d}). \quad (21)$$

Then, by the ordered property of $T_{L,x}^{(r)}$; $r \in \{1, \dots, |\mathbf{D}_x(\mathbf{d})|\}$ and the definition of $r_{L,x}$, we have that:

$$p_{L,x}(\mathbf{d}) = 1 - \frac{r_{L,x}}{|\mathbf{D}_x(\mathbf{d})|}. \quad (22)$$

Moreover, p-value $p_{L,x}(\mathbf{d})$ complies with the following property:

$$\Pr(p_{L,x}(\mathbf{d}) \leq \phi | X = x) \leq \phi \forall \phi \in [0, 1].$$

We implemented a inference method that tests for the multiple null hypothesis that each outcome $Y_k; k \in L$ is independent of treatment status D conditional on pre-program variables X . The representation of these multiple hypothesis in the same fashion as the single (joint) null hypothesis, namely:

$$H_L = \cap_{k \in L} H_{\{k\}} ; H_{\{k\}} : Y_k \perp\!\!\!\perp D | (Z, U).$$

The multiple hypothesis testing differs from the single (joint) hypothesis testing in the way it controls for the probability of false rejection. Specifically, let the subset L_0 be the set of true Hypothesis $H_{\{k\}}$ such that $k \in L_0 \subset L$. Our multiple hypothesis testing controls for the familywise error rate (FWER), that is, the probability of even one false rejection among the set of true hypothesis L_0 . Formally, we control for:

$$\Pr(\text{reject at least one } H_{\{k\}}; k \in L_0 | H_{L_0} \text{ is true}) \leq \alpha,$$

while single (joint) hypothesis testing controls for $P(\text{reject } H_L | H_L \text{ is true}) \leq \alpha$.

Bonferroni or Holm are examples of inference methods that test multiple hypothesis controlling for FWER. These methods rely upon a “least favorable” dependence structure among the p-values. The step-down procedure of [Romano and Wolf \(2005a\)](#) is less conservative as it accounts for the information about the dependence structure of p -values. The method is based on the monotonicity assumption, which, in our case, can be stated as:

$$c_{K,x}(Y_K, \mathbf{d}, \alpha) \geq c_{L_0,x}(Y_{L_0}, \mathbf{d}, \alpha) \text{ for any subset } K \text{ of } L \text{ containing } L_0 \text{ i.e. } L_0 \subset K \subset L. \quad (23)$$

Assumption (23) is satisfied by our choice of test statistic (18) and the fact that $L_0 \subset K$.

The stepdown procedure given in [Romano and Wolf \(2005a\)](#) is a stepwise method summarized in the following algorithm:

Algorithm 1.

Step 1: Set $L_1 = L$. If

$$\max_{k \in L_1} T_k(Y_k, \mathbf{d}) \leq c_{L,x}(Y_{L_1}, \mathbf{d}, \alpha), \quad (24)$$

then stop and reject no null hypotheses; otherwise, reject any $H_{\{k\}}$ with

$$T_k(Y_k, \mathbf{d}) > c_{L,x}(Y_{L_1}, \mathbf{d}, \alpha)$$

and go to Step 2.

\vdots

Step j : Let L_j denote the indices of remaining null hypotheses. If

$$\max_{k \in L_j} T_k(Y_k, \mathbf{d}) \leq c_{L,x}(Y_{L_j}, \mathbf{d}, \alpha), \quad (25)$$

then stop and reject no further null hypotheses; otherwise, reject any $H_{\{k\}}$ with

$$T_k(Y_k, \mathbf{d}) > c_{L,x}(Y_{L_j}, \mathbf{d}, \alpha)$$

and go to Step $j + 1$.

\vdots

We can compute the multiplicity-adjusted p -values of Equations(24)–(25) in the same fashion described by Equations (20)–(22).

C.1 Conditioning and Linearity

A typical problem in small sample randomized trials is sampling variation, where pre-program variables differ across treatment groups by chance. One can increase the power of a statistical inference by conditioning on those pre-program variables. Let Z be the pre-program variables that were not used in the randomization protocol and we ought to control for.

Variables Z precede the treatment intervention and therefore $Z \perp\!\!\!\perp D | X$ holds due to randomization. Under the hypothesis of no-treatment, $Y \perp\!\!\!\perp D | X$ also holds. These two relations imply that $Y \perp\!\!\!\perp D | (X, Z)$. Likewise Section 4.1, we can use this relation to generate a permutation test that consider the strata formed by values of covariates X and Z . This way we can generates an inference method that non-parametrically condition on variables X and Z .

Non-parametric conditioning through block permutation comes at a cost. A fine conditioning set decreases the share of available data that can be permuted and a sufficiently large conditioning set prohibits the implementation of a permutation-based test. We solve this problem by evoking linearity. That is to say, we condition variables through a linear regression instead of a non-parametric block permutation. [Anderson and Legendre \(1999\)](#) tested a range of permutation methods for linear models. They found that [Freedman and Lane \(1983\)](#) generated the most consistent and reliable results among the available models in this literature.

We non-parametrically condition on variables used in the randomization protocol to achieve valid exchangeable properties (i.e. we use permutations in \mathcal{G}_X); We linearly condition on additional pre-program variables Z not used in the randomization protocol. According to [Freedman and Lane \(1983\)](#) method, our approach can be summarized by the following steps: (1) compute the residuals $Y - Z\hat{\beta}$ such that $\hat{\beta} = (Z'Z)^{-1}Z'Y$; (2) permute these residuals according to permutations $g \in \mathcal{G}_X$. (3) add these permuted residuals to $Z\hat{\beta}$, call it \tilde{Y} ; (4) regress \tilde{Y} on Z and the treatment statuses D . (5) we then use the t-statistic associated with covariate D of the last regression as test statistic.

As mentioned, [Beaton \(1978\)](#) and [Freedman and Lane \(1983\)](#) suggested a permutation inference based on Shuffle Residuals. Buy this I mean regressing Y on X , shuffling the residuals from this regression, and adding them to the predicted Y , say \hat{Y} , to form a new variable, say \tilde{Y} , which is then regressed on Z and D . Formally, let the regression:

$$Y = Z\beta + D\delta + \epsilon,$$

where Z stands for the pre-program variables we wish to control for and includes a vector of elements ones

that play the role of a contant term for the regression. Error term ϵ is a mean-zero exogenous random variable independent of Z and D .

Now let $B_g; g \in \mathcal{G}_X$ be a permutation matrix associated with a permutation g in \mathcal{G}_X . Let also the operator that projects a vector in the orthogonal space generated by columns of Z be $M_Z = I - Z(Z'Z)^{-1}Z'$, where I denotes the identity matrix. As properties of Matrix M_Z , we can say that M_Z is symmetric and idempotent, that is:

$$M_Z = M'_Z = M_Z M_Z = M'_Z M_Z. \quad (26)$$

The estimated residuals of Y generated by the the regression

$$Y = Z\beta + \epsilon$$

is given by $\hat{e} = M_Z Y$. The predicted outcome based on this regression is given by: $\hat{Y} = Z(Z'Z)^{-1}X'Y$.

We define the new outcome based on the sum of the predicted outcome \hat{Y} with permuted errors \hat{e} according to permutation $g \in \mathcal{G}_X$ as

$$\tilde{Y} = \hat{Y} + B_g \hat{e}. \quad (27)$$

We then use the newly computed outcome in the following regression:

$$\tilde{Y} = Z\beta + D\delta + \tilde{\epsilon}. \quad (28)$$

We now examine the δ estimate on Equation (28). This estimate ia actually the same as the one computed by the following regression:

$$M_Z \tilde{Y} = M_Z D\delta + \tilde{\epsilon}. \quad (29)$$

Thus. by applying the Ordinary Least Square formula, we obtain:

$$\hat{\delta}_g = (D'M'_Z M_Z D)^{-1} D'M'_Z M_Z \tilde{Y}. \quad (30)$$

We now use previous equations to transform Equation (30) into a more general formula:

$$\begin{aligned}
\hat{\delta}_g &= (D'M'_Z M_Z D)^{-1} D'M'_Z M_Z \tilde{Y} && \text{by (30),} \\
&= (D'M_Z D M_Z D'M_Z \tilde{Y}) && \text{by (26),} \\
&= (D'M_Z D M_Z D'M_Z (Y + B_g \hat{e})) && \text{by (27) ,} \\
&= (D'M_Z D M_Z D'M_Z ((I - M_Z)Y + B_g \hat{e})) && \text{because } M_Z = I - Z(Z'Z)^{-1}Z', \\
&= (D'M_Z D M_Z D'((M_Z - M_Z)Y + M_Z B_g \hat{e})), \\
&= (D'M_Z D M_Z D'(M_Z B_g \hat{e})), \\
&= (D'M_Z D M_Z D'(M_Z B_g M_Z Y)) && \text{because } \hat{e} = M_Z Y. \quad (31)
\end{aligned}$$

Kennedy (1995) pointed out that Freedman and Lane (1983) algorithm is summarized by Equation 31. Notationally, we can use $T_Z(Y, gD); g \in \mathcal{G}_X$ (instead of $T(Y, gD); g \in \mathcal{G}_X$) to represent the distribution of the test statistic associated with the t-statsitic of the D covariate in the Freedman and Lane (1983) regression just described. Using this notation, the analysis of the previous sections holds unaltered.

D Additional Baseline Tables

These tables explore differences in pre-program variables between treatment and control groups at each follow up wave. These results are presented in order to highlight that there were no differential patterns of attrition across waves.

Table D.1: Descriptive Statistic of Baseline Characteristics (Year 6)

	Whole Sample						Female Sample						Male Sample					
	C Mean	C SD	T Mean	T SD	Pval	C Mean	C SD	T Mean	T SD	Pval	C Mean	C SD	T Mean	T SD	Pval	C Mean	C SD	T Mean
<i>Background Characteristics</i>																		
Maternal Race (Black)	0.060	0.238	0.100	0.301	0.100	0.067	0.251	0.081	0.274	0.668	0.054	0.226	0.119	0.325	0.070			
Marital Status (Married)	0.016	0.124	0.015	0.122	0.952	0.009	0.094	0.010	0.101	0.922	0.022	0.148	0.020	0.140	0.883			
Maternal Age	18.060	3.220	18.060	3.294	0.999	18.219	3.299	18.152	3.607	0.874	17.902	3.138	17.970	2.971	0.850			
Years of Education	10.263	1.881	10.120	2.024	0.395	10.313	1.841	10.081	2.069	0.339	10.214	1.922	10.158	1.989	0.813			
Mother in School	0.649	0.489	0.580	0.495	0.497	0.570	0.496	0.616	0.489	0.432	0.647	0.479	0.545	0.500	0.084			
Head of Household is Employed	0.562	0.497	0.492	0.501	0.106	0.605	0.490	0.475	0.502	0.031	0.518	0.501	0.510	0.502	0.897			
% of Census Tract Below Poverty	34.812	21.371	35.518	20.221	0.687	33.195	20.304	36.724	22.248	0.179	36.428	22.316	34.336	18.049	0.371			
Household Density	0.940	0.497	1.027	0.569	0.064	0.961	0.499	1.070	0.669	0.151	0.920	0.495	0.986	0.451	0.236			
<i>Total Household Income (Past 6 Months)</i>																		
Less than \$3000	0.283	0.451	0.365	0.483	0.044	0.290	0.455	0.364	0.483	0.202	0.277	0.448	0.366	0.484	0.116			
\$3000 - \$6999	0.237	0.425	0.225	0.419	0.746	0.219	0.414	0.222	0.418	0.945	0.254	0.437	0.228	0.421	0.601			
\$7000 - \$10999	0.228	0.420	0.205	0.405	0.515	0.219	0.414	0.222	0.418	0.945	0.237	0.426	0.188	0.393	0.317			
Greater than \$11000	0.161	0.368	0.125	0.332	0.222	0.188	0.391	0.081	0.274	0.005	0.134	0.341	0.168	0.376	0.434			
Income, No Response	0.092	0.289	0.080	0.272	0.625	0.085	0.279	0.111	0.316	0.476	0.098	0.298	0.050	0.218	0.099			
<i>Region of Residence</i>																		
Inner City	0.295	0.456	0.290	0.455	0.905	0.286	0.453	0.303	0.462	0.755	0.304	0.461	0.277	0.450	0.628			
Bisson	0.192	0.394	0.215	0.412	0.506	0.179	0.384	0.232	0.424	0.282	0.205	0.405	0.198	0.400	0.879			
Cawthon	0.194	0.396	0.190	0.393	0.900	0.210	0.408	0.162	0.370	0.297	0.179	0.384	0.218	0.415	0.420			
Hollywood	0.319	0.467	0.305	0.462	0.719	0.326	0.470	0.303	0.462	0.684	0.313	0.465	0.307	0.464	0.920			
<i>Maternal Mental Health</i>																		
Maternal IQ (Shipley)	96.270	10.287	96.440	10.360	0.847	96.223	10.279	96.061	10.618	0.898	96.317	10.317	96.812	10.140	0.686			
Maternal Bayolek Score	99.794	7.657	101.133	8.502	0.057	100.091	7.411	101.431	8.727	0.186	99.499	7.899	100.842	8.309	0.173			
Maternal Mental Health	100.184	9.979	99.447	10.352	0.398	99.717	9.777	99.741	10.172	0.984	100.649	10.178	99.158	10.568	0.235			
Self-Efficacy	100.083	10.017	99.788	9.866	0.727	100.862	9.778	100.583	9.253	0.806	99.307	10.212	99.008	10.419	0.810			
Maternal Mastery	100.065	10.213	99.535	9.992	0.537	99.879	10.155	99.173	10.246	0.568	100.250	10.290	99.891	9.774	0.764			
Maternal Psychological Resources	100.060	10.045	99.533	10.649	0.554	100.030	9.711	99.619	10.634	0.743	100.090	10.390	99.448	10.715	0.615			
<i>Maternal Health Characteristics</i>																		
Maternal Height	164.557	7.253	164.064	6.569	0.397	164.331	7.404	164.472	6.546	0.865	164.781	7.108	163.651	6.601	0.170			
Pre-Pregnancy Weight	62.097	14.866	62.339	13.588	0.839	62.828	13.775	61.394	12.375	0.355	61.362	15.885	63.264	14.683	0.294			
Gestational Age (Intake)	16.560	5.794	16.630	5.728	0.887	16.402	5.746	16.364	5.596	0.955	16.719	5.850	16.891	5.870	0.807			
<i>Maternal Social Support</i>																		
Grandmother Social Support	100.197	9.474	101.517	8.566	0.081	99.357	10.486	101.434	9.100	0.073	101.034	8.285	101.599	8.054	0.563			
Husband/Boyfriend Social Support	100.030	9.994	100.704	9.754	0.421	99.892	10.057	99.907	9.524	0.990	100.169	9.952	101.484	9.960	0.272			
<i>Maternal Risky Behaviors</i>																		
Alcohol Consumption (Past 2 wks)	0.043	0.202	0.050	0.218	0.680	0.036	0.186	0.071	0.258	0.228	0.049	0.217	0.030	0.171	0.385			
Smoking (Past 3 days)	0.085	0.279	0.110	0.314	0.334	0.081	0.273	0.121	0.328	0.284	0.089	0.286	0.099	0.300	0.784			
Used Marijuana (Past 2 wks)	0.034	0.309	0.070	0.860	0.560	0.027	0.283	0.020	0.201	0.809	0.040	0.332	0.119	1.194	0.517			
Used Cocaine (Past 2 wks)	0.007	0.142	0.000	0.000	0.318	0.000	0.000	0.000	0.000	0.000	0.013	0.200	0.000	0.000	0.318			
Sexually Transmitted Diseases	0.333	0.472	0.375	0.485	0.301	0.330	0.471	0.354	0.480	0.688	0.335	0.473	0.396	0.492	0.294			

Notes: This table presents the statistical description of selected pre-program variables after 6 years of the program. The first column of the table gives the variable description. Variables are divided into groups that share similar meanings. The remainder of the table consists of the blocks of variables associated with the whole sample, the female sample and the male sample. Each block has 6 columns: (1) Control mean (C Mean), (2) Control standard deviation (C SD), (3) Treatment mean (T Mean), (4) Treatment standard deviation (T SD), and (5) Asymptotic p-value associated with the difference in means. Bold p-values indicate that the t-statistic between the control and the treatment means is significant at the 10% level.

Table D.2: Descriptive Statistic of Baseline Characteristics (Year 12)

	Whole Sample						Female Sample						Male Sample					
	C Mean	C SD	T Mean	T SD	Pval	C Mean	C SD	T Mean	T SD	Pval	C Mean	C SD	T Mean	T SD	Pval	C Mean	C SD	T Mean
<i>Background Characteristics</i>																		
Maternal Race (Black)	0.057	0.232	0.084	0.278	0.244	0.056	0.231	0.065	0.248	0.770	0.057	0.233	0.101	0.303	0.208			
Marital Status (Married)	0.014	0.119	0.010	0.102	0.690	0.005	0.069	0.011	0.104	0.603	0.024	0.153	0.010	0.101	0.346			
Maternal Age	18.052	3.215	18.047	3.268	0.986	18.258	3.324	18.174	3.581	0.847	17.842	3.093	17.929	2.960	0.812			
Years of Education	10.254	1.860	10.073	2.025	0.296	10.324	1.828	10.043	2.080	0.265	10.182	1.893	10.101	1.982	0.735			
Mother in School	0.509	0.491	0.565	0.497	0.444	0.557	0.498	0.508	0.493	0.505	0.641	0.481	0.535	0.501	0.081			
Head of Household is Employed	0.556	0.497	0.495	0.501	0.163	0.585	0.494	0.478	0.502	0.089	0.526	0.501	0.510	0.502	0.793			
% of Census Tract Below Poverty	34.800	21.380	35.727	20.185	0.606	33.632	20.150	37.208	22.390	0.189	35.990	22.550	34.351	17.900	0.492			
Household Density	0.940	0.486	1.023	0.559	0.081	0.969	0.483	1.049	0.662	0.299	0.911	0.488	0.998	0.445	0.123			
<i>Total Household Income (Part 6 Months)</i>																		
Less than \$3000	0.280	0.449	0.361	0.482	0.048	0.277	0.449	0.337	0.475	0.305	0.282	0.451	0.384	0.489	0.083			
\$3000 - \$6999	0.242	0.429	0.236	0.425	0.870	0.239	0.428	0.239	0.429	0.995	0.244	0.431	0.232	0.424	0.822			
\$7000 - \$10999	0.230	0.421	0.188	0.392	0.238	0.230	0.422	0.217	0.415	0.808	0.230	0.422	0.162	0.370	0.151			
Greater than \$11000	0.159	0.366	0.126	0.332	0.269	0.178	0.384	0.087	0.283	0.022	0.139	0.347	0.162	0.370	0.606			
Income, No Response	0.090	0.287	0.089	0.285	0.967	0.075	0.264	0.120	0.326	0.251	0.105	0.308	0.061	0.240	0.166			
<i>Region of Residence</i>																		
Inner City	0.291	0.455	0.283	0.452	0.825	0.282	0.451	0.293	0.458	0.836	0.301	0.460	0.273	0.448	0.603			
Bisson	0.194	0.396	0.225	0.419	0.391	0.169	0.376	0.239	0.429	0.176	0.220	0.415	0.212	0.411	0.874			
Cavithon	0.204	0.403	0.188	0.392	0.657	0.221	0.416	0.152	0.361	0.148	0.187	0.391	0.222	0.418	0.477			
Hollywood	0.310	0.463	0.304	0.461	0.867	0.329	0.471	0.315	0.467	0.819	0.292	0.456	0.293	0.457	0.985			
<i>Maternal Mental Health</i>																		
Maternal IQ (Shipley)	96.066	9.987	96.759	10.181	0.433	96.075	10.002	96.011	10.789	0.961	96.057	9.997	97.455	9.585	0.240			
Maternal Bayley Score	99.947	7.604	101.078	8.568	0.118	100.190	7.489	101.427	8.718	0.238	99.701	7.729	100.754	8.459	0.296			
Maternal Mental Health	100.106	9.744	99.550	10.612	0.538	99.766	9.529	99.909	10.429	0.911	100.451	9.908	99.216	10.821	0.339			
Self-Efficacy	99.813	9.995	99.671	9.912	0.870	100.640	9.746	100.192	9.339	0.705	98.973	10.197	99.186	10.440	0.866			
Maternal Mastery	100.059	10.236	99.446	10.098	0.489	99.954	10.301	99.085	10.533	0.507	100.165	10.193	99.781	9.718	0.751			
Maternal Psychological Resources	99.857	9.652	99.664	10.914	0.834	99.947	9.401	99.537	10.896	0.754	99.765	9.923	99.782	10.984	0.990			
<i>Maternal Health Characteristics</i>																		
Maternal Height	164.595	7.349	164.303	6.680	0.630	164.297	7.483	164.904	6.664	0.485	164.896	7.217	163.732	6.680	0.170			
Pre-Pregnancy Weight	62.398	15.149	62.735	13.786	0.786	63.078	14.076	61.880	12.369	0.458	61.701	16.178	63.530	15.003	0.332			
Gestational Age (Intake)	16.474	5.830	16.607	5.639	0.789	16.235	5.791	16.228	5.489	0.993	16.718	5.873	16.960	5.780	0.733			
<i>Maternal Social Support</i>																		
Grandmother Social Support	100.407	9.331	101.623	8.406	0.110	99.624	10.361	101.370	9.306	0.148	101.200	8.102	101.858	7.514	0.485			
Husband/Boyfriend Social Support	100.266	9.951	100.299	9.986	0.969	100.023	9.949	99.833	9.700	0.877	100.511	9.971	100.731	10.275	0.859			
<i>Maternal Risky Behaviors</i>																		
Alcohol Consumption (Past 2 wks)	0.040	0.197	0.047	0.212	0.710	0.038	0.191	0.065	0.248	0.345	0.043	0.203	0.030	0.172	0.568			
Smoking (Past 3 days)	0.081	0.273	0.105	0.307	0.356	0.075	0.265	0.120	0.326	0.255	0.086	0.281	0.091	0.289	0.891			
Used Marijuana (Past 2 wks)	0.036	0.318	0.073	0.880	0.566	0.028	0.291	0.022	0.209	0.824	0.043	0.344	0.121	1.206	0.528			
Used Cocaine (Past 2 wks)	0.007	0.146	0.000	0.318	0.000	0.000	0.000	0.000	0.000	-	0.014	0.208	0.000	0.000	0.318			
Sexually Transmitted Diseases	0.347	0.477	0.372	0.485	0.554	0.335	0.473	0.337	0.475	0.972	0.359	0.481	0.404	0.493	0.450			

Notes: This table presents the statistical description of selected pre-program variables after 6 years of the program. The first column of the table gives the variable description. Variables are divided into groups that share similar meanings. The remainder of the table consists of the description of the blocks of variables associated with the whole sample, the female sample and the male sample. Each block has 6 columns: (1) Control mean (C Mean), (2) Control standard deviation (C SD), (3) Treatment mean (T Mean), (4) Treatment standard deviation (T SD), and (5) Asymptotic p-value associated with the difference in means. Bold p-values indicate that the t-statistic between the control and the treatment means is significant at the 10% level.

E Additional Inference Results: Addressing Attrition using Inverse Propensity Weights

One aspect of the NFP that may cause concern is attrition. In order to address this we proceed as follows. We estimate by OLS a linear regression model which dependent variable is binary and equal to one if the mother represents an attrition case. We choose the model as to maximize the R^2 and incorporate pre-program variables with very few missing values. This permits us to establish the set of variables that provides the maximum amount of information when it comes to estimate the probability of attrition. Then, we predict the probability of attrition through a Logit model and apply an inverse probability weighting scheme to our estimations. The results do not change much after this correction. Tables E.4–10 show these results. The tables can be read in the same way as Tables 7–10 in the paper.

Table E.3: Using Logit to Obtain Probabilities

Sample		LR	Chi2	Prob. > Chi2	AIC	BIC
<i>Treatment Females</i>						
Year 12	x					
Year 9	x	x	x	x	x	x
Year 6	x	x	x	x	x	x
Year 4.5	x	x	x	x	x	x
Year 2	x	x	x	x	x	x
<i>Control Females</i>						
Year 12	x	x	x	x	x	x
Year 9	x	x	x	x	x	x
Year 6	x	x	x	x	x	x
Year 4.5	x	x	x	x	x	x
Year 2	x	x	x	x	x	x
<i>Treatment Males</i>						
Year 12	x	x	x	x	x	x
Year 9	x	x	x	x	x	x
Year 6	x	x	x	x	x	x
Year 4.5	x	x	x	x	x	x
Year 2	x	x	x	x	x	x
<i>Control Males</i>						
Year 12	x	x	x	x	x	x
Year 9	x	x	x	x	x	x
Year 6	x	x	x	x	x	x
Year 4.5	x	x	x	x	x	x
Year 2	x	x	x	x	x	x

Notes: The table describes the pre-program variables used to calculate the inverse probability weights. The first column provides the four division groups: treatment females, control females, treatment males, and control males. Additionally, there is a corresponding time period for each row. The next 23 columns represents the set of pre-program characteristics that were used for logit. An “ \times ” represents that that variable was used for the specific sample and time period. The column labeled “LR Chi2” is the chi-squared calculated using the logit regression and the next column, “Prob. > Chi2,” provides the corresponding p -values. The last two columns, AIC and BIC, provides the Akaike information criterion and Bayesian information criterion respectively.

Table E.4: Child Health Outcomes

Outcome Description	Females						Males					
	Basic Statistics			Block Perm. FL			Basic Statistics			Block Perm. FL		
	Cntr. Mean	Cd. Diff. Mn.	Cd. Eff. Size	Asy P-val	Single P-val	Stepdown	Cntr. Mean	Cd. Diff. Mn.	Cd. Eff. Size	Asy P-val	Single P-val	Stepdown
<i>Birth Outcomes for Child</i>												
Placenta Weight	683.488	-11.638	-0.073	0.707	0.467	0.717	662.401	27.965	0.157	0.112	0.014	0.036
Birth Weight	3050.505	-128.456	-0.235	0.966	0.903	0.903	2993.726	204.977	0.292	0.006	0.000	0.001
Head Circumference	33.257	0.038	0.023	0.425	0.203	0.459	33.506	0.327	0.146	0.107	0.060	0.060
Length	49.652	0.234	0.087	0.236	0.202	0.513	49.908	0.711	0.196	0.042	0.018	0.033
Gestational Age at Delivery	39.092	-0.545	-0.242	0.940	0.854	0.919	38.526	0.745	0.214	0.028	0.001	0.005
<i>Child Health Outcomes (Year 12)</i>												
Any Injuries since Last Interview	0.175	-0.043	-0.122	0.171	0.216	0.386	0.232	-0.059	-0.140	0.132	0.120	0.474
# Hospitalizations for Injuries since Last Interview	0.009	-0.011	-0.116	0.138	0.185	0.451	0.011	-0.013	-0.134	0.132	0.170	0.582
Total # Injuries since Last Interview	0.200	-0.068	-0.156	0.102	0.074	0.224	0.278	-0.057	-0.110	0.212	0.268	0.685
Hospitalized since Last Interview	0.059	-0.044	-0.226	0.033	0.035	0.140	0.040	0.054	0.299	0.975	0.890	0.890
Have Chronic Condition /Health Problem	0.203	-0.003	-0.009	0.473	0.639	0.639	0.360	0.077	0.163	0.885	0.849	0.905
Standardized Child BMI	1.090	-0.240	-0.277	0.019	0.012	0.060	0.778	0.224	0.257	0.968	0.833	0.988

Notes: The first column provides the outcome description. Our results are presented in six columns for each gender. The first column (Cntr. Mean) of each result set shows the mean for the control group. When factor scores were computed, we set the mean in the control group to zero. The second column (Cd. Diff. Mn.) gives the conditional difference in means between the treatment group and the control group. The third column (Cd. Eff. Size) calculates the conditional effect size for the respective group. The fourth column (Asy. P-val.) provides the asymptotic *p*-value for the one-sided single hypothesis test associated with the *t*-statistic for the difference in means between treatment and control groups. As mentioned in Section 2, the control group stands for the original treatment group 2 of the NFP experiment and the treatment group stands for the original group 4. The fifth column (Block Perm. FL/Single P-val.) presents the one-sided restricted permutation *p*-values for the single-hypothesis testing based on the *t*-statistic associated with the treatment indicator in the [Freedman and Lane \(1983\)](#) regression as described in Section 4. By restricted permutation we mean that permutations are done within strata defined by the baseline variables used in the randomization protocol: maternal age and race, gestational age at enrollment, employment status of the head of the household, and geographic region. The covariates used in the [Freedman and Lane \(1983\)](#) regression are: maternal height, household income, grandmother support, maternal parenting attitudes and mother currently in school. Finally, the last column (Block Perm. FL/Stepdown) provides *p*-values that account for multiple-hypothesis testing based on the Stepdown algorithm of [Romano and Wolf \(2005a\)](#). Blocks of outcomes that are tested jointly are separated by lines. The selection of blocks of outcomes is done on the basis of their meaning. Outcomes that share similar meaning are grouped together. Female maternal outcomes allude to mothers whose first child is a girl. Likewise, male maternal outcomes allude to mothers whose first child is a boy. The results in this table use an inverse probability weighting scheme to address attrition. The weights are based on the predicted probability to drop the sample. The prediction is based on a Logit model that is described at the beginning of this section.

Table E.5: Family Environment

	Outcome Description	Females						Males					
		Basic Statistics			Block Perm. FL			Basic Statistics			Block Perm. FL		
<i>Home Environment, Parenting (Year 1) - Factor Scores</i>		Cntr. Mean	Cd. Diff. Mn.	Cd. Eff. Size	Asy P-val	Single P-val	Stepdown	Cntr. Mean	Cd. Diff. Mn.	Cd. Eff. Size	Asy P-val	Single P-val	Stepdown
<i>Home Observation Measurement of the Environment (HOME)</i>	Home Observation Measurement of the Environment (HOME)	0.000	0.338	0.338	0.004	0.004	0.004	-0.005	0.154	0.154	0.114	0.079	0.079
	Non-Abusive Parenting Attitudes (Bavolek)	0.007	0.294	0.293	0.010	0.003	0.006	-0.002	0.364	0.364	0.002	0.001	0.002
<i>Home Environment, Parenting (Year 2)- Factor Scores</i>	Home Observation Measurement of the Environment (HOME)	0.001	0.298	0.297	0.010	0.004	0.007	-0.008	0.116	0.116	0.186	0.111	0.111
	Non-Abusive Parenting Attitudes (Bavolek)	0.012	0.374	0.372	0.003	0.005	0.005	-0.005	0.481	0.481	0.000	0.001	0.001
<i>Maternal Mental Health (Year 2)</i>													
Anxiety		-0.001	-0.226	-0.226	0.042	0.038	0.086	0.012	-0.052	-0.052	0.340	0.348	0.633
Depression		0.000	-0.115	-0.115	0.180	0.102	0.169	0.010	-0.011	-0.011	0.465	0.524	0.692
Positive Well-Being		-0.002	0.096	0.096	0.222	0.413	0.413	-0.006	-0.213	-0.214	0.950	0.947	0.947
Emotional Stability		0.001	0.185	0.185	0.076	0.056	0.113	-0.012	0.042	0.042	0.367	0.427	0.689
Overall Mental Health		0.000	0.193	0.193	0.066	0.066	0.122	-0.011	-0.047	-0.047	0.644	0.666	0.772
Self Esteem		0.011	0.283	0.283	0.014	0.003	0.014	-0.011	0.045	0.045	0.367	0.467	0.707
Mastery		0.009	0.251	0.250	0.030	0.018	0.057	-0.010	0.253	0.252	0.026	0.040	0.137
<i>Total Cost of Govt. Programs (Child_Ages 1 - 12 Years)</i>													
AFDC/TANF		2585.286	-177.226	-0.070	0.280	0.627	0.627	2557.084	-4264.34	-0.105	0.973	0.987	0.156
Food Stamp		2900.613	-374.602	-0.229	0.026	0.241	0.362	3191.672	-288.782	-0.187	0.061	0.118	0.155
Medicaid		3462.064	-367.166	-0.221	0.035	0.275	0.377	3747.045	-271.420	-0.183	0.068	0.153	0.153

Notes: The first column provides the outcome description. Our results are presented in six columns for each gender. The first column (Cntr. Mean) of each result set shows the mean for the control group. When factor scores were computed, we set the mean in the control group to zero. The second column (Cd. Diff. Mn.) gives the conditional difference in means between the treatment group and the control group. The third column (Cd. Eff. Size) calculates the conditional effect size for the respective group. The fourth column (Asy. P-val.) provides the asymptotic *p*-value for the one-sided single hypothesis test associated with the *t*-statistic for the difference in means between treatment and control groups. As mentioned in Section 2, the control group stands for the original treatment group 2 of the NFP experiment and the treatment group stands for the original group 4. The fifth column (Block Perm. FL/Single P-val.) presents the one-sided restricted permutation *p*-values for the single-hypothesis testing based on the *t*-statistic associated with the treatment indicator in the Freedman and Lane (1983) regression as described in Section 4. By restricted permutation we mean that permutations are done within strata defined by the baseline variables used in the randomization protocol: maternal age at enrollment, employment status of the head of the household, and geographic region. The covariates used in the Freedman and Lane (1983) regression are: maternal height, household income, grandmother support, maternal parenting attitudes and mother currently in school. Finally, the last column (Block Perm. FL/Stepdown) provides *p*-values that account for multiple-hypothesis testing based on the Stepdown algorithm of Romano and Wolf (2005a). Blocks of outcomes that are tested jointly are separated by lines. The selection of blocks of outcomes is done on the basis of their meaning. Outcomes that share similar meaning are grouped together. Female maternal outcomes allude to mothers whose first child is a girl. Likewise, male maternal outcomes allude to mothers whose first child is a boy. The results in this table use an inverse probability weighting scheme to address attrition. The weights are based on the predicted probability to drop the sample. The prediction is based on a Logit model that is described at the beginning of this section.

Table E.6: Cognitive Abilities and Achievement Outcomes

Outcome Description	Females						Males					
	Basic Statistics			Block Perm. FL			Basic Statistics			Block Perm. FL		
	Cnt. Mean	Cd. Diff. Mn.	Cd. Eff. Size	Asy P-val	Single P-val	Stepdown	Cnt. Mean	Cd. Diff. Mn.	Cd. Eff. Size	Asy P-val	Single P-val	Stepdown
<i>Kaufman Assessment Battery for Children (Year 6)</i>												
Gestalt Closure	9.026	0.244	0.081	0.266	0.193	0.487	9.787	-0.388	-0.134	0.837	0.636	0.636
Hand Movements	9.267	0.438	0.203	0.065	0.025	0.150	9.319	0.127	0.060	0.332	0.398	0.711
Matrix Analogies	8.636	0.136	0.080	0.273	0.300	0.579	8.480	0.285	0.180	0.092	0.124	0.434
Number Recall	9.390	0.437	0.152	0.120	0.086	0.327	8.886	1.004	0.421	0.002	0.004	0.029
Photo Series	7.040	0.424	0.212	0.055	0.064	0.284	6.791	0.030	0.014	0.458	0.496	0.700
Spatial Memory	8.441	0.204	0.084	0.264	0.341	0.516	8.568	0.218	0.090	0.258	0.194	0.531
Triangles	8.845	0.435	0.188	0.070	0.129	0.402	9.201	0.094	0.041	0.382	0.213	0.522
Word Order	9.737	-0.079	-0.030	0.591	0.386	9.148	0.763	0.298	0.016	0.006	0.039	
<i>Kaufman Assessment Battery for Children (Year 6)</i>												
Nonverbal	89.267	2.118	0.239	0.041	0.051	0.104	89.466	1.104	0.118	0.196	0.187	0.235
Sequential Processing	96.587	1.685	0.131	0.160	0.071	0.124	94.353	3.676	0.312	0.013	0.011	0.023
Simultaneous Processing	88.981	1.980	0.196	0.072	0.094	0.094	90.128	0.498	0.050	0.359	0.231	0.231
<i>WISC-III, PPVT-III for Children (Year 6)</i>												
Wechsler Intelligence Scale for Children (WISC-III)	96.518	0.900	0.050	0.348	0.352	0.352	90.692	1.746	0.102	0.227	0.298	0.298
Peabody Picture Vocabulary Test (PPVT-III)	83.682	1.685	0.154	0.119	0.164	0.286	82.695	2.325	0.221	0.062	0.013	0.024
<i>Child Cognition (Year 6) - Factor Scores</i>												
Cognition + achievement (KABC, PPVT, WISC)	0.005	0.118	0.118	0.188	0.067	0.092	-0.010	0.182	0.182	0.092	0.063	0.063
Cognitive skills (Mental Processing Composite-KABC)	0.000	0.137	0.137	0.150	0.073	0.073	-0.007	0.277	0.277	0.023	0.015	0.021
<i>Reading Achievement for the Child (Year 12)</i>												
Average Reading Grade (Grades 1 - 5)	2.694	0.076	0.101	0.228	0.107	0.271	2.348	0.058	0.078	0.296	0.100	0.164
TCAP % Language (School Years 1 - 5, Grd 3+)	51.600	0.372	0.016	0.456	0.180	0.307	37.918	5.076	0.233	0.067	0.005	0.021
TCAP % Reading (School Years 1 - 5, Grd 3+)	42.374	0.197	0.010	0.473	0.164	0.310	35.020	1.750	0.088	0.280	0.043	0.117
PIAT Total Reading (Derived Score)	90.420	0.662	0.069	0.307	0.344	0.404	89.350	1.381	0.103	0.221	0.063	0.129
PIAT Reading Comprehension (Derived Score)	88.458	-0.232	-0.026	0.576	0.546	0.546	87.641	2.369	0.203	0.072	0.022	0.070
PIAT Reading Recognition (Derived Score)	94.486	2.175	0.180	0.102	0.156	0.325	92.620	0.266	0.018	0.447	0.136	
<i>Math Achievement for the Child (Year 12)</i>												
Average Math Grade (Grades 1 - 5)	2.622	0.093	0.113	0.196	0.146	0.270	2.391	0.099	0.130	0.183	0.072	0.072
TCAP % Math (School Years 1 - 5, Grd 3+)	47.610	1.896	0.080	0.291	0.188	0.279	40.176	3.086	0.139	0.185	0.033	0.082
PIAT Mathematics (Derived Score)	87.413	-0.080	-0.008	0.525	0.727	0.727	86.538	1.947	0.193	0.086	0.048	0.085

Notes: The first column provides the outcome description. Our results are presented in six columns for each gender. The first column (Cnt. Mean) of each result set shows the mean for the control group. When factor scores were computed, we set the mean in the control group to zero. The second column (Cd. Diff. Mn.) gives the conditional difference in means between the treatment group and the control group. The third column (Cd. Size) calculates the conditional effect size for the respective group. The fourth column (Asy. P-val.) provides the asymptotic *p*-value for the one-sided single hypothesis test associated with the *t*-statistic for the difference in means between treatment and control groups. As mentioned in Section 2, the control group stands for the original treatment group 2 of the NFP experiment and the treatment group stands for the original group 4. The fifth column (Block Perm.). Freedman and Lane (1983) presents the one-sided restricted permutation *p*-values for the single-hypothesis testing based on the *t*-statistic associated with the treatment indicator in the Freedman and Lane (1983) regression as described in Section 4. By restricted permutation we mean that permutations are done within strata defined by the baseline variables used in the randomization protocol: maternal age and race, gestational age at enrollment, employment status of the head of the household, and geographic region. The covariates used in the Freedman and Lane (1983) regression are: maternal height, household income, grandmother support, maternal parenting attitudes and mother currently in school. Finally, the last column (Block Perm. FL/Stepdown) provides *p*-values that account for multiple-hypothesis testing based on the Stepdown algorithm of Romano and Wolf (2005a). Blocks of outcomes that are tested jointly are separated by lines. The selection of blocks of outcomes is done on the basis of their meaning. Outcomes that share similar meaning are grouped together. Female maternal outcomes allude to mothers whose first child is a girl. Likewise, male maternal outcomes allude to mothers whose first child is a boy. The results in this table use an inverse probability weighting scheme to address attrition. The weights are based on the predicted probability to drop the sample. The prediction is based on a Logit model that is described at the beginning of this section.

Table E.7: Socio- Emotional Abilities

Outcome Description	Females						Males					
	Basic Statistics			Block Perm. FL			Basic Statistics			Block Perm. FL		
	Crit. Mean	Cd. Diff. Mn.	Cd. Eff. Size	Asy P-val	Single P-val	Stepdown	Crit. Mean	Cd. Diff. Mn.	Cd. Eff. Size	Asy P-val	Single P-val	Stepdown
<i>Child Behavior Checklist (Year 2) - Factor Scores</i>												
Affective Problems	-0.001	-0.337	-0.002	0.003	0.015		0.004	0.287	0.287	0.985	0.955	0.955
Anxiety Problems	-0.002	-0.181	0.066	0.249	0.007		0.016	0.016	0.016	0.550	0.636	0.907
Pervasiveness Developmental Problems	-0.005	-0.261	0.013	0.060	0.100		0.005	0.185	0.185	0.925	0.817	0.950
Attention Deficit Hyperactivity Disorder	-0.001	-0.243	0.025	0.019	0.060		0.003	0.056	0.056	0.670	0.706	0.923
Oppositional Defiant Problems	-0.001	-0.217	0.040	0.053	0.120		0.005	0.126	0.126	0.853	0.880	0.962
<i>Child Behavior Checklist (Year 6) - Factor Scores</i>												
Affective Problems	-0.010	-0.007	-0.007	0.479	0.612	0.796	-0.004	-0.103	-0.103	0.203	0.151	0.481
Anxiety Problems	-0.008	-0.061	-0.061	0.306	0.492	0.759	0.009	0.083	0.082	0.729	0.813	0.813
Somatic Problems	-0.003	0.130	0.130	0.832	0.884	0.884	0.007	0.063	0.063	0.678	0.442	0.757
Attention Deficit Hyperactivity Problems	-0.012	-0.230	0.035	0.096	0.307	-0.006	-0.040	-0.040	-0.040	0.379	0.310	0.713
Oppositional Defiant Problems	0.000	-0.027	-0.027	0.415	0.286	0.608	-0.013	-0.083	-0.083	0.270	0.317	0.672
Conduct Problems	-0.002	-0.267	-0.266	0.013	0.003	0.015	-0.009	-0.011	-0.011	0.467	0.485	0.605
<i>MacArthur Story Stem Battery (MSSB) (Year 6) - Factor Scores</i>												
Dysregulated Aggression	-0.006	-0.027	-0.027	0.413	0.135	0.269	-0.009	-0.130	-0.130	0.189	0.137	0.496
Warmth and Empathy	-0.011	0.388	0.002	0.005	0.019	-0.011	-0.099	-0.099	-0.099	0.770	0.535	0.832
Emotional Integration	-0.005	-0.028	-0.028	0.585	0.765	0.765	-0.015	0.055	0.055	0.349	0.429	0.849
Performance Anxiety	0.010	-0.038	-0.038	0.373	0.093	0.259	-0.009	0.077	0.077	0.701	0.843	0.843
Aggression	-0.005	-0.164	-0.164	0.084	0.003	0.012	-0.010	-0.095	-0.095	0.260	0.177	0.570
<i>Internalizing, Externalizing, Absences (Year 12)</i>												
Internalizing Disorders	0.240	-0.028	-0.066	0.309	0.453	0.813	0.397	-0.087	-0.183	0.090	0.082	0.154
Externalizing Disorders	0.183	-0.013	-0.032	0.402	0.641	0.866	0.183	0.089	0.239	0.951	0.859	0.859
Average # of Absences (School Years 1 - 5)	10.144	0.263	0.035	0.605	0.666	0.666	11.548	-1.838	-1.838	-0.246	0.029	0.027

Notes: The first column provides the outcome description. Our results are presented in six columns for each gender. The first column (Cntr. Mean) of each result set shows the mean for the control group. When factor scores were computed, we set the mean in the control group to zero. The second column (Cd. Diff. Mn.) gives the conditional difference in means between the treatment group and the control group. The third column (Cd. Eff. Size) calculates the conditional effect size for the respective group. The fourth column (Asy. P-val.) provides the asymptotic p -value for the one-sided single hypothesis test associated with the t -statistic for the difference in means between treatment and control groups. As mentioned in Section 2, the control group stands for the original treatment group 2 of the NFP experiment and the treatment group stands for the original group 4. The fifth column (FL/Single P-val.) presents the one-sided restricted permutation p -values for the single-hypothesis testing based on the t -statistic associated with the treatment indicator in the [Freedman and Lane \(1983\)](#) regression as described in Section 4. By restricted permutation we mean that permutations are done within strata defined by the baseline variables used in the randomization protocol: maternal age and race, gestational age at enrollment, employment status of the head of the household, and geographic region. The covariates used in the [Freedman and Lane \(1983\)](#) regression are: maternal height, household income, grandmother support, maternal parenting attitudes and mother currently in school. Finally, the last column (Block Perm. FL/Stepdown) provides p -values that account for multiple-hypothesis testing based on the Stepdown algorithm of [Romano and Wolf \(2005a\)](#). Blocks of outcomes that are tested jointly are separated by lines. The selection of blocks of outcomes is done on the basis of their meaning. Outcomes that share similar meaning are grouped together. Female maternal outcomes allude to mothers whose first child is a girl. Likewise, male maternal outcomes allude to mothers whose first child is a boy. The results in this table use an inverse probability weighting scheme to address attrition. The weights are based on the predicted probability to drop the sample. The prediction is based on a Logit model that is described at the beginning of this section.

F Theoretical Framework for Mediation Analysis

This section develops a theoretical framework that helps to interpret the estimates of a standard mediation model for early childhood interventions. Our model is based on a technology of skill formation according to (Cunha and Heckman, 2007b). In it, later skills build on previous ones to generate human capital. Notationally, let $\boldsymbol{\theta}_{i,t}$ be the vector of skills during childhood for individual i at period t and $t \in \{0, 1, \dots, T\}$, where T is the number of periods of childhood. Let $\mathbf{I}_{i,t}$ represent investments at the same period. We use X_i for family background characteristics and $v_{i,t}$ for an exogenous error term independent of $\boldsymbol{\theta}_{i,t}, \mathbf{I}_{i,t}$ and X_i . The structural equation that governs the evolution of skills is given by:

$$\boldsymbol{\theta}_{i,t+1} = q_{t+1}(\boldsymbol{\theta}_{i,t}, \mathbf{I}_{i,t+1}, X_i, v_{i,t+1}); t \in \{0, 1, \dots, T-1\}. \quad (32)$$

By structural equation, we mean autonomous functions in the language of Frisch (1938), i.e. deterministic functions whose functional form do not change as its arguments vary. We also allow for skills to affect investments, that is:

$$\mathbf{I}_{i,t+1} = h_{t+1}(\boldsymbol{\theta}_{i,t}, X_i, \varepsilon_{i,t+1}); t \in \{0, 1, \dots, T-1\}, \quad (33)$$

where $\varepsilon_{i,t+1}$ is an exogenous error term independent of $\boldsymbol{\theta}_{i,t}$ and X_i . Our model is completed by the following structural outcome equation at period T :

$$Y_i = g_T(\boldsymbol{\theta}_{i,T}, X_i, \xi_{i,T}). \quad (34)$$

where $\xi_{i,T}$ is an exogenous error term independent of $\boldsymbol{\theta}_{i,T}$ and X_i .

We can use a recursive substitution of investments and skills of Equations (32)–(33) into (34) to generate the following equation:

$$Y_i = f_{t'}(\boldsymbol{\theta}_{i,t'}, X_i, \{v_{i,\tilde{t}}\}_{\tilde{t}=t'}^T, \{\varepsilon_{i,\tilde{t}}\}_{\tilde{t}=t'}^T, \xi_{i,T}), \quad (35)$$

where $\{v_{i,\tilde{t}}\}_{\tilde{t}=t'}^T = \{v_{i,t'}, v_{i,t'+1}, \dots, v_{i,T}\}$ and $\{\varepsilon_{i,\tilde{t}}\}_{\tilde{t}=t'}^T = \{\varepsilon_{i,t'}, \varepsilon_{i,t'+1}, \dots, \varepsilon_{i,T}\}$.

Suppose that an intervention occurs at period t' where $t' \in \{1, \dots, T\}$. Let $D_i \in \{0, 1\}$ be the treatment indicator of this intervention which takes value 1 if participant i is treated and 0 otherwise. The intervention enters our technology of skill formation model as a form of skill investment. Thus we append the investment Equation (33) at period t' by:

$$\mathbf{I}_{i,t'} = h_{t'}(\boldsymbol{\theta}_{i,t'-1}, D_i, X_i, \varepsilon_{i,t'}); \text{ for some } t' \in \{0, 1, \dots, T-1\}, \quad (36)$$

The counterfactual values investment $\mathbf{I}_{i,t'}$ are defined by the value $\mathbf{I}_{i,t'}$ takes when the intervention D_i is fixed at a level $d \in \{0, 1\}$. By fixing, I mean the causal operation defined in Haavelmo (1944) where D_i is set to $d \in \{0, 1\}$ as argument in the structural equation (36). That is:

$$\mathbf{I}_{i,t',d} = h_{t'}(\boldsymbol{\theta}_{i,t'-1}, d, X_i, \varepsilon_{i,t'}); d \in \{0, 1\} \text{ for some } t' \in \{0, 1, \dots, T-1\}. \quad (37)$$

Let the counterfactual skills be defined in a symmetric fashion by:

$$\boldsymbol{\theta}_{i,t',d} = q_{t'}(\boldsymbol{\theta}_{i,t'-1}, \mathbf{I}_{i,t',d}, X_i, v_{i,t'}). \quad (38)$$

We also define the counterfactual skills and investments for periods $t > t'$ by:

$$\begin{aligned} \mathbf{I}_{i,t+1,d} &= h_{t+1}(\boldsymbol{\theta}_{i,t,d}, X_i, \varepsilon_{i,t+1}), \text{ and} \\ \boldsymbol{\theta}_{i,t+1,d} &= q_{t+1}(\boldsymbol{\theta}_{i,t,d}, \mathbf{I}_{i,t+1,d}, X_i, v_{i,t+1}); t > t'. \end{aligned}$$

We can also define the counterfactual outcomes by:

$$Y_{i,d} = f_{t'}(\boldsymbol{\theta}_{i,t',d}, X_i, \{\epsilon_{i,\tilde{t}}\}_{\tilde{t}=t'}^T, \{\varepsilon_{i,\tilde{t}}\}_{\tilde{t}=t'}^T, \xi_{i,T}), \quad (38)$$

If the intervention assignment uses the method of randomization, then we have that:

$$(Y_{i,d}, \boldsymbol{\theta}_{i,t',d}) \perp\!\!\!\perp D_i | X_i; d \in \{0, 1\}.$$

We can also write the realized values of skills and outcomes as:

$$\begin{aligned} Y_i &= Y_{i,1}D_i + Y_{i,0}(1 - D_i), \text{ and} \\ \boldsymbol{\theta}_{i,t} &= \boldsymbol{\theta}_{i,t,1}D_i + \boldsymbol{\theta}_{i,t,0}(1 - D_i); t \geq t'. \end{aligned}$$

We now cast on Equation (38) to generate a tractable equation to examine mediation effects. Note that Equation (38) holds ont onlt for t' but for any $t \geq t'$.

$$Y_{i,d} = f_t(\boldsymbol{\theta}_{i,t,d}, X_i, \{v_{i,\tilde{t}}\}_{\tilde{t}=t}^T, \{\varepsilon_{i,\tilde{t}}\}_{\tilde{t}=t}^T, \xi_{i,T}), \text{ for any } t \in \{t', t'+1, \dots, T\}. \quad (39)$$

Error terms $(\{v_{i,\tilde{t}}\}_{\tilde{t}=t}^T, \{\varepsilon_{i,\tilde{t}}\}_{\tilde{t}=t}^T, \xi_{i,T})$ are independent of $\boldsymbol{\theta}_{i,t,d}$ and X_i . For sake of notational simplicity, we

can substitute those error terms by ζ_t without loss of generality. Equation (39) then becomes:

$$Y_{i,d} = f_t(\boldsymbol{\theta}_{i,t,d}, X_i, \zeta_{i,t}). \quad (40)$$

We achieve a linear form of Equation (40) by approximating it through a Maclaurin expansion. This generates the following equation:

$$Y_{i,d} = \kappa_t + \boldsymbol{\alpha}_{t,d}\boldsymbol{\theta}_{i,t,d} + \boldsymbol{\beta}_{t,d}X_i + \epsilon_{i,t,d}, \quad d \in \{0, 1\}. \quad (41)$$

where $\epsilon_{i,t,d}$ accounts for the approximation error. Equations (40)–(41) are used in our mediation analysis in Section 5.

G Mediation Methodology

G.1 Three Step Procedure

This part of the appendix explains in detail the three step procedure that we use in order to decompose the NFP treatment effects. As highlighted in the paper, we perform two sets of analysis. First, we study if the treatment effects on child skills at age 6 were mediated by program enhancement of birth weight, parenting attitudes and investments, and maternal socio-emotional skills at age 2. Second, we study if the program impact on outcomes at age 12 was mediated by the NFP enhancement of skills at age 6. The results from these analysis shed light on the complementarity of investments and skills in explaining the NFP treatment effects.

Step One The idea is to develop a measurement system that links the observed items and the latent skills. In order to do that, we assume that our measurements are dedicated. This means that each observed measurement is linked to a unique skill. Specifically, let \mathcal{M}^j be the index set of measures associated with trait j , where $j \in \mathcal{J} = \{P, C, SE\}$. P, C, SE denote, respectively, parenting skills, child cognitive skills, and child socio-emotional abilities.¹⁸ Thus, our linear measurement system looks as follows:¹⁹

$$M_{m^j,d}^j = \nu_{m^j}^j + \varphi_{m^j}^j \theta_d^j + \eta_{m^j,d}^j, \quad (42)$$

where $\nu_{m^j}^j$ is the intercept term and $\varphi_{m^j}^j$ represents the loading factor of trait j . We cannot reject the null hypothesis that the intercepts and loading factors depend on treatment status. $\eta_{m^j,d}^j$ is a mean zero

¹⁸This follows the same notation as Heckman et al. (2013)

¹⁹We control for pre-program variables X but we keep it implicit to shorten notation.

idiosyncratic error term which, by assumption, is independent of $\theta_d^j \forall j \in \mathcal{J}$. We normalize the loading factor associated with the first measure of each factor to 1 to set a scale, otherwise the scale is arbitrary.²⁰ Finally, we allow for factor correlation.

The parameters that identify the measurement system are the factor means, the factor covariances, the intercepts, the factor loadings, and the variances of the error terms: $E[\theta^j(d)] = \mu_d^j$, $Var[\theta_d] = \Sigma_{\theta_d}$, $\nu_{m^j}^j$, $\varphi_{m^j}^j$, $Var[\eta_{m^j}^j]$). Heckman et al. (2013) show that the existence of at least three measures for each latent skill guarantees identification.²¹ Broadly, means, variances, and covariances across the measures identify the parameters of the system.

We estimate the parameters of the measurement system that links skills with measures both at ages 2 and 6. Variables become potential mediators if we estimate an effect of the NFP on it, so that they are potential meaningful channels. For age 2, non-abusive parenting attitudes are approximated by the Adult-Adolescent Parenting Inventory (Bavolek), which comprises 32 items, and home investments are measured by the Bradley and Caldwell Home Observation for measurement of the Environment (HOME) inventory, which is composed by 45 items.

The maternal skills selected correspond to anxiety, assessed by the Rand Mental Health Inventory, self-esteem, measured by the Rosenberg scale, and mastery, approximated by the Pearlin scale. Similarly, for age 6, we select as plausible mediators children's skills influenced by the NFP. Children cognition is measured by 8 subtests from the K-ABC mental processing composite. For children's socio-emotional skills, we identify as potential mediators the treatment reduction in conduct, attention and aggression problems, as well as the enhancement of children's pro-social skills. Attention and conduct problems are approximated by items from the Child Behavior Checklist. Pro-social skills (warmth or empathy) and aggression problems are approximated by items from the MacArthur Story Stem Battery. Section B of the Appendix explains in more detail these tests, as well as the instruments they use.

We estimate the parameters of the measurement system by maximum likelihood. In order to do this, we assume that the latent skills and the error terms, $\theta^j, \eta_{m^j}^j$, are normal and i.i.d. We use full-information maximum likelihood to deal with the missing values in the measures for some individuals. Recent work by citation shows that FIML yields unbiased estimates that are more efficient than ad hoc methods like list-wise and pair-wise deletion, which work under the implicit assumption of random missing data.²²

For the case of the measurement system at age 2, we have 146 items. Although it is ideal to estimate the complete set of items (skills) jointly, it is not feasible. Thus, we estimate them in two blocks: one for

²⁰Given that the first measure sets the scale, we choose it to be the most correlated with the skill. The results are robust to alterations of this.

²¹ Carneiro et al. (2003) and Cunha et al. (2010) also discuss identification of factor models.

²²Missing at random means that the probability of missing data in a variable x can depend on other observed variables but not on the values of x itself

parenting and home investments and other for maternal characteristics. This allows us to account for the correlation between the skills that are in the same block. For the case of the measurement system at age 6, the set of items is smaller and we do a joint estimation.

Step Two In the second step we use the parameter estimates from the first step to construct factor scores for each children. The objective of this is to construct approximations for the latent skills. The two most common linear scoring methods are the regression method (Bartlett, 1937; Thomson, 1934) and the Bartlett method, which resembles GLS. We use the Bartlett (1937) method because it estimates unbiased approximations of the unobserved skills. Actually, this guarantees that the difference in means between the factor scores for children in the treatment and the control groups equals the difference in means in the true scores. The derivation of the Bartlett estimator begins with the measurement system summarized as:

$$\underbrace{\mathbf{M}_i}_{|\mathcal{M}| \times 1} = \underbrace{\boldsymbol{\varphi}}_{|\mathcal{M}| \times |\mathcal{J}|} \underbrace{\boldsymbol{\theta}_i}_{|\mathcal{J}| \times 1} + \underbrace{\boldsymbol{\eta}_i}_{|\mathcal{M}| \times 1}$$

where the dimension of each term is below the braces (recall that \mathcal{J} and \mathcal{M} are the indexing sets for skills and measures respectively). Assume that the $(\boldsymbol{\theta}_i, \boldsymbol{\eta}_i)$, $i \in \{1, \dots, I\}$, are independent across i . For simplicity, we assume that they are i.i.d.²³ Let $Cov(\mathbf{M}_i, \mathbf{M}_i) = \boldsymbol{\Sigma}$, $Cov(\boldsymbol{\theta}_i, \boldsymbol{\theta}_i) = \boldsymbol{\Phi}$ and $Cov(\boldsymbol{\eta}_i, \boldsymbol{\eta}_i) = \boldsymbol{\Omega}$. The linear relation between the factor scores and the measures is the following:

$$\boldsymbol{\theta}_{S,i} = \mathbf{L}' \mathbf{M}_i \tag{43}$$

In order to obtain unbiased estimates, Barlett imposes the restriction that $\mathbf{L}' \boldsymbol{\varphi} = \mathbf{I}_{|\mathcal{J}|}$. The Bartlett estimator for the vector of approximated skills $(\boldsymbol{\theta}_i)$ is:

$$\boldsymbol{\theta}_{S,i} = (\hat{\boldsymbol{\varphi}}' \hat{\boldsymbol{\Omega}}^{-1} \hat{\boldsymbol{\varphi}})^{-1} \hat{\boldsymbol{\varphi}}' \hat{\boldsymbol{\Omega}}^{-1} \mathbf{M}_i, \tag{44}$$

where the matrix of loading factors, $\hat{\boldsymbol{\varphi}}$, and $\hat{\boldsymbol{\Omega}} = Cov(\boldsymbol{\eta}_i, \boldsymbol{\eta}_i)$ are both estimated in the first step. Bartlett's estimator is a Generalized Least Squares, *GLS*, procedure where measures are used as dependent variables and loading factors are treated as regressors. By the Gauss-Markov theorem, the Bartlett *GLS* estimator is optimal and hence leads to the best linear unbiased predictor (BLUE).

There are individuals that have missing data in some of the items that compose the measurement system. In order to take advantage of the information that they have (instead of list-wise delete them), we predict factor scores for them. We use the covariance between the measures and the factors from the sample with

²³This is not strictly required but simplifies the notation.

complete measurement system to predict scores for these people. Additionally, for the cases where individuals are missing a factor score because they did not have any item in that measurement system, we impute factor scores with the regression method.²⁴ This procedure recovers around 10% of the randomized sample.

Step 3 In this step, we use factor scores as approximations of the true skills to estimate the models that link the later outcomes with the intermediate skills. The factor scores are measured with error, which produces downward biased estimates of the parameters of the outcome equations. This bias corresponds to the traditional attenuation that results from classical measurement error. In factor scored regressions, Bolck et al. (2008) prove this. We adopt the bias correction strategy proposed by Croon (2002). In summary, this approach takes advantage of the fact that we have estimates of all the components of the bias. This strategy, also used by Heckman et al. (2013), can be summarized as follows:

Consider the model following model. To simplify notation, we use W to denote pre-program variables X , treatment indicator and the intercept of equation 8:

$$Y_i = \alpha\theta_i + \gamma W_i + \epsilon_i, \quad i = 1, \dots, N. \quad (45)$$

The covariance matrix of (θ_i, W_i) is

$$\begin{pmatrix} Cov(\theta, \theta) & Cov(\theta, W) \\ Cov(W, \theta) & Cov(W, W) \end{pmatrix}.$$

We measure θ_i with error. Thus,

$$\theta_{S,i} = \theta_i + V_i, \quad i = 1, \dots, N$$

$$(W_i, \theta_i) \perp\!\!\!\perp V_i, \quad E(V_i) = 0, \quad Cov(V, V) = \Sigma_V V$$

Denote $Cov(\theta_{S,i}, \theta_{S,i}) = \Sigma_{\theta_S, \theta_S}$. We assume that the $(\theta_i, W_i, \epsilon_i)$ are i.i.d, but much weaker conditions suffice. Note that we do not assume that $\theta_i \perp\!\!\!\perp W_i$ as in traditional factor analysis. We do assume that $(\theta_i, W_i) \perp\!\!\!\perp \epsilon_i$ and $E(\epsilon_i) = 0$.

If we use $\theta_{S,i}$ in place of Y_i , it follows that:

$$Y_i = \alpha\theta_{S,i} + \gamma W_i + \epsilon_i - \alpha V_i. \quad (46)$$

²⁴We impute factor scores for individuals that have at least two other factor scores.

The estimation of equation 46 using OLS produces estimates that are biased:

$$plim \begin{pmatrix} \hat{\alpha} \\ \hat{\gamma} \end{pmatrix} = \begin{pmatrix} Cov(\boldsymbol{\theta}_S, \boldsymbol{\theta}_S) & Cov(\boldsymbol{\theta}_S, \mathbf{W}) \\ Cov(\mathbf{W}, \boldsymbol{\theta}_S) & Cov(\mathbf{W}, \mathbf{W}) \end{pmatrix}^{-1} \begin{pmatrix} Cov(\boldsymbol{\theta}, \boldsymbol{\theta}) & Cov(\boldsymbol{\theta}, \mathbf{W}) \\ Cov(\mathbf{W}, \boldsymbol{\theta}) & Cov(\mathbf{W}, \mathbf{W}) \end{pmatrix} \begin{pmatrix} \alpha \\ \gamma \end{pmatrix}.$$

Let $\Sigma_{\mathbf{B}, \mathbf{C}}$ be $Cov(\mathbf{B}, \mathbf{C})$. Observe that $\Sigma_{\boldsymbol{\theta}, \mathbf{W}} = \Sigma_{\boldsymbol{\theta}_S, \mathbf{W}}$ as a consequence of our assumptions. In this notation

$$plim \begin{pmatrix} \hat{\alpha} \\ \hat{\gamma} \end{pmatrix} = \underbrace{\begin{pmatrix} \Sigma_{\boldsymbol{\theta}, \boldsymbol{\theta}} + \Sigma_{\mathbf{V}, \mathbf{V}} & \Sigma_{\boldsymbol{\theta}, \mathbf{W}} \\ \Sigma_{\mathbf{W}, \boldsymbol{\theta}} & \Sigma_{\mathbf{W}, \mathbf{W}} \end{pmatrix}^{-1} \begin{pmatrix} \Sigma_{\boldsymbol{\theta}, \boldsymbol{\theta}} & \Sigma_{\boldsymbol{\theta}, \mathbf{W}} \\ \Sigma_{\mathbf{W}, \boldsymbol{\theta}} & \Sigma_{\mathbf{W}, \mathbf{W}} \end{pmatrix}}_{\mathbf{A}} \begin{pmatrix} \alpha \\ \gamma \end{pmatrix} \quad (47)$$

which is the usual attenuation formula.

From the estimation of the measurement system, we can identify $\Sigma_{\boldsymbol{\theta}, \boldsymbol{\theta}}$, $\Sigma_{\boldsymbol{\theta}, \mathbf{W}}$, $\Sigma_{\mathbf{V}, \mathbf{V}}$, and we have all the components of \mathbf{A} . Hence if we pre-multiply the least squares estimator by \mathbf{A}^{-1} , we obtain:

$$plim \mathbf{A}^{-1} \begin{pmatrix} \hat{\alpha} \\ \hat{\gamma} \end{pmatrix} = \begin{pmatrix} \alpha \\ \gamma \end{pmatrix}.$$

This is called ‘‘Croon’s method’’ in psychometrics (Croon, 2002). In our application, there are two groups corresponding to $D = 0$ and $D = 1$ (control and treatment, respectively). We allow $\boldsymbol{\theta}_i$ to vary by treatment status. Indeed, our method assumes that treatment only operates through shifting the distribution of $\boldsymbol{\theta}$. We do not normalize the means of $\boldsymbol{\theta}$ (or \mathbf{W}) to be zero.

In the third step of our estimation procedure we compute bootstrapped p-values for each decomposition channel of the treatment effects. We take 100,000 resamples with replacement. The bootstrapped p-value for the null hypothesis $H_0 : \alpha_j = 0$ is calculated as follows:

$$p\text{-value} = \frac{1}{B} \sum_{b=1}^B 1(t_b^{j,*} > t^j) \text{ with } t^j = \frac{\hat{\alpha}^j}{\hat{\sigma}(\hat{\alpha}^j)} \text{ and } t_b^{j,*} = \frac{(\hat{\alpha}_b^j - \hat{\alpha}^j)}{\hat{\sigma}(\hat{\alpha}_b^j)} \quad (48)$$

where $\hat{\alpha}_b^j$ is bootstrapped estimated in the b^{th} resample and $\hat{\alpha}^j$ is estimated from the original data. Given the estimates of the outcome equation and of the factor scores, we construct the bootstrapped p-value for the contribution of skill k under the null hypothesis $H_0 : \hat{\alpha}^j E(\theta_1^j - \theta_0^j) = 0$ as follows:

$$p\text{-value} = \frac{1}{B} \sum_{b=1}^B 1(T_b^{j,*} > T^j) \text{ with } T^j = \frac{\hat{\alpha}^j * E(\widehat{\theta^j(1) - \theta^j(0)})}{\hat{\sigma}(\hat{\alpha}^j * E(\widehat{\theta^j(1) - \theta^j(0)}))} \quad (49)$$

where $T_b^{j,*}$ is the statistic T^j computed with the parameters obtained in the b^{th} resample. Notice that the p-value combines the variation in two population parameters: 1) the coefficient of the outcome equation; 2) the experimentally induced difference in means in the skills. It could be the case that each of these parameters are, separately, statistically significant. However, the p-value may increase due to a loss in power when they are combined.

Tables G.8 - G.11 shows the parameters of the outcome equations as wells as the decompositions components.

Table G.8: Female Decomposition (Year 6)

Outcome Coefficients	Treatment Coefficient	Birth Weight Coefficient	Home y2 Coefficient	Parenting y2 Coefficient	Anxiety y2 Coefficient	Self-Esteem y2 Coefficient	Mastery y2 Coefficient	Sample Size	
								p-value	p-value
<i>Treatment Effect</i>									
Cognitive	0.04	0.391	0.08	0.089	0.23	0.035	0.06	0.139	0.21
Attention Problems	-0.15	0.083	-0.11	0.013	-0.11	0.169	-0.07	0.042	-0.14
Conduct Problems	-0.15	0.036	-0.09	0.018	-0.07	0.249	-0.03	0.192	-0.18
Warmth/Empathy	0.18	0.060	0.05	0.192	0.29	0.003	0.09	0.014	-0.01
Aggression	-0.13	0.103	-0.04	0.218	-0.15	0.107	-0.01	0.416	0.13
<i>Treatment Effect Fraction</i>									
Cognitive	0.29	0.391	-0.01	0.110	0.04	0.032	0.02	0.079	0.03
Attention Problems	-0.15	0.083	0.01	0.099	-0.02	0.144	-0.02	0.046	-0.02
Conduct Problems	-0.15	0.036	0.01	0.112	-0.01	0.223	-0.01	0.170	-0.03
Warmth/Empathy	0.18	0.060	-0.01	0.169	0.05	0.007	0.03	0.018	-0.00
Aggression	-0.13	0.103	0.00	0.173	-0.03	0.090	-0.00	0.401	0.02

Notes: The first column provides the outcome description and the top row provides information on the mediators. For Year 6, the mediators are treatment, birth weight, home environment, parenting, anxiety, self-esteem and mastery. The last column provides the sample size for the mediators. The rows are divided into 3 groups: Outcome Coefficients, Treatment Effect and Treatment Effect Fraction. The last of these groups is also shown visually in Figure 3. Each mediator has two subcolumns of information: the coefficient and the p-value. Bold p-values are significant at the 10% level. We used the following controls: maternal race, maternal age, gestational age, household density, region, employment status of household head, grandmother support, randomization wave, income category, mother currently in school, and maternal parenting attitudes.

Table G.9: Male Decomposition (Year 6)

	Treatment		Birth Weight		Home y2		Parenting y2		Anxiety y2		Self-Esteem y2		Mastery y2		Sample Size
	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value	
<i>Outcome Coefficients</i>															
Cognitive	0.08	0.240	0.08	0.093	0.35	0.004	0.11	0.014	0.06	0.327	-0.04	0.447	0.02	0.464	305
Aggression	-0.08	0.186	-0.02	0.331	0.07	0.241	-0.05	0.091	-0.23	0.014	0.37	0.058	-0.11	0.310	305
<i>Treatment Effect</i>															
Cognitive	0.08	0.240	0.02	0.064	0.04	0.054	0.02	0.047	0.00	0.281	-0.00	0.362	0.00	0.422	305
Aggression	-0.08	0.186	-0.01	0.296	0.01	0.165	-0.01	0.091	-0.01	0.252	0.02	0.173	-0.02	0.230	305
<i>Treatment Effect Fraction</i>															
Cognitive	0.50	0.240	0.14	0.064	0.22	0.054	0.11	0.047	0.02	0.281	-0.02	0.362	0.02	0.422	305
Aggression	0.84	0.186	0.05	0.296	-0.07	0.165	0.08	0.091	0.12	0.252	-0.23	0.173	0.20	0.230	305

Notes: The first column provides the outcome description and the top row provides information on the mediators. For Year 6, the mediators are treatment, birth weight, home environment, parenting, anxiety, self-esteem and mastery. The last column provides the sample size for the corresponding outcome in the first column. The rows are divided into 3 groups: Outcome Coefficients, Treatment Effect and Treatment Effect Fraction. The last of these groups is also shown visually in Figure 4. Each mediator has two subcolumns of information: the coefficient and the p-value. Bold p-values are significant at the 10% level. We used the following controls: maternal race, maternal age, household density, region, employment status of household head, grandmother support, randomization wave, income category, mother currently in school, and maternal parenting attitudes.

Table G.10: Female Decomposition (Year 12)

Outcome Coefficients	Treatment		Cognition		Attention Problems		Conduct Problems		Warmth/Empathy		Aggression		Sample Size
	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value	
Total # Days Child Used Marijuana	-0.15	0.050	-0.12	0.086	0.03	0.573	0.00	0.515	0.12	0.158	0.04	0.192	271
Child Used Alcohol, Marijuana, or Tobacco in Last 30 Days	-0.02	0.198	-0.02	0.048	0.00	0.0467	0.02	0.358	-0.00	0.477	0.00	0.457	268
Standardized Child BMI (Year 12)	-0.30	0.016	-0.11	0.100	-0.22	0.115	0.537	0.030	0.08	0.206	-0.11	0.197	272
<i>Treatment Effect</i>													
Child Ever Used Marijuana	-0.15	0.060	-0.01	0.218	-0.00	0.318	-0.00	0.484	0.04	0.111	-0.01	0.155	271
Child Used Alcohol, Marijuana, or Tobacco in Last 30 Days	-0.02	0.198	-0.00	0.217	-0.00	0.431	-0.00	0.273	-0.00	0.469	-0.00	0.424	268
Standardized Child BMI (Year 12)	-0.30	0.016	-0.01	0.209	0.03	0.109	-0.05	0.060	0.02	0.162	0.02	0.145	272
<i>Treatment Effect Fraction</i>													
Child Ever Used Marijuana	1.12	0.050	0.05	0.218	0.03	0.318	0.00	0.484	-0.26	0.111	0.06	0.155	271
Child Used Alcohol, Marijuana, or Tobacco in Last 30 Days	0.83	0.198	0.05	0.217	0.02	0.431	0.07	0.273	0.01	0.469	0.01	0.424	268
Standardized Child BMI (Year 12)	1.06	0.016	0.02	0.209	-0.11	0.109	0.19	0.060	-0.08	0.162	-0.08	0.145	272

Notes: The first column provides the outcome description and the top row provides information on the mediators. For Year 12, the mediators are treatment, cognition, attention problems, Conduct Problems, Warmth/Empathy and Aggression. The last column provides the sample size for the corresponding outcome in the first column. The rows are divided into 3 groups: Outcome Coefficients, Treatment Effect and Treatment Effect Fraction. The last of these groups is also shown visually in Figure 7. Each mediator has two subcolumns of information: the coefficient and the p-value. Bolded p-values are significant at the 10% level. Bolded coefficients are significant at the 10% level. We used the following controls: maternal race, maternal age, maternal height, gestational age, household density, region, employment status of household head, grandmother support, randomization wave, income category, mother currently in school, and maternal parenting attitudes.

Table G.11: Male Decomposition (Year 12)

	Treatment	Cognition	Attention problems	Conduct Problems	Warmth/Empathy	Aggression	Sample Size	
	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value	Coefficient	p-value
<i>Outcome Coefficients</i>								
Average TCAP percentile, y1-5; language composite	2.88	0.188	11.93	0.000	2.21	0.379	-0.94	0.442
PIAT reading comprehension derived score	1.69	0.134	7.44	0.000	-1.41	0.326	0.45	0.480
Average math grade, years 1-5	0.03	0.368	0.50	0.000	-0.21	0.145	0.22	0.137
Average math grade, Years 1-5 after KG	-0.00	0.538	0.50	0.000	-0.15	0.205	0.16	0.198
average top percentile y1-5; math	0.81	0.348	15.29	0.000	5.32	0.231	-2.86	0.336
PIAT math derived score	1.64	0.106	7.86	0.000	-1.36	0.324	0.20	0.515
SC ever tried smoking; 1=yes	-0.05	0.079	0.02	0.254	0.04	0.279	0.02	0.341
SC use alc, mar, tob last 30 days	-0.05	0.04	-0.00	0.40	-0.01	0.41	0.04	0.25
Internalizing disorders - Youth report	-0.05	0.213	-0.07	0.047	0.02	0.421	0.03	0.406
Anxious/depressed - clinical or borderline disorder, youth report	-0.05	0.082	-0.05	0.016	-0.05	0.167	0.06	0.101
Average number of absences, school years 1-5	-1.05	0.146	-2.25	0.001	4.36	0.010	-3.87	0.22
<i>Treatment Effect</i>								
Average TCAP percentile, y1-5; language composite	2.88	0.188	2.09	0.064	-0.02	0.432	0.03	0.361
PIAT reading comprehension derived score	1.69	0.134	1.44	0.041	0.11	0.255	-0.03	0.364
Average math grade, years 1-5	0.03	0.368	0.08	0.080	-0.00	0.366	0.00	0.449
Average math grade, Years 1-5 after KG	-0.00	0.538	0.08	0.061	0.00	0.451	-0.00	0.335
average top percentile y1-5; math	0.81	0.348	2.68	0.070	-0.09	0.367	0.09	0.313
PIAT math derived score	1.64	0.106	1.55	0.042	0.11	0.242	-0.01	0.420
SC ever tried smoking; 1=yes	-0.05	0.079	0.00	0.198	-0.00	0.234	-0.00	0.169
SC use alc, mar, tob last 30 days	-0.05	0.043	-0.00	0.342	0.00	0.328	-0.00	0.334
Internalizing disorders - Youth report	-0.05	0.213	-0.01	0.058	-0.00	0.342	-0.00	0.262
Anxious/depressed - clinical or borderline disorder, youth report	-0.05	0.082	-0.01	0.028	0.00	0.213	-0.00	0.303
Average number of absences, school years 1-5	-1.05	0.146	-0.36	0.063	-0.27	0.258	0.07	0.424
<i>Treatment Effect Fraction</i>								
Average TCAP percentile, y1-5; language composite	0.57	0.188	0.41	0.064	-0.00	0.432	0.01	0.361
PIAT reading comprehension derived score	0.54	0.134	0.46	0.041	0.03	0.255	-0.01	0.364
Average math grade, Years 1-5 after KG	0.23	0.368	0.68	0.080	-0.03	0.366	0.01	0.449
average top percentile y1-5; math	0.20	0.348	0.66	0.070	-0.02	0.367	0.02	0.313
PIAT math derived score	0.54	0.106	0.51	0.042	0.04	0.242	-0.00	0.420
SC use alc, mar, tob last 30 days	0.92	0.043	0.02	0.342	-0.02	0.328	0.04	0.262
Internalizing disorders - Youth report	0.63	0.213	0.17	0.058	0.01	0.342	0.02	0.303
Anxious/depressed - clinical or borderline disorder, youth report	0.71	0.082	0.14	0.028	-0.05	0.213	0.05	0.219
Average number of absences, school years 1-5	0.70	0.146	0.24	0.063	0.18	0.258	-0.05	0.424

Notes: The first column provides the outcome description and the top row provides information on the mediators. For Year 12, the mediators are treatment, cognition, attention problems, Conduct Problems, Warmth/Empathy and Aggression. The last column provides the sample size for the corresponding outcome in the first column. The rows are divided into 3 groups: Outcome Coefficients, Treatment Effect and Treatment Effect Fraction. The last of these groups is also show visually in Figures 5 - 6. Each mediator has two subcolumns of information: the coefficient and the p-value. Bold p-values are significant at the 10% level. We used the following controls: maternal race, maternal age, maternal height, gestational age, household density, region, employment status of household head, grandmother support, randomization wave, income category, mother currently in school, and maternal parenting attitudes.

H Mediation Specification Test

In this section we specify how do we empirically test the effect that the mediators have on the final outcomes. We use \mathcal{J} for an indexing set of skills. We use $\mathcal{J}_p \subseteq \mathcal{J}$ for the subset of measured skills. Our model for the outcome equation is:

$$Y_d = \kappa_d + \sum_{j \in \mathcal{J}} \alpha_d^j \theta_d^j + \beta_d \mathbf{X} + \tilde{\epsilon}_d, \quad d \in \{0, 1\},$$

where κ_d is an intercept, $(\alpha_d^j; j \in \mathcal{J})$ are loading factors and β_d are $|\mathbf{X}|$ -dimensional vectors of parameters. The error term $\tilde{\epsilon}_d$ is a zero-mean i.i.d. random variable assumed to be independent of regressors $(\theta_d^j; j \in \mathcal{J})$ and \mathbf{X} .

The NFP analysts collected a rich array of measures of cognitive and personality skills. However, it is likely that there are skills that they did not measure. As noted before, we use $\mathcal{J}_p \subseteq \mathcal{J}$ be the index set of measured skills. Namely, skills for which we have enough psychological instruments that allows for estimation. We rewrite the equation for potential outcome Y_d as:

$$\begin{aligned} Y_d &= \kappa_d + \sum_{j \in \mathcal{J}} \alpha_d^j \theta_d^j + \beta_d \mathbf{X} + \tilde{\epsilon}_d \\ &= \underbrace{\kappa_d + \sum_{j \in \mathcal{J}_p} \alpha_d^j \theta_d^j}_{\text{skills that we measure}} + \underbrace{\sum_{j \in \mathcal{J} \setminus \mathcal{J}_p} \alpha_d^j \theta_d^j}_{\text{skills that we do not measure}} + \beta_d \mathbf{X} + \tilde{\epsilon}_d \\ &= \underbrace{\kappa_d + \sum_{j \in \mathcal{J} \setminus \mathcal{J}_p} \alpha_d^j E(\theta_d^j)}_{\text{new intercept}} + \underbrace{\sum_{j \in \mathcal{J}_p} \alpha_d^j \theta_d^j}_{\text{skills that we measure}} + \underbrace{\sum_{j \in \mathcal{J} \setminus \mathcal{J}_p} \alpha_d^j (\theta_d^j - E(\theta_d^j))}_{\text{skills that we do not measure}} + \beta_d \mathbf{X} + \tilde{\epsilon}_d, \\ &= \underbrace{\tau_d}_{\text{new intercept}} + \underbrace{\sum_{j \in \mathcal{J}_p} \alpha_d^j \theta_d^j}_{\text{skills that we measure}} + \underbrace{\sum_{j \in \mathcal{J} \setminus \mathcal{J}_p} \alpha_d^j (\theta_d^j - E(\theta_d^j))}_{\text{new error term}} + \tilde{\epsilon}_d \end{aligned} \tag{50}$$

where $d \in \{0, 1\}$, $\tau_d = \kappa_d + \sum_{j \in \mathcal{J} \setminus \mathcal{J}_p} \alpha_d^j E(\theta_d^j)$. Any differences in the error terms between treatment and control groups can be attributed to differences in unmeasured skills. Thus, we assume, without loss of generality, that $\tilde{\epsilon}_1 \stackrel{d}{=} \tilde{\epsilon}_0$, where $\stackrel{d}{=}$ means equality in distribution.

The goal of this section is to examine the statistical assumptions needed to estimate unbiased parameters $(\alpha_d^j : j \in \mathcal{J}_p, d \in \{0, 1\})$. These parameters are used to perform the decomposition of outcome treatment effects into parts associated with skills enhancement $(\theta_1^j - \theta_0^j : j \in \mathcal{J}_p)$. Parameters α may suffer from confounding effects if measured and unmeasured skills are not independent. We can solve this confounding

problem by assuming that unmeasured skills are independent of measures skills. Namely,

$$(\theta_d^j; j \in \mathcal{J} \setminus \mathcal{J}_p) \perp\!\!\!\perp (\theta_d^j; j \in \mathcal{J}_p) | \mathbf{X}; d \in \{0, 1\},$$

then the regression:

$$Y_d = \tau_d + \sum_{j \in \mathcal{J}_p} \alpha_d^j \theta_d^j + \beta_d \mathbf{X} + \epsilon_d, \quad (51)$$

produces unbiased estimates of parameter $(\alpha_d^j; j \in \mathcal{J}_p); d \in \{0, 1\}$. Indeed error terms ϵ_d in equation (51) are given by

$$\epsilon_d = \tilde{\epsilon}_d + \sum_{j \in \mathcal{J} \setminus \mathcal{J}_p} \alpha_d^j (\theta_d^j - E(\theta_d^j))$$

which are independent of $(\theta_d^j; j \in \mathcal{J}_p)$ conditional on \mathbf{X} under the assumption that skills are independent.

Now suppose that instead of the skills independence assumption for both groups, we focus only on the control group, thus,

$$(\theta_0^j; j \in \mathcal{J} \setminus \mathcal{J}_p) \perp\!\!\!\perp (\theta_0^j; j \in \mathcal{J}_p) | \mathbf{X}.$$

Moreover, suppose we also assume that $\alpha_1^j = \alpha_0^j; j \in \mathcal{J}$. Equivalently, the outcome loading factors for both treatment and control groups are the same. In this new setup, the regression

$$Y_0 = \tau_0 + \sum_{j \in \mathcal{J}_p} \alpha^j \theta_0^j + \beta_0 \mathbf{X} + \epsilon_0, \quad (52)$$

also produces unbised estimates of $(\alpha^j; j \in \mathcal{J}_p)$. Now consider the regression

$$Y_1 = \tau_1 + \sum_{j \in \mathcal{J}_p} \alpha^j \theta_1^j + \beta_1 \mathbf{X} + \epsilon_1.$$

According to our rationale, this regression only produces unbiased estimates of $(\alpha^j; j \in \mathcal{J}_p)$ if:

$$(\theta_1^j; j \in \mathcal{J} \setminus \mathcal{J}_p) \perp\!\!\!\perp (\theta_1^j; j \in \mathcal{J}_p) | \mathbf{X}, \quad (53)$$

or, alternatively,

$$(\theta_1^j - \theta_0^j; j \in \mathcal{J} \setminus \mathcal{J}_p) \perp\!\!\!\perp (\theta_1^j - \theta_0^j; j \in \mathcal{J}_p) | \mathbf{X}. \quad (54)$$

Thus, under this new set of assumptions, testing $H_0 : \boldsymbol{\alpha}_1 = \boldsymbol{\alpha}_0$ is translated into testing the independence relations of equations (53)–(54).

While the skill independence assumption in equation (53) may appear strong, the rich settlement of

information on NFP surveys makes this assumption more plausible. NFP data has a huge selection of psychological questionnaires that aims to measure both cognitive and non-cognitive skills through childhood. We examine all the available data and only a subset of these measures turns out to be statistically relevant for mediation analysis. We use these measures to estimate factors that are able to explain the majority of the treatment effects. Thus, it seems unlikely that some unobserved skills overlooked by psychologists could have a major impact on mediating treatment effects.

H.1 Skills and the Measurement System

The assumption that the loading factors in the measurement system (equation 42) are the same for treatment and control is not necessary to identify the model. It is useful for clarity in the interpretation because the treatment operates by the shift of the latent skills and not by the map between measures and skills.

Ultimately, we need the decomposition of the treatment effects, (12), to be invariant to the choice of the measurement system we used. Thus, for each skill's contribution to treatment effect on each outcome, we want to test the null hypothesis that:

$$H_0 : \boldsymbol{\alpha}_0(E(\boldsymbol{\theta}_1 - \boldsymbol{\theta}_0)) = \boldsymbol{\alpha}_1(E(\boldsymbol{\theta}_1 - \boldsymbol{\theta}_0)) \quad (55)$$

where $\boldsymbol{\alpha}_d = (\alpha_d^j : j \in \mathcal{J}_p)$ and $\boldsymbol{\theta}_d = (\theta_d^j : j \in \mathcal{J}_p)$ such that $d \in \{0, 1\}$ denotes treatment status.

Let $\hat{\boldsymbol{\theta}}_i$ be the estimated factor score for individual i , assigned to treatment status $D_i \in \{0, 1\}$, using the estimated loading factors from the subsample of individuals with the same treatment status, i.e. for each individual factor score:

$$\hat{\boldsymbol{\theta}}_i = (\boldsymbol{\varphi}_{D_i}'(\boldsymbol{\Omega}_{D_i})^{-1} \boldsymbol{\varphi}_{D_i})^{-1} \boldsymbol{\varphi}_{D_i}'(\boldsymbol{\Omega}_{D_i})^{-1} M_i.$$

We would like to test if the contributions to the treatment effects is independent if we use the parameters' from different measurement system (i.e if we estimate a different set of loading factors for the treatment and control group).

Hence, an appropriate single hypothesis test statistic for each skill $j \in \mathcal{J}_p$ becomes:

$$\hat{\alpha}_0^j(\hat{\theta}_1^j - \hat{\theta}_0^j) - \hat{\alpha}_1^j(\hat{\theta}_1^j - \hat{\theta}_0^j)$$

where we use a hat subscript to denote estimated parameters. $\hat{\alpha}$ are Croon corrected estimates of α . We can use a summary statistic to test the joint hypothesis stated in (55).

Independence between $\hat{\alpha}_d$ and $\hat{\theta}_d - \hat{\theta}_0$ yields:

$$\text{Var}(\hat{\alpha}_d(\hat{\theta}_1 - \hat{\theta}_0)) = (\hat{\alpha}_d)^2 \text{Var}(\hat{\theta}_1 - \hat{\theta}_0) + \text{Var}(\hat{\alpha}_d)(\hat{\theta}_1 - \hat{\theta}_0)^2 + \text{Var}(\hat{\alpha}) \text{Var}(\hat{\theta}_1 - \hat{\theta}_0)$$

Independence between the quantities estimated for each of the d 's yields:

$$\text{Var}(\hat{\alpha}_0(\hat{\theta}_1 - \hat{\theta}_0) - \hat{\alpha}^1(\hat{\theta}_1 - \hat{\theta}_0)) = \text{Var}(\hat{\alpha}_0(\hat{\theta}_1 - \hat{\theta}_0)) + \text{Var}(\hat{\alpha}_1(\bar{\hat{\theta}}_1 - \bar{\hat{\theta}}_0))$$

This variance helps us to get the z -statistic:

$$z = \frac{\hat{\alpha}_0(\hat{\theta}_1 - \hat{\theta}_0) - \hat{\alpha}_1(\hat{\theta}_1 - \hat{\theta}_0)}{\sqrt{\text{Var}(\hat{\alpha}_0(\hat{\theta}_1 - \hat{\theta}_0) - \hat{\alpha}^1(\hat{\theta}_1 - \hat{\theta}_0))}}$$

A two-sided z -test gives a p -value associated with the skill and outcome null hypothesis of invariance to the choice of the measurement system.

These (outcome, skill) paired p -values are shown in Tables [H.12](#) and [H.13](#). We find that we can not reject the null hypothesis for any skill-outcome pair which suggests that our decompositions of the NFP treatment effects are not driven by the choice of the measurement system.

H.1.1 Additional Specification Test for the Outcome Equation

In order to clearly interpret the channels through which the NFP affects later outcomes, (5) assumes that the parameters that map skills and pre-program variables with the outcomes are not affected by the programs. Put another way, the mediated channels operate exclusively on the program effect on the skills. This assumption is not necessary to identify the model.

For each outcome decomposed, we test the hypothesis that $\alpha_1^j = \alpha_0^j, \forall j \in \mathcal{J}$ and $\beta_1 = \beta_0$ with a Wald test. Tables [H.14](#) and [H.15](#) show the results of this test. We cannot reject the null hypothesis of equality of the coefficients for the treatment and control groups. This evidence strengthens the validity of our interpretation of the decomposition of the NFP treatment effect into interpretable channels.

I Oaxaca-Blinder Decomposition Results

Oaxaca-Blinder decompositions are often used to examine sources of treatment effects. This method decomposes the difference in means between two groups (treatment and control) into the part that is due to the group differences in the channels and into the part that is due to group differences in the parameters that capture the relationship between the channels and the outcomes. In our context, the Oaxaca-Blinder

decomposition is summarized as follows:²⁵

$$\underbrace{E(Y|D=1) - E(Y|D=0)}_{\text{Treatment Effects}} = \underbrace{(\alpha_1 - \alpha_0)\theta_0}_{\text{Differences unexplained by the skills}} + \underbrace{(\theta_1 - \theta_0)\alpha}_{\text{Explained: differences in skills}}. \quad (56)$$

The decomposition that we propose summarizes the unexplained part in the above equation through the difference in the intercepts between the treatment and the control groups. In order to assess if our decomposition is a plausible specification, we estimate an Oaxaca-Blinder decomposition. The results in Tables I.16 - I.20 evidence that the Oaxaca-Blinder unexplained part that accounts for differences in the mapping of the skills on outcomes is not statistically significant for any outcome. Therefore, the results from the decomposition of the NFP treatment effects presented in the paper seem to be correctly specified.

²⁵We implicitly control for pre-program variables.

Table H.12: Specification Test - Invariance of the Contribution of Skills to the Choice of the Measurement System (Females)

Factor Testing Results - Females						
Age 6 outcomes	Home	Parenting	Anxiety	Esteem	Mastery	Maternal skills- age 2
Cognition	0.263	0.907	0.859	0.698	0.672	
Attention problems	0.363	0.709	0.702	0.667	0.748	
Conduct problems	0.421	0.694	0.922	0.721	0.677	
Warmth-empathy (pro-social skills)	0.267	0.907	0.644	0.833	0.973	
Aggression Problems	0.692	0.819	0.862	0.821	0.786	

Children's skills, Age 6						
Age 12 outcomes	Cognition	Attention	Conduct	Probs	Empathy	Aggression
SC # days ever used marijuana	0.867	0.878	0.592	0.885	0.280	
SC use alc, mar, tob last 30 days	0.876	0.695	0.907	0.893	0.812	
Standardized Child BMI	0.889	0.822	0.574	0.953	0.324	

Notes: The table shows p-values for the Wald test: $z = \frac{\hat{\alpha}^0(\hat{\theta}_1^0 - \hat{\theta}_0^0) - \hat{\alpha}^1(\hat{\theta}_1^1 - \hat{\theta}_0^1)}{\sqrt{\text{Var}(\hat{\alpha}^0(\hat{\theta}_1^0 - \hat{\theta}_0^0) - \hat{\alpha}^1(\hat{\theta}_1^1 - \hat{\theta}_0^1))}}$

Table H.13: Specification Test - Invariance of the Contribution of Skills to the Choice of the Measurement System (Males)

Age 6 outcomes	Maternal skills- age 2			Children's skills. Age 6		
	Home	Parenting	anxiety	esteem	mastery	conduct
Cognition	0.349	0.394	0.971	0.927	0.946	
Aggression Problems	0.928	0.959	0.950	0.843	0.537	
Age 12 outcomes	Cognition	probs	Attention	conduct	Empathy	Aggression
Average TCAP percentile. Years 1-5 after KG: Language PIAT reading comprehension derived score	0.529	0.975	0.993	0.636	0.882	
Average math grades. Years 1-5 after KG	0.420	0.794	0.941	0.867	0.812	
Average TCAP percentile. Years 1-5 after KG: Math PIAT mathematics derived score SC use of alc, mar, tob. Lat 30 days	0.425	0.953	0.830	0.871	0.792	
Internalizing disorders - youth report Clinical or borderline anxious/depressed disorder Average number of absences, school years 1-5 after KG	0.571	0.940	0.951	0.940	0.875	
	0.433	0.503	0.817	0.976	0.652	
	0.845	0.970	0.751	0.791	0.538	
	0.582	0.934	0.911	0.905	0.509	
	0.537	0.936	0.771	0.916	0.687	
	0.379	0.908	0.706	0.833	0.735	

Notes: The table shows p-values for the Wald test: $z = \frac{\hat{\alpha}^0(\hat{\theta}_1^0 - \tilde{\theta}_0^0) - \hat{\alpha}^1(\hat{\theta}_1^1 - \tilde{\theta}_0^1)}{\sqrt{\text{Var}(\hat{\alpha}^0(\hat{\theta}_1^0 - \tilde{\theta}_0^0) - \hat{\alpha}^1(\hat{\theta}_1^1 - \tilde{\theta}_0^1))}}$

Table H.14: Specification Test - Outcome Equation (Females)

Outcome <i>6 Years</i>	Test Stat P-Val		
	Cognition	0.982	0.490
Attention prob.	1.753	0.018	
Conduct Prob.	0.846	0.675	
Pro-social	1.264	0.189	
Aggression	0.558	0.955	
<i>12 Years</i>			
	SC use alc, mar, tob last 30 days	1.266	0.189
	SC # days use of alc, mar, tob last 30 days	1.271	0.186
	Standardized Child BMI (Year 12)	1.172	0.270

Notes: The table shows p-values for Wald tests for the equality of slopes between treatment and control group in the outcome equation.

Table H.15: Specification Test - Outcome Equation (Males)

Outcome 6 Years	Test Stat P-Val		
	Cognition	0.609	0.926
<i>12 Years</i>			
average tcap percentile, y1-5: language composite	1.162	0.283	
PIAT reading comprehension derived score	1.286	0.175	
Average math grade grades 1-5	1.655	0.034	
Average math grade. Years 1-5 after KG	1.493	0.073	
average tcap percentile y1-5: math	1.242	0.213	
PIAT math derived score	1.102	0.343	
SC use alc, mar, tob last 30 days	1.208	0.237	
Internalizing disorders - Youth report	0.993	0.477	
Anxious/depressed - clinical or borderline disorder	0.682	0.867	
Average number of absences, school years 1-5	0.798	0.738	

Notes: The table shows p-values for Wald tests for the equality of slopes between treatment and control group in the outcome equation.

Table I.16: Oaxaca-Blinder Decomposition, outcomes at age 6 (Females)

	Cognition			Attention Problems			Conduct Problems			Warmth/Empathy			Aggression			
	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	
<i>Overall</i>																
	TotalDiff. in Means	0.114	0.112	0.311	-	-0.189	0.092	0.039	-	-0.197	0.072	0.006	-	0.235	0.102	0.021
	Explained	0.083	0.041	0.044	0.706	-0.080	0.037	0.033	0.271	-0.051	0.030	0.086	0.213	0.069	0.035	0.050
	Unexplained	0.031	0.112	0.784	0.294	-0.110	0.093	0.237	0.729	-0.146	0.072	0.045	0.787	0.166	0.099	0.093
<i>Explained Portion</i>																
	Home Index	0.032	0.020	0.113	0.355	-0.016	0.015	0.279	0.096	-0.010	0.013	0.420	0.063	0.034	0.019	0.071
	Parenting Index	0.028	0.026	0.284	0.137	-0.048	0.024	0.046	0.093	-0.018	0.018	0.314	0.046	0.040	0.023	0.074
	Maternal Anxiety Index	0.024	0.020	0.217	0.254	-0.018	0.016	0.271	0.100	-0.019	0.014	0.181	0.137	0.006	0.014	0.671
82	Maternal Self-Esteem Index	0.007	0.021	0.751	0.238	0.009	0.020	0.642	-0.204	-0.032	0.022	0.145	0.187	-0.043	0.028	0.122
	Maternal Mastery Index	0.002	0.021	0.913	-0.192	-0.019	0.023	0.409	0.256	0.017	0.019	0.375	-0.157	0.039	0.028	0.158
	Birthweight	-0.011	0.012	0.393	-0.086	0.012	0.013	0.353	-0.070	0.011	0.012	0.361	-0.063	-0.006	0.009	0.481
<i>Unexplained Portion</i>																
	Home Index	0.008	0.024	0.746	0.068	-0.004	0.018	0.842	0.019	0.000	0.014	0.994	0.001	0.028	0.023	0.222
	Parenting Index	0.020	0.028	0.461	0.179	0.033	0.022	0.130	-0.176	-0.001	0.016	0.965	0.004	0.007	0.021	0.741
	Maternal Anxiety Index	-0.017	0.021	0.434	-0.145	0.034	0.024	0.161	-0.181	0.032	0.020	0.111	-0.161	-0.007	0.017	0.696
	Maternal Self-Esteem Index	-0.009	0.029	0.757	-0.080	0.041	0.029	0.164	-0.216	0.022	0.022	0.306	-0.113	-0.018	0.035	0.599
	Maternal Mastery Index	0.017	0.034	0.628	0.147	-0.046	0.036	0.200	0.244	-0.038	0.026	0.148	0.193	0.018	0.037	0.625
	Birthweight	-0.002	0.007	0.719	-0.022	0.000	0.003	0.915	-0.002	0.002	0.006	0.695	-0.011	-0.002	0.007	0.758
	Residual	0.014	0.117	0.904	0.124	-0.169	0.094	0.074	0.891	-0.163	0.074	0.028	0.828	0.140	0.099	0.156

Notes: The indices are means of the non-missing items. The fractions are proportions of the total conditional difference in means.

Table I.17: Oaxaca-Blinder Decomposition, outcomes at age 6 (Males)

	Cognition			Attention Problems			Conduct Problems			Warmth/Empathy			Aggression				
	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction		
	0.173	0.105	0.100	-0.025	0.095	0.797	-0.012	0.088	0.891	-0.080	0.104	0.442	-0.099	0.086	0.250	-	
83	TotalDiff. in Means	0.092	0.037	0.012	0.496	-0.064	0.033	0.051	-5.856	-0.056	0.035	0.111	-1.130	0.022	0.025	-0.254	-0.025
	Explained	0.081	0.101	0.422	0.504	0.039	0.092	0.670	6.856	0.044	0.090	0.628	2.130	-0.102	0.105	0.332	0.322
	Unexplained	0.081	0.101	0.422	0.504	0.039	0.092	0.670	6.856	0.044	0.090	0.628	2.130	-0.102	0.105	0.332	0.383
	<i>Explained Portion</i>																
	Home Index	0.021	0.022	0.344	0.220	-0.003	0.006	0.627	-0.303	-0.009	0.010	0.395	-0.395	0.006	0.009	0.513	-0.161
	Parenting Index	0.044	0.022	0.042	0.112	-0.021	0.019	0.258	-0.479	-0.011	0.018	0.540	-0.041	0.008	0.017	0.640	-0.007
	Maternal Anxiety Index	0.001	0.004	0.847	0.019	-0.007	0.012	0.561	-0.544	-0.008	0.014	0.546	-0.297	0.003	0.007	0.629	-0.046
	Maternal Self-Esteem Index	-0.005	0.009	0.607	-0.016	0.005	0.010	0.592	1.536	-0.011	0.015	0.490	-0.514	-0.003	0.009	0.690	0.034
	Maternal Mastery Index	0.009	0.018	0.598	0.021	-0.015	0.018	0.385	-3.978	-0.001	0.014	0.964	0.553	0.004	0.018	0.831	-0.020
	Birthweight	0.022	0.017	0.192	0.140	-0.023	0.018	0.214	-2.089	-0.016	0.015	0.283	-0.435	0.004	0.014	0.747	-0.054
	<i>Unexplained Portion</i>																
	Home Index	0.002	0.011	0.834	0.013	-0.003	0.009	0.763	0.111	0.002	0.009	0.846	-0.152	0.008	0.012	0.529	-0.096
	Parenting Index	-0.007	0.024	0.760	-0.043	0.012	0.024	0.627	-0.471	0.016	0.022	0.467	-1.314	0.010	0.027	0.698	-0.129
	Maternal Anxiety Index	0.006	0.012	0.622	0.035	0.000	0.006	0.945	0.016	-0.005	0.011	0.625	0.451	0.003	0.009	0.708	-0.042
	Maternal Self-Esteem Index	0.004	0.010	0.665	0.024	-0.002	0.008	0.771	0.091	0.004	0.010	0.688	-0.321	0.005	0.010	0.642	-0.059
	Maternal Mastery Index	-0.033	0.028	0.241	-0.192	-0.007	0.026	0.780	0.294	0.020	0.023	0.396	-1.627	-0.023	0.029	0.421	0.288
	Birthweight	0.020	0.024	0.418	0.113	-0.060	0.028	0.034	2.422	-0.065	0.028	0.022	5.335	-0.015	0.024	0.525	0.191
	Residual	0.090	0.107	0.400	0.519	0.100	0.093	0.284	-4.061	0.072	0.098	0.462	-5.970	-0.090	0.116	0.436	1.121
	<i>Notes:</i> The indices are means of the non-missing items. The fractions are proportions of the total conditional difference in means.																

Table I.18: Oaxaca-Blinder Decomposition, outcomes at age 12 (Females)

SC # days ever used marijuana			SC use alc, mar, tob last 30 days			Standardized Child BMI (12Y)		
	Effect	SE	P-Val	Fraction	Effect	SE	P-Val	Fraction
Total Diff. in Means	-0.141	0.085	0.098	-	-0.021	0.020	0.281	-
Explained	0.026	0.038	0.488	-0.184	-0.005	0.007	0.460	0.242
Unexplained	-0.167	0.111	0.133	1.184	-0.016	0.021	0.429	0.758

<i>Explained</i>								
Cognitive	-0.006	0.018	0.723	0.046	-0.001	0.003	0.708	0.058
Attention Problems	0.000	0.013	0.991	0.001	-0.001	0.005	0.827	0.051
Conduct Problems	-0.003	0.010	0.775	0.019	-0.003	0.004	0.468	0.149
Warmth/Empathy	0.038	0.038	0.318	-0.268	0.000	0.004	0.934	-0.015
Aggression	-0.003	0.005	0.644	0.018	0.000	0.002	0.988	-0.001

<i>Unexplained</i>								
Cognitive	0.012	0.018	0.523	-0.084	0.003	0.004	0.496	-0.135
Attention Problems	0.002	0.015	0.889	-0.015	0.008	0.007	0.288	-0.364
Conduct Problems	0.013	0.018	0.482	-0.091	-0.008	0.012	0.522	0.364
Warmth/Empathy	-0.029	0.032	0.374	0.202	-0.005	0.004	0.254	0.228
Aggression	-0.002	0.009	0.803	0.016	-0.001	0.003	0.697	0.062
Residual	-0.163	0.096	0.089	1.155	-0.013	0.027	0.629	0.603

Notes: The indices are means of the non-missing items. The fractions are proportions of the total conditional difference in means.

Table I.19: Oaxaca-Blinder outcomes at age 12, Decomposition Part 1 (Males)

language composite												PLAT math derived score												
			derived score			Average math grade 1-5			after KG			average tcap percentile 1-5; math												
			Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	Effect	SE	P-Val Fraction	
Total Diff. in Means	4.403	3.289	0.181	-	2.022	1.584	0.202	0.117	0.107	0.275	-	0.083	0.103	0.422	-	2.818	3.429	0.411	-	2.447	1.324	0.065	-	
Explained	1.564	1.520	0.304	0.355	0.941	0.808	0.244	0.466	0.077	0.063	0.219	0.660	0.067	0.058	0.242	0.814	2.226	1.820	0.221	0.790	0.946	0.817	0.247	0.387
Unexplained	2.839	3.105	0.361	0.645	1.080	1.454	0.457	0.534	0.040	0.090	0.658	0.340	0.015	0.087	0.860	0.186	0.592	3.111	0.849	0.210	1.501	1.103	0.174	0.613
<i>Explained</i>																								
Cognitive	1.831	1.337	0.171	0.416	0.910	0.705	0.197	0.450	0.057	0.054	0.285	0.492	0.057	0.051	0.266	0.682	2.146	1.664	0.197	0.762	0.939	0.750	0.211	0.384
Attention Problems	0.075	0.275	0.787	0.017	0.060	0.131	0.647	0.030	0.009	0.016	0.570	0.080	0.007	0.012	0.548	0.087	0.057	0.312	0.855	-0.020	0.067	0.123	0.589	0.027
Conduct Problems	-0.003	0.273	0.992	-0.001	0.037	0.122	0.765	0.018	0.000	0.010	0.964	-0.004	-0.001	0.008	0.933	-0.008	0.020	0.281	0.945	0.007	0.035	0.110	0.751	0.014
Warmth/Empathy	-0.535	0.468	0.253	-0.122	-0.079	0.156	0.611	-0.039	-0.009	0.013	0.475	-0.079	-0.012	0.014	0.362	-0.149	-0.063	0.385	0.870	-0.022	-0.004	0.122	0.441	-0.038
Aggression	0.197	0.419	0.639	0.045	0.014	0.161	0.930	0.007	0.020	0.018	0.267	0.171	0.017	0.017	0.328	0.203	0.181	0.439	0.681	0.064	-0.001	0.142	0.995	0.000
<i>Unexplained</i>																								
Cognitive	0.540	0.980	0.582	0.123	-0.015	0.288	0.958	-0.007	0.005	0.019	0.787	0.045	0.009	0.019	0.652	0.105	0.563	0.780	0.470	0.200	-0.016	0.228	0.943	-0.007
Attention Problems	0.699	0.769	0.363	0.159	0.449	0.342	0.189	0.222	0.009	0.020	0.659	0.077	0.006	0.020	0.752	0.075	0.518	0.663	0.435	0.184	-0.162	0.292	0.579	-0.066
Conduct Problems	0.003	0.427	0.995	0.001	-0.092	0.242	0.705	-0.045	-0.003	0.016	0.858	-0.024	-0.003	0.015	0.864	-0.031	0.002	0.402	0.995	0.001	0.004	0.183	0.983	0.002
Warmth/Empathy	0.373	0.691	0.590	0.085	0.134	0.271	0.622	0.066	0.011	0.020	0.588	0.092	0.012	0.021	0.559	0.150	-0.076	0.650	0.907	-0.027	0.070	0.222	0.752	0.029
Aggression	-0.078	0.495	0.875	-0.018	-0.071	0.270	0.793	-0.035	-0.006	0.017	0.740	-0.049	-0.001	0.013	0.933	-0.014	-0.266	0.614	0.664	-0.094	-0.168	0.231	0.468	-0.069
Residual	1.302	3.447	0.706	0.296	0.675	1.617	0.676	0.334	0.023	0.090	0.796	0.200	-0.008	0.089	0.927	-0.099	-0.150	3.289	0.964	-0.053	1.773	1.191	0.137	0.724

Notes: The indices are means of the non-missing items. The fractions are proportions of the total conditional difference in means.

Table I.20: Oaxaca-Blinder outcomes at age 12, Decomposition Part 2 (Males)

	SC ever tried smoking: 1=yes			SC use alc, mar, tob last 30 days			Internalizing disorders - Youth			Anxious/depressed - clinical or			Average number of absences,			
	Effect	SE	P-Val	Fraction	Effect	SE	P-Val	Fraction	Effect	SE	P-Val	Fraction	Effect	SE	P-Val	Fraction
Total Diff. in Means	-0.063	0.034	0.065	-	-0.034	0.025	0.176	-	-0.068	0.063	0.281	-	-0.053	0.030	0.081	-
Explained	-0.005	0.010	0.644	0.076	-0.003	0.010	0.741	0.099	-0.030	0.022	0.163	0.445	-0.014	0.012	0.248	0.262
Unexplained	-0.058	0.036	0.103	0.924	-0.031	0.025	0.231	0.901	-0.038	0.062	0.546	0.555	-0.039	0.030	0.192	0.738
<i>Explained</i>																
Cognitive	0.001	0.004	0.727	-0.021	0.000	0.003	0.886	0.013	-0.006	0.009	0.477	0.090	-0.006	0.006	0.330	0.108
Attention Problems	-0.004	0.005	0.505	0.057	0.001	0.003	0.789	-0.023	-0.004	0.008	0.588	0.062	0.000	0.002	0.890	0.006
Conduct Problems	-0.001	0.005	0.777	-0.022	-0.001	0.004	0.740	0.042	-0.002	0.007	0.811	0.024	-0.001	0.004	0.742	0.026
Warmth/Empathy	0.002	0.004	0.569	-0.034	0.004	0.004	0.296	-0.117	-0.002	0.007	0.762	0.030	0.001	0.004	0.811	-0.018
Aggression	-0.003	0.006	0.556	0.054	-0.006	0.008	0.459	0.184	-0.016	0.015	0.267	0.239	-0.007	0.007	0.313	0.140
<i>Unexplained</i>																
Cognitive	-0.001	0.005	0.906	0.010	-0.006	0.007	0.382	0.187	-0.003	0.012	0.799	0.046	-0.001	0.007	0.879	0.020
Attention Problems	-0.004	0.010	0.650	0.069	0.000	0.005	0.980	-0.003	-0.007	0.016	0.657	0.107	-0.001	0.005	0.907	0.010
Conduct Problems	0.002	0.006	0.783	-0.025	0.002	0.005	0.734	-0.047	0.001	0.010	0.960	-0.007	0.002	0.006	0.765	-0.034
Warmth/Empathy	-0.007	0.007	0.335	0.105	0.000	0.004	0.913	0.012	0.014	0.014	0.358	-0.203	0.003	0.008	0.678	-0.064
Aggression	0.001	0.006	0.872	-0.014	0.006	0.009	0.520	-0.171	0.004	0.014	0.742	-0.066	0.001	0.008	0.932	-0.054
Residual	-0.049	0.042	0.239	0.780	-0.031	0.026	0.235	0.923	-0.046	0.069	0.503	0.679	-0.044	0.035	0.211	0.818

Notes: The indices are means of the non-missing items. The fractions are proportions of the total conditional difference in means.